

The 8th KIAS workshop on particle physics and cosmology

Forecast for Higgs boson self coupling measurement at the HL-100 TeV collider.

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Standard Model

Di-Higgs Production

$$-\mathcal{L} = \frac{1}{3!} \left(\frac{3M_H^2}{v} \right) \lambda_{3H} H^3 + g_t^S \frac{m_t}{v} \bar{t} t H$$

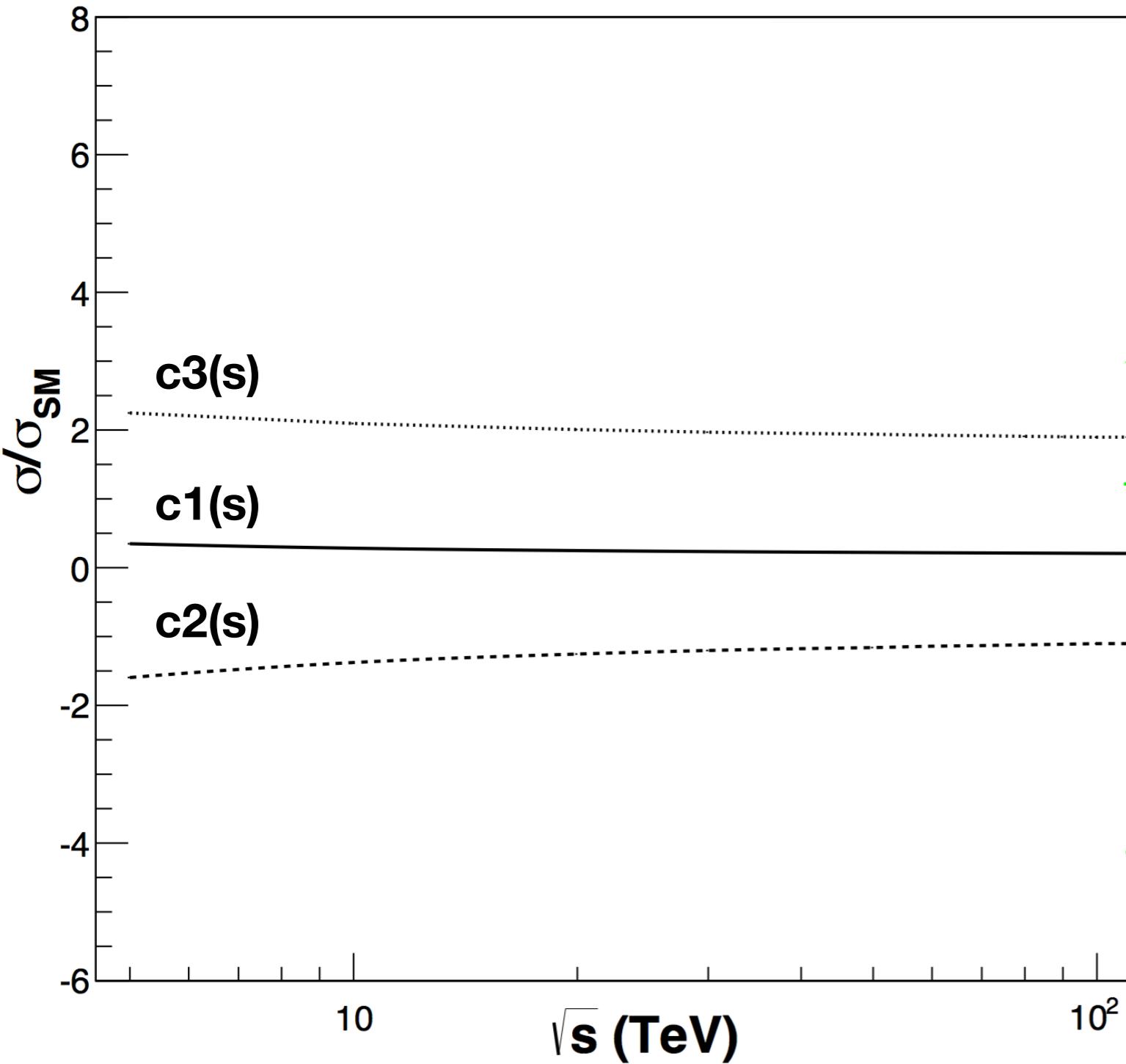


$$\frac{d\hat{\sigma}(gg \rightarrow HH)}{d\hat{t}} = \frac{G_F^2 \alpha_s^2}{512(2\pi)^3} \left[\left| \lambda_{3H} g_t^S D(\hat{s}) F_\Delta^S + (g_t^S)^2 F_\square^{SS} \right|^2 + \left| (g_t^S)^2 G_\square^{SS} \right|^2 \right]$$

$$D(\hat{s}) = \frac{3M_H^2}{\hat{s} - M_H^2 + iM_H\Gamma_H}$$

$$F_\Delta^S = +\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2), \quad F_\square^{SS} = -\frac{2}{3} + \mathcal{O}(\hat{s}/m_Q^2), \quad G_\square^{SS} = \mathcal{O}(\hat{s}/m_Q^2)$$

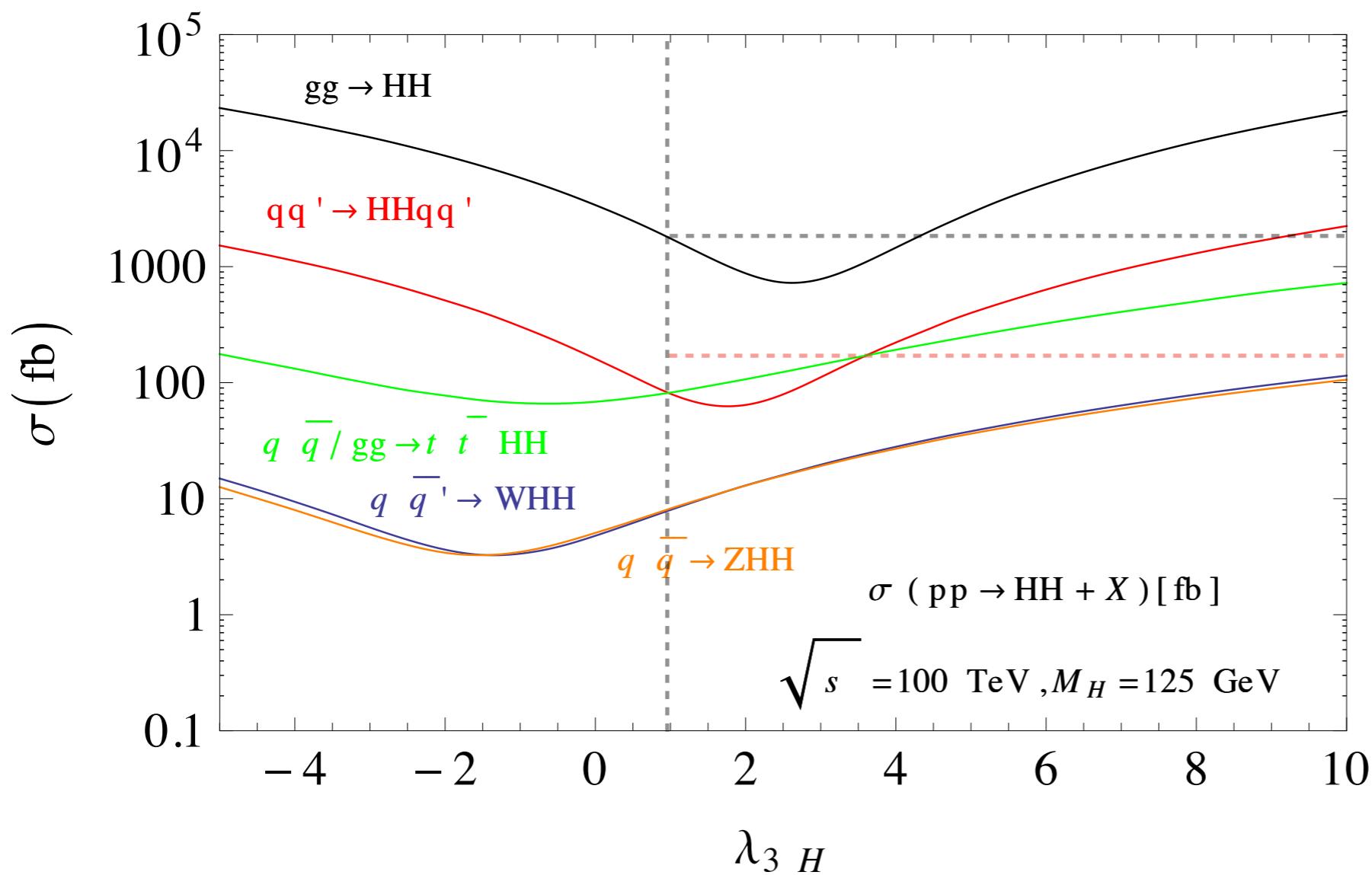
$$\frac{\sigma^{\text{LO}}(gg \rightarrow HH)}{\sigma_{\text{SM}}^{\text{LO}}(gg \rightarrow HH)} = c_1(s) \lambda_{3H}^2 (g_t^S)^2 + c_2(s) \lambda_{3H} (g_t^S)^3 + c_3(s) (g_t^S)^4$$



$c_1(s)$, $c_2(s)$, $c_3(s)$ are related to CM energy \sqrt{s} and kinematic cuts.

\sqrt{s} (TeV)	$c_1(s)$ [$\lambda_{3H}^2 (g_t^S)^2$]	$c_2(s)$ [$\lambda_{3H} (g_t^S)^3$]	$c_3(s)$ [(g_t^S) ⁴]
8	0.300	-1.439	2.139
14	0.263	-1.310	2.047
33	0.232	-1.193	1.961
100	0.208	-1.108	1.900

**Probe Di-Higgs Production :
Higgs boson self coupling
Top Yukawa coupling**



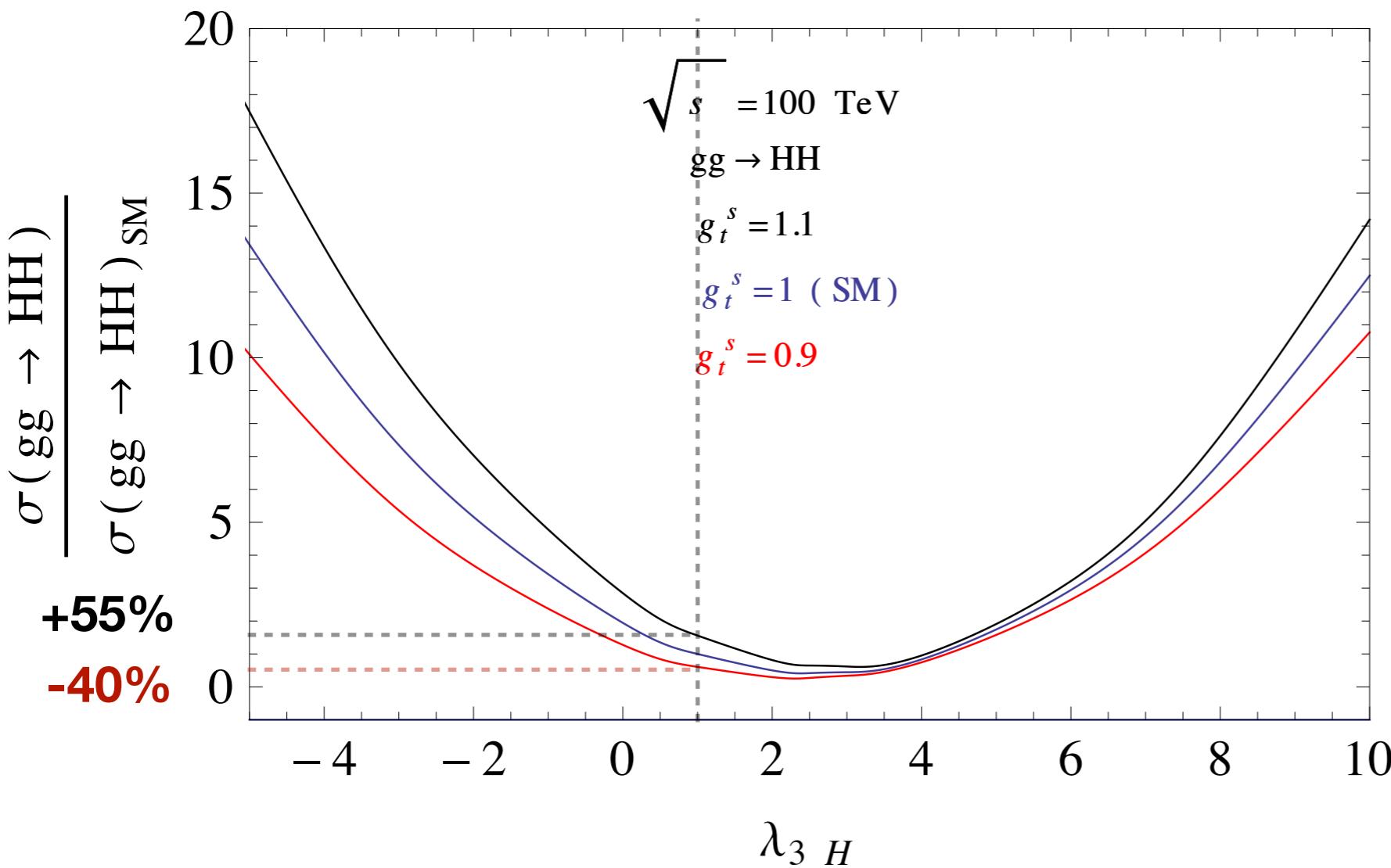
100 TeV $\sigma(p p > h h) :$
1749 fb[1], 1224 fb[2]

14 TeV $\sigma(p p > h h) :$
45.05 fb[1], 36.69 fb[2]

[1] : calculated at NNLO accuracy including NNLL gluon resummation in the infinite top quark mass approximation.

[2] : incorporate the finite top-quark mass effects at NNLO by adopting the FT (Full Theory) approximation.

- [1] D. de Florian and J. Mazzitelli, JHEP 1509, 053 (2015), R. Contino et al., CERN Yellow Report, no. 3, 255 (2017).
- [2] M. Grazzini, G. Heinrich, S. Jones, S. Kallweit, M. Kerner, J. M. Lindert and J. Mazzitelli, JHEP 1805 (2018) 059.



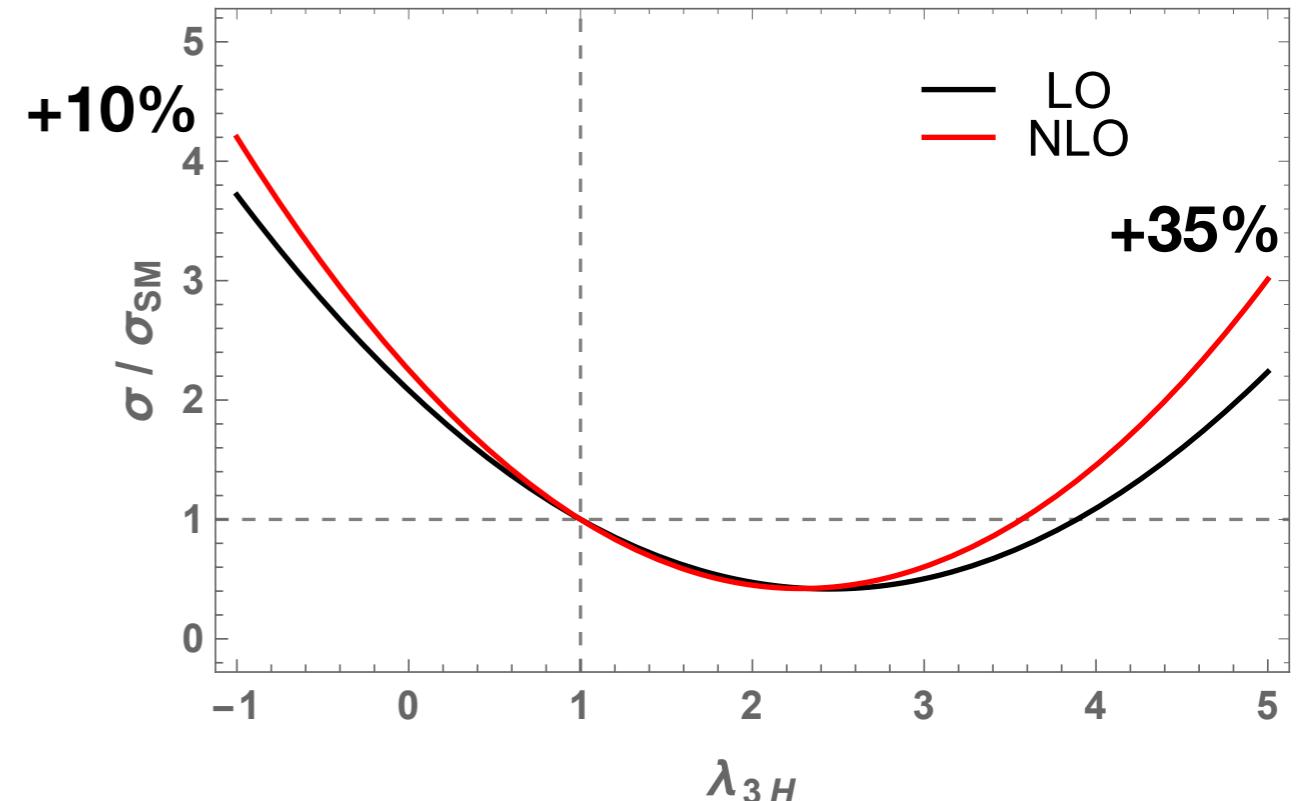
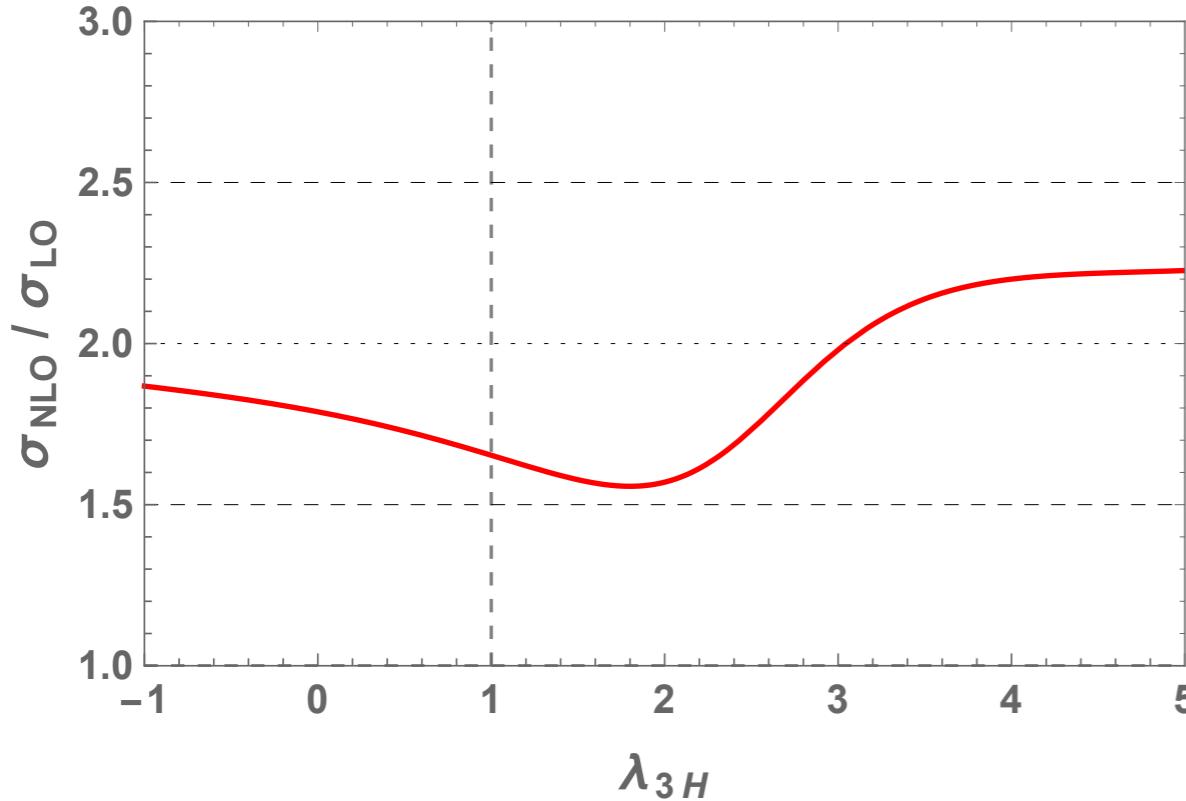
The expected Y_t uncertainty is 1% at the 100-TeV pp colliders [1].

At the HL-LHC, the expected precision of measurement of the top-quark Yukawa coupling (Y_t) is 10% [1].

Without knowing no better than 10% precision of the absolute Y_t , we still considered 10% uncertainty for Y_t at the 100-TeV pp colliders.

[1] M. Vos, arXiv:1701.06537 [hep-ex].

QCD corrections for λ_{3H}



QCD corrections are less significant than the uncertainties associated with the top-Yukawa coupling. In this respect, we have not taken account of the λ_{3H} -dependent QCD corrections on the ratio $\sigma(\text{HH})/\sigma(\text{HH})_{\text{SM}}$ in this work.

Search for Di-Higgs production at collider

	reconstruct τ / W	b-tagging, QCD BG
Decay channels	$HH \rightarrow bb\gamma\gamma$	$HH \rightarrow bb\tau\tau$
Branching ratios	0.263%	7.29%

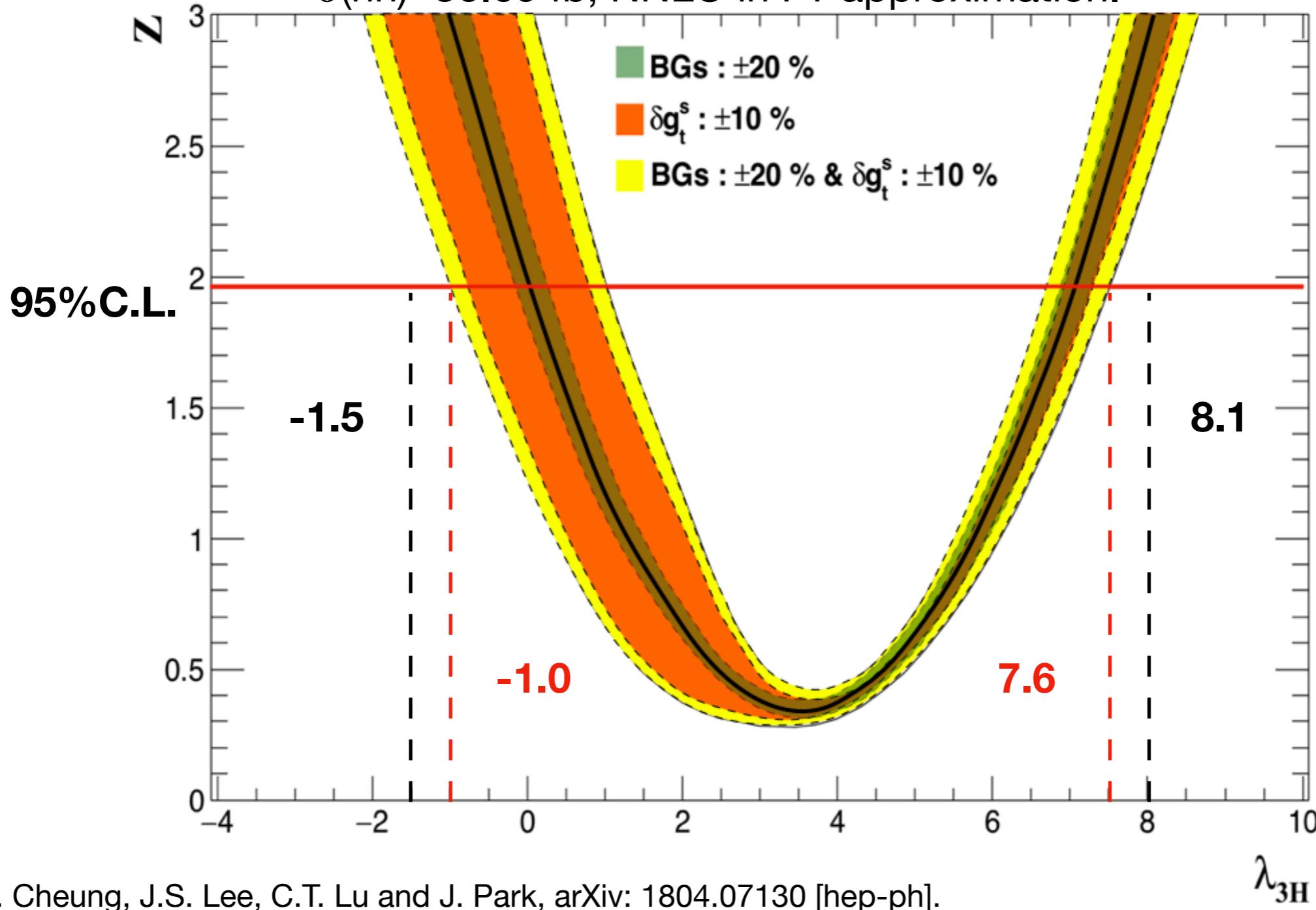
small BR
relatively clean channel
dominate BGs comes from fake photon or b-jet

In our study : $bb\gamma\gamma$ channel

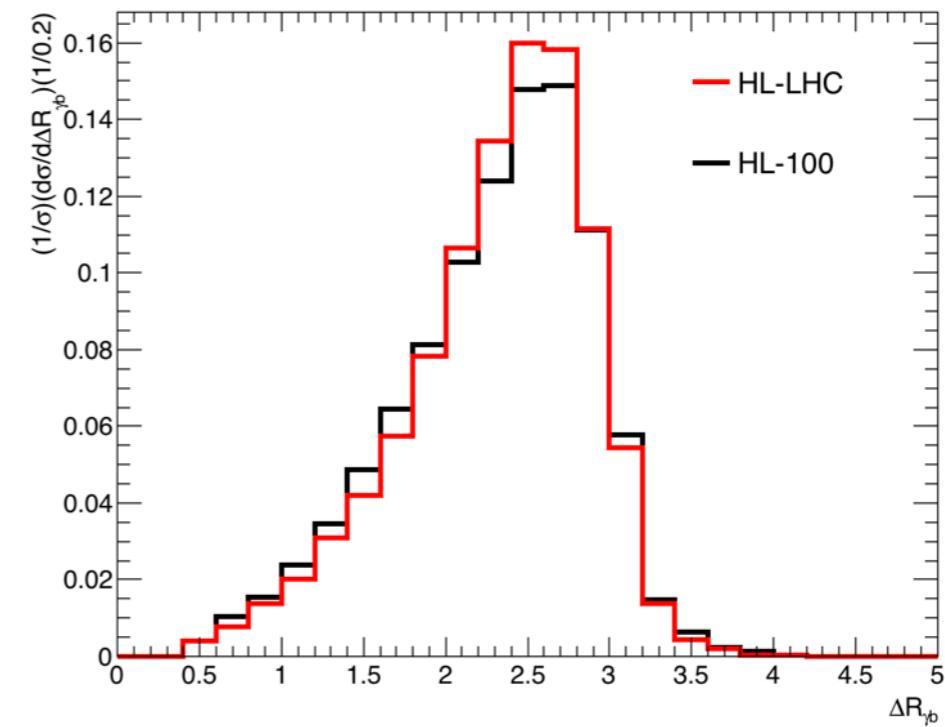
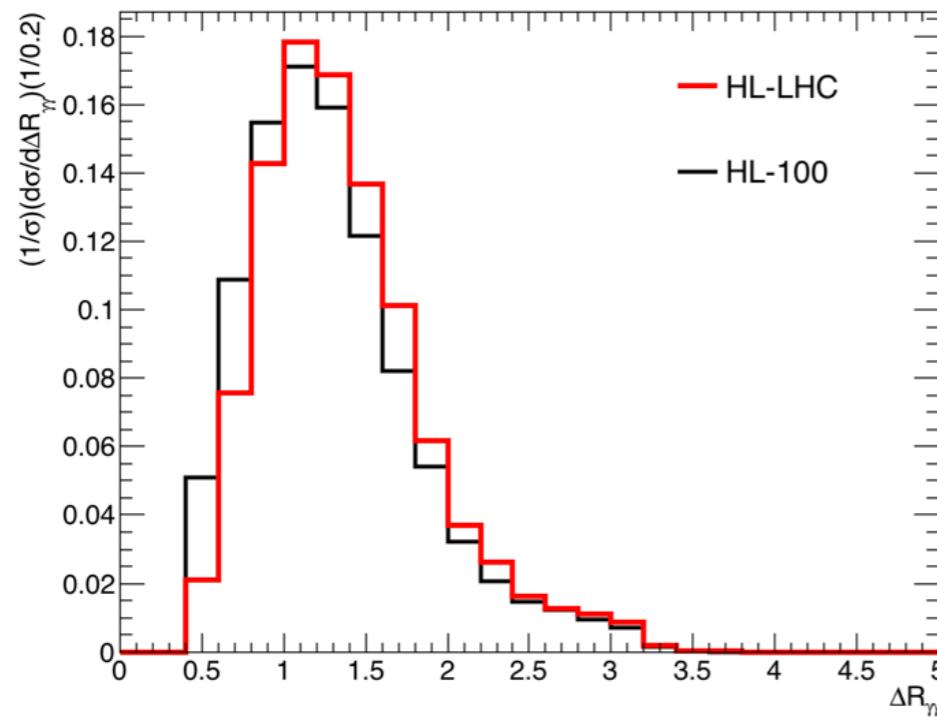
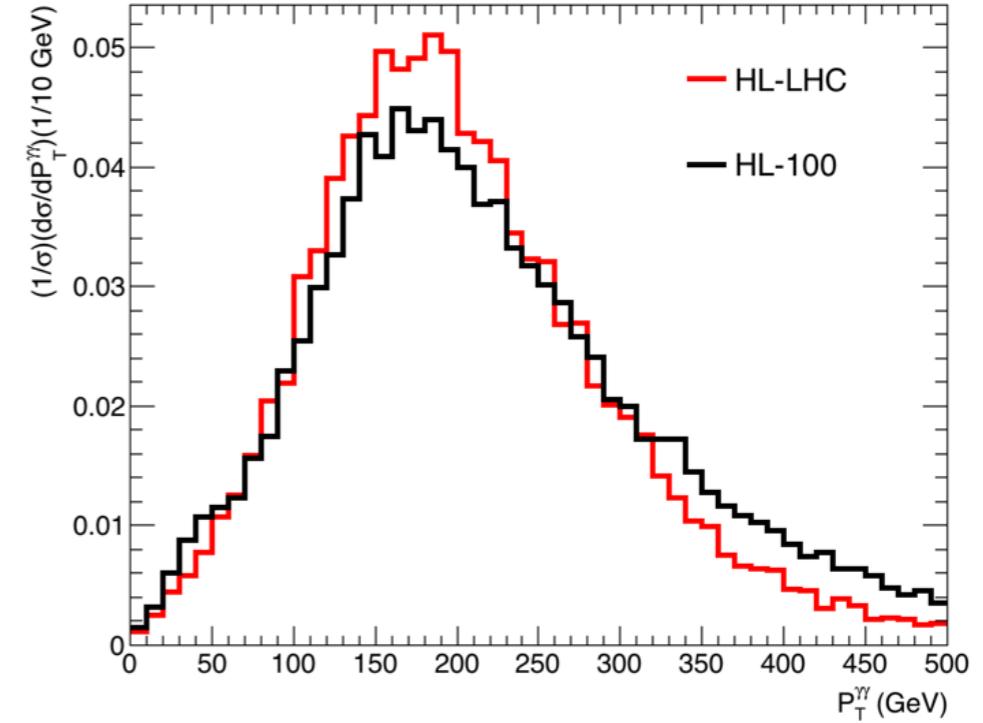
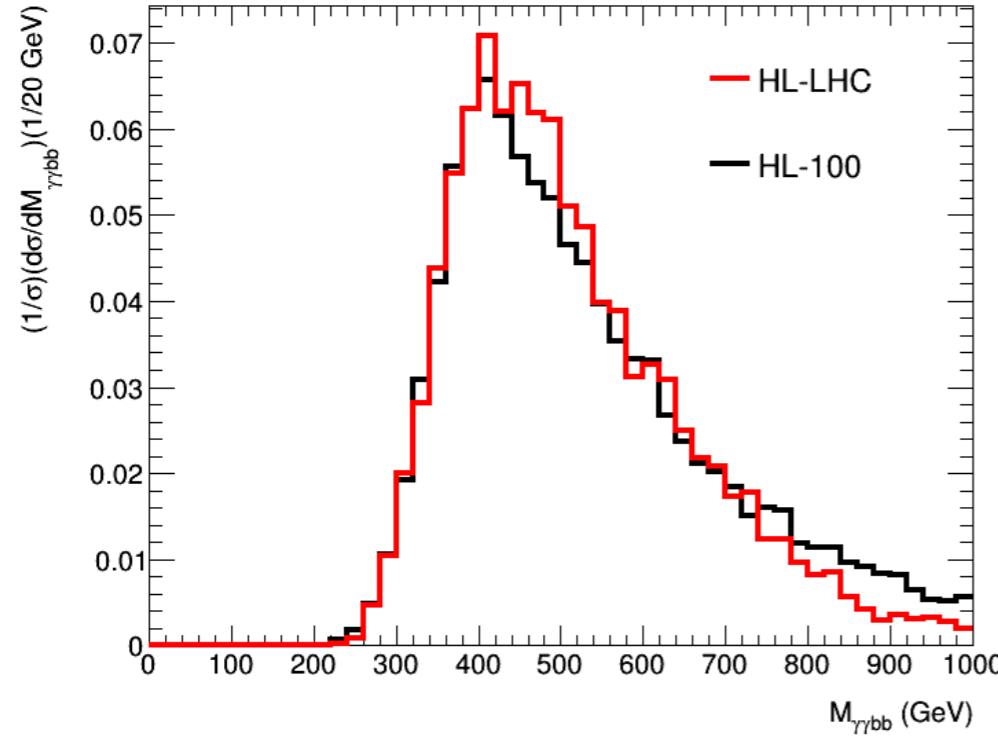
HL-LHC

$\sigma(hh)=45.05 \text{ fb, NNLO +NNLL.}$

$\sigma(hh)=36.69 \text{ fb, NNLO in FT approximation.}$



HL-LHC vs HL-100



$bb\gamma\gamma$ channel BGs

single Higgs

ggH
ttH
ZH
bbH

non-resonant

$bb\gamma\gamma$
cc $\gamma\gamma$
jj $\gamma\gamma$
bbj γ
ccj γ
bbjj

resonant

$Z(bb)\gamma\gamma$
tt
tty

Signal					
Signal process	Generator/Parton Shower	$\sigma \cdot BR$ [fb]	Order	PDF used	
			in QCD		
$gg \rightarrow HH \rightarrow b\bar{b}\gamma\gamma$ [20]	MG5_aMC@NLO/PYTHIA8	4.62	NNLO	NNPDF2.3LO	+NNLL
Backgrounds					
Background(BG)	Process	Generator/Parton Shower	$\sigma \cdot BR$ [fb]	Order	PDF used
			in QCD		
Single-Higgs associated BG	$ggH(\rightarrow \gamma\gamma)$ [20]	POWHEG – BOX/PYTHIA8	1.82×10^3	NNNLO	CT10
	$t\bar{t}H(\rightarrow \gamma\gamma)$ [20]	PYTHIA8/PYTHIA8	7.29×10^1	NLO	
	$ZH(\rightarrow \gamma\gamma)$ [20]	PYTHIA8/PYTHIA8	2.54×10^1	NNLO	
	$b\bar{b}H(\rightarrow \gamma\gamma)$ [37]	PYTHIA8/PYTHIA8	1.96×10^1	NNLO(5FS)	
Non-resonant BG	$b\bar{b}\gamma\gamma$	MG5_aMC@NLO/PYTHIA8	4.93×10^3	LO	CTEQ6L1
	$c\bar{c}\gamma\gamma$	MG5_aMC@NLO/PYTHIA8	4.54×10^4	LO	
	$jj\gamma\gamma$	MG5_aMC@NLO/PYTHIA8	5.38×10^5	LO	
	$b\bar{b}j\gamma$	MG5_aMC@NLO/PYTHIA8	1.44×10^7	LO	
	$c\bar{c}j\gamma$	MG5_aMC@NLO/PYTHIA8	4.20×10^7	LO	
	$b\bar{b}jj$	MG5_aMC@NLO/PYTHIA8	1.60×10^{10}	LO	
$t\bar{t}$ and $t\bar{t}\gamma$ BG [20] (≥ 1 lepton)	$Z(\rightarrow b\bar{b})\gamma\gamma$	MG5_aMC@NLO/PYTHIA8	9.53×10^1	LO	
	$t\bar{t}$	MG5_aMC@NLO/PYTHIA8	1.76×10^7	NLO	CT10
	$t\bar{t}\gamma$	MG5_aMC@NLO/PYTHIA8	4.18×10^4	NLO	CTEQ6L1

[20] R. Contino et al., CERN Yellow Report, no. 3, 255 (2017).

[37] <https://twiki.cern.ch/twiki/bin/view/LHCPhysics/HiggsEuropeanStrategy>.

Background(BG)	Process	Fake Process	Fake rate	
Non-resonant BG	$b\bar{b}\gamma\gamma$	N/A	14 TeV	N/A
	$c\bar{c}\gamma\gamma$	$c \rightarrow b, \bar{c} \rightarrow \bar{b}$	0.125	$(0.1)^2$
	$jj\gamma\gamma$	$c_s \rightarrow b, \bar{c}_s \rightarrow \bar{b}$		$(0.1)^2$
	$b\bar{b}j\gamma$	$j \rightarrow \gamma$	5e-4	1.35×10^{-3}
	$c\bar{c}j\gamma$	$c \rightarrow b, \bar{c} \rightarrow \bar{b}, j \rightarrow \gamma$		$(0.1)^2 \cdot (1.35 \times 10^{-3})$
	$b\bar{b}jj$	$j \rightarrow \gamma, j \rightarrow \gamma$		$(1.35 \times 10^{-3})^2$
	$Z(\rightarrow b\bar{b})\gamma\gamma$	N/A		N/A
$t\bar{t}$	Leptonic decay	$e \rightarrow \gamma, e \rightarrow \gamma$	$(0.02)^2 / 0.02 \cdot 0.05 / (0.05)^2$	
	Semi-leptonic decay	$e \rightarrow \gamma, j \rightarrow \gamma$	$(0.02) \cdot 1.35 \times 10^{-3} / (0.05) \cdot 1.35 \times 10^{-3}$	
$t\bar{t}\gamma$	Leptonic decay	$e \rightarrow \gamma$	0.02/0.05 barrel/endcap	
	Semi-leptonic	$e \rightarrow \gamma$	0.02/0.05	

here we take the separation between the barrel and endcap regions at $|n| = 2$

14 TeV : ATLAS Collaboration, ATL-PHYS-PUB-2017-001.

100 TeV : R. Contino et al., CERN Yellow Report, no. 3, 255 (2017).

Backgrounds: $b\bar{b}\gamma\gamma$ channel

single Higgs non-resonant resonant

$Z \sim S/\sqrt{B}$

	14 TeV (fb)	100 TeV (fb)	HL-100/HL-LHC	$\sqrt{(HL-100/HL-LHC)}$
$HH \rightarrow b\bar{b}\gamma\gamma$	0.12	4.62	38.82	
ggH	120.00	1820.00	15.17	3.89
ttH	1.37	72.90	53.21	7.29
ZH	2.24	25.40	11.34	3.37
bbH	1.26	19.60	15.56	3.94
$bb\gamma\gamma$	140.00	4930.00	35.21	5.93
$cc\gamma\gamma$	1140.00	45400.00	39.82	6.31
$jj\gamma\gamma$	16200.00	538000.00	33.21	5.76
$bbj\gamma$	367000.00	14400000.00	39.24	6.26
$ccj\gamma$	1050000.00	42000000.00	40.00	6.32
$bbjj$	434000000.00	16000000000.00	36.87	6.07
$Z(bb)\gamma\gamma$	5.17	95.30	18.43	4.29
tt	530000.00	17600000.00	33.21	5.76
$t\bar{t}\gamma$	1600.00	41800.00	26.13	5.11

HL-LHC constraint HL-100 measurement

Event generations and detector simulations

Pre-selection cut : $P_{T_j} > 20 \text{ GeV}$, $P_{T_b} > 20 \text{ GeV}$, $P_{T_\gamma} > 25 \text{ GeV}$, $P_{T_l} > 10 \text{ GeV}$,
 $|\eta_j| < 6$, $|\eta_\gamma| < 6$, $|\eta_l| < 6$, $\Delta R_{jj,ll,\gamma\gamma,\gamma j,jl,\gamma l} > 0.4$,
 $M_{jj} > 25 \text{ GeV}$, $M_{bb} > 45 \text{ GeV}$, $60 < M_{\gamma\gamma} < 200 \text{ GeV}$.

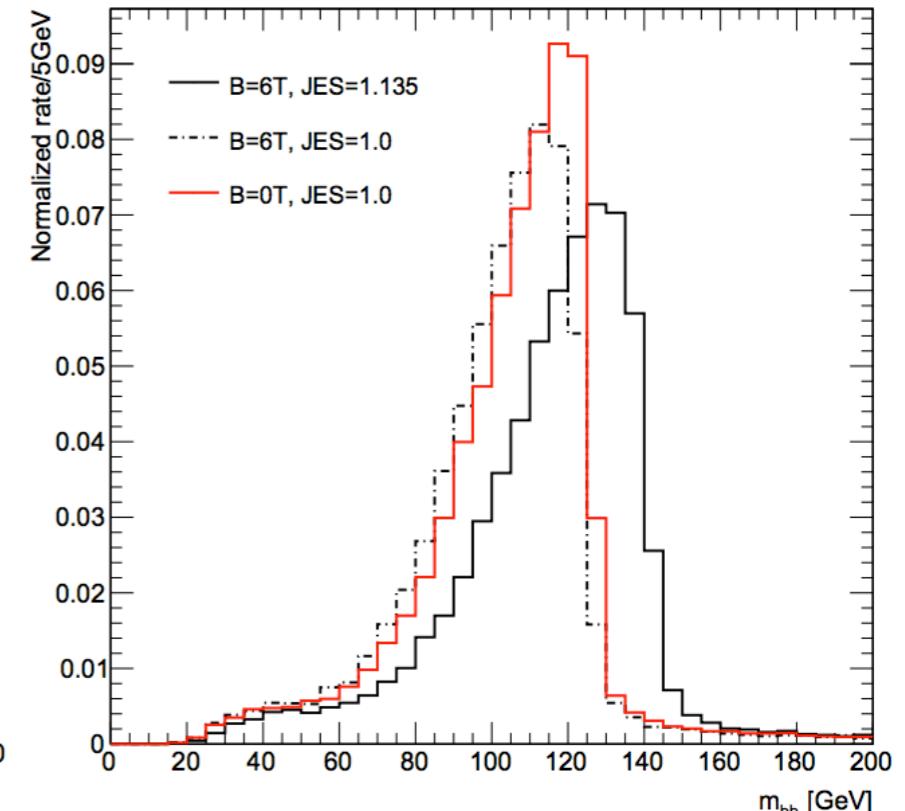
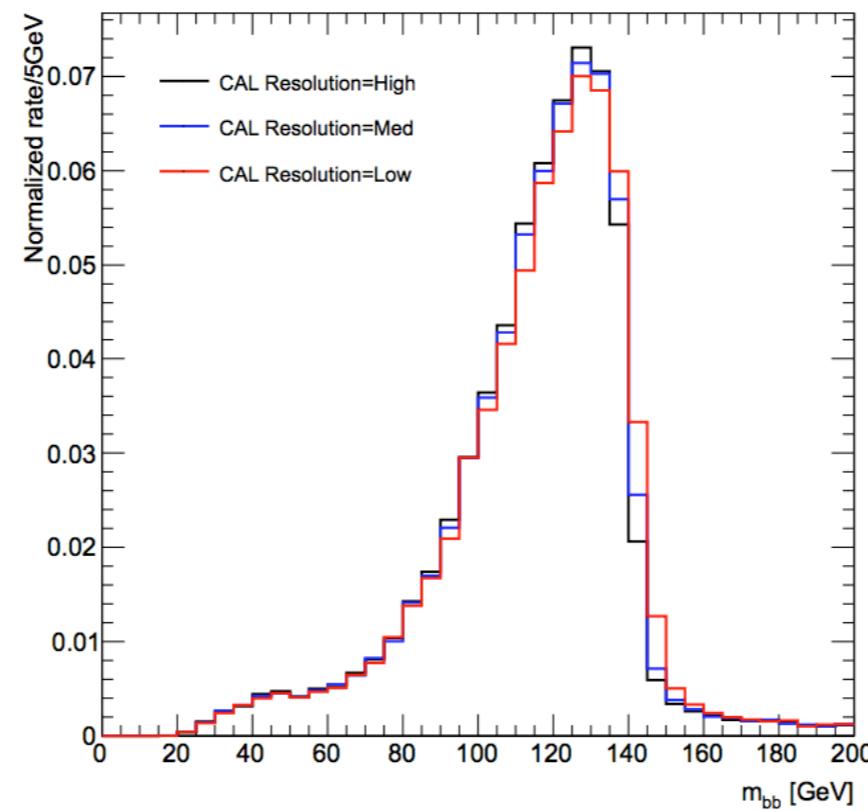
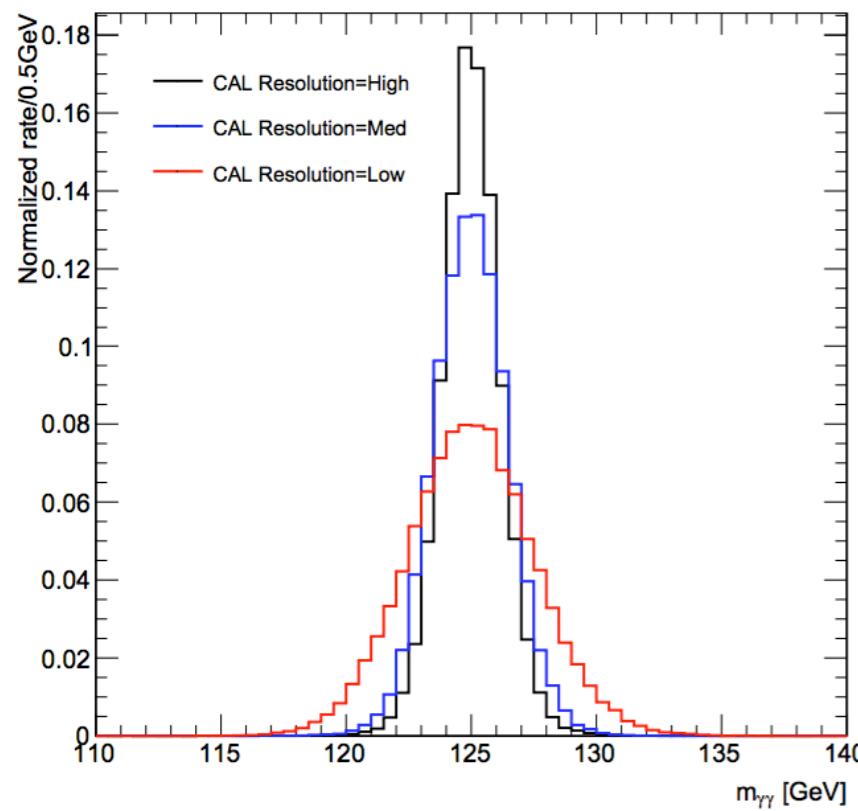
Detector simulation : Delphes3, FCChh template.

ECAL energy resolution $\Delta E/E|_{\text{ECAL}} = \sqrt{0.01^2 + 0.1^2 \text{GeV}/E}$

HCAL energy resolution $\Delta E/E|_{\text{HCAL}} = \begin{cases} \sqrt{0.03^2 + 0.5^2 \text{GeV}/E} & \text{for } |\eta| \leq 4, \\ \sqrt{0.05^2 + 1.0^2 \text{GeV}/E} & \text{for } 4 < |\eta| \leq 6. \end{cases}$

HL-100 TeV

		ECAL				HCAL			
		$ \eta \leq 4$		$4 < \eta \leq 6$		$ \eta \leq 4$		$4 < \eta \leq 6$	
		<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>	<i>a</i>	<i>b</i>
Low		0.02	0.2	0.01	0.1	0.05	1.0	0.05	1.0
Medium		0.01	0.1	0.01	0.1	0.03	0.5	0.05	1.0
High		0.007	0.06	0.01	0.1	0.01	0.3	0.03	0.5



Detector simulation : Delphes3, FCChh template.

Magnetic field 6 T and the jet energy scale of 1.135 is taken to get the correct peak position at MH in the invariant mass distribution of the b-quark pair in the signal process.

For the b -jet tagging efficiency and related jet fake rates, we are taking $\epsilon_b = 75\%$, $P_{c \rightarrow b} = 10\%$, and $P_{j \rightarrow b} = 1\%$ [20].

For the photon efficiency and jet fake rate, we are taking: $\epsilon_\gamma = 95\% (|\eta_\gamma| \leq 1.5)$, $90\% (1.5 < |\eta_\gamma| \leq 4)$, $80\% (4 < |\eta_\gamma| \leq 6)$, and $P_{j \rightarrow \gamma} = 1.35 \times 10^{-3}$ [20]. For the $e \rightarrow \gamma$ fake rate, with a separation between the barrel and endcap regions at $|\eta| = 2$, we take $P_{e \rightarrow \gamma} = 2\% (5\%)$ in the barrel (endcap) region as a reference [30] .

$$p_{j \rightarrow \gamma} = \alpha \exp(-p_{T,j}/\beta), \quad (44)$$

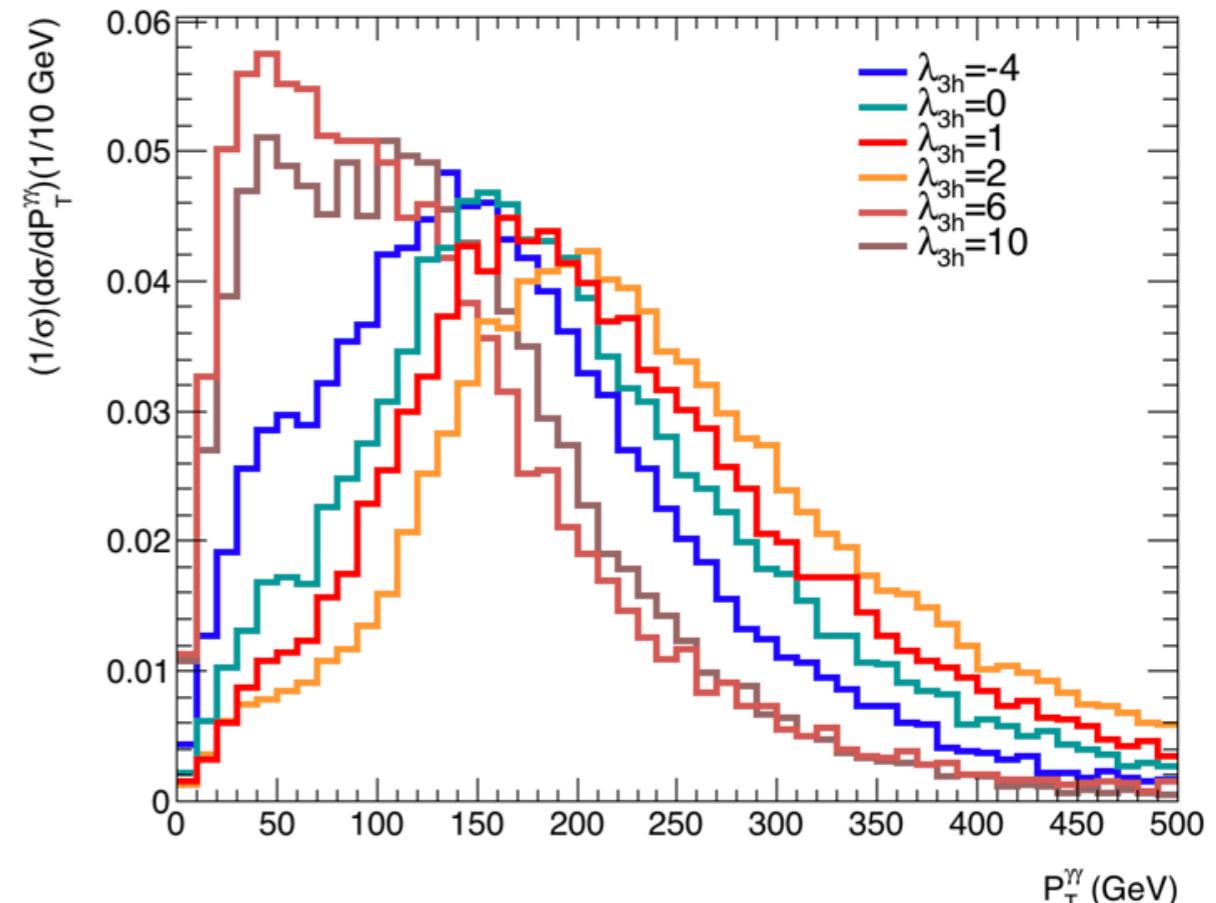
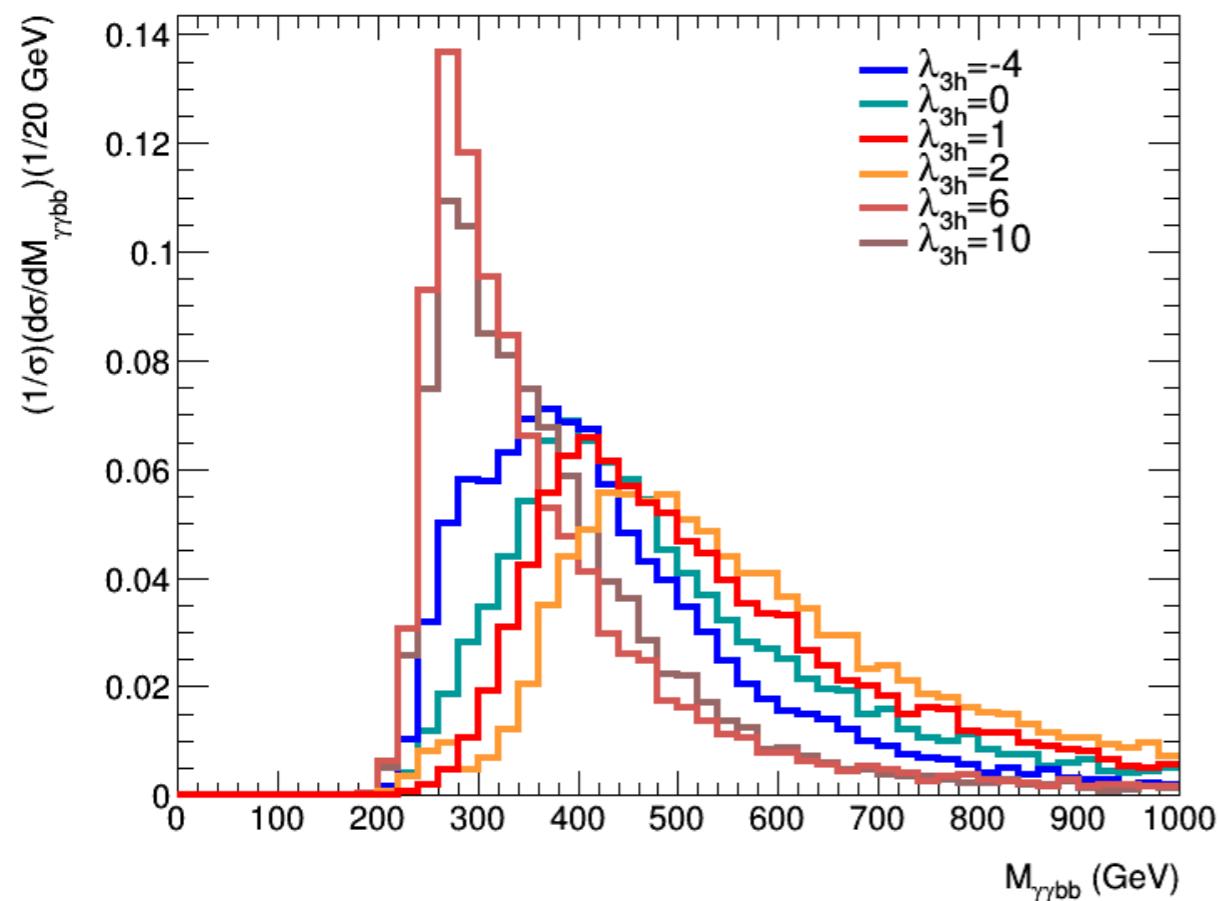
where α and β are parameters whose benchmark values are set to $\alpha = 0.01$ and $\beta = 30$ GeV. Photons

[20] R. Contino et al., CERN Yellow Report, no. 3, 255 (2017)

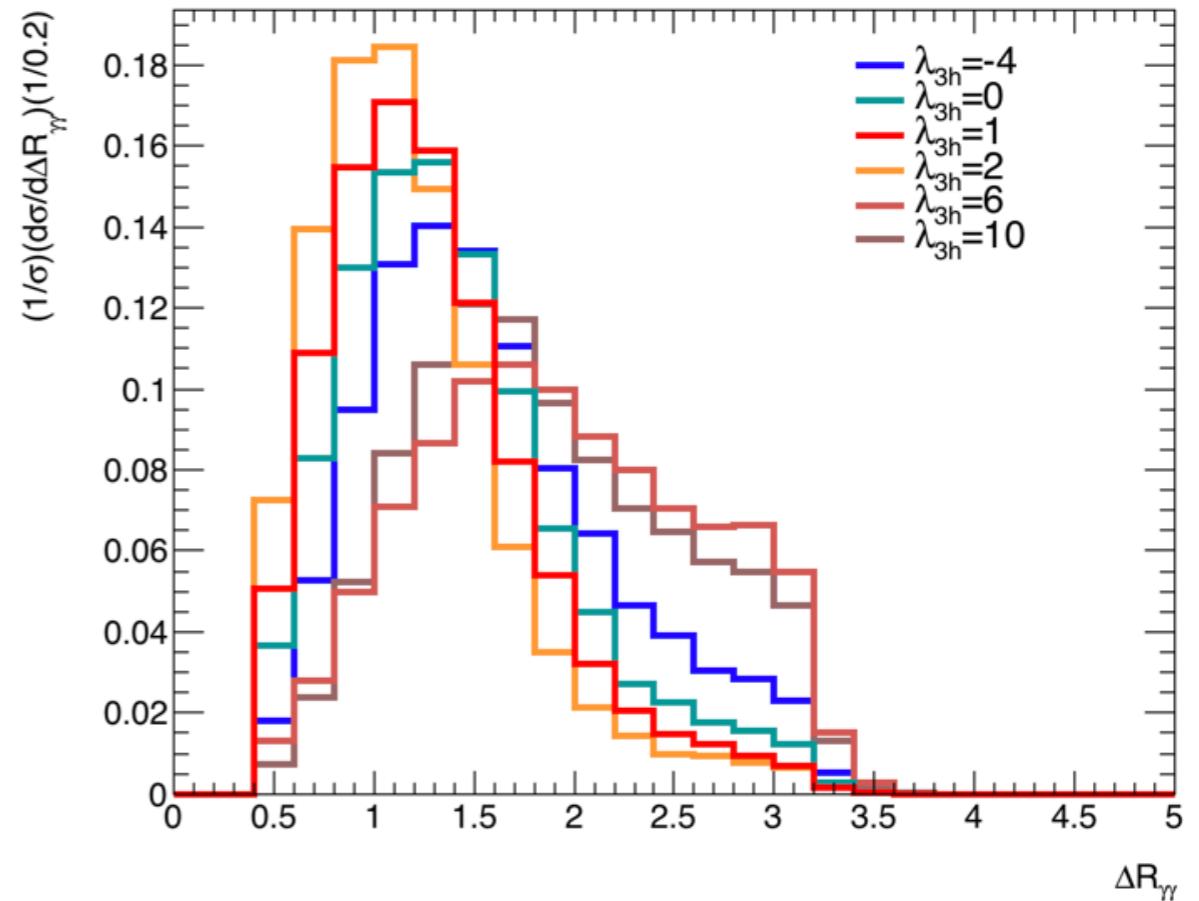
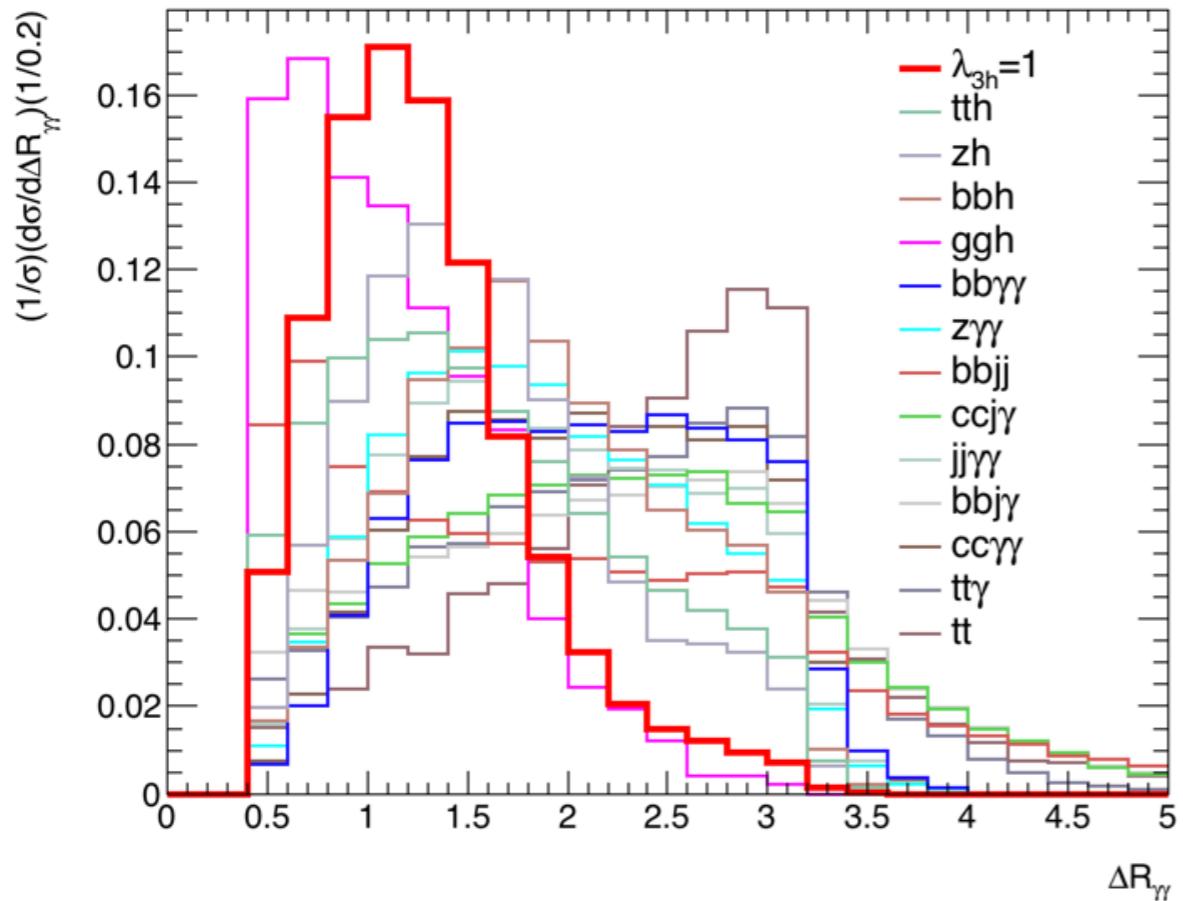
[30] ATLAS Collaboration, ATL-PHYS-PUB-2017-001

100 TeV $\sigma(h h)_{\text{SM}}$: 1749 fb, NNLO+NNLL

λ_{3H}	-4	0	1	2	6	10
$\sigma \cdot BR(HH \rightarrow b\bar{b}\gamma\gamma)$ [fb]	46.97	8.99	4.62	2.32	13.61	57.78



Sequence	Event Selection Criteria at the HL-100 TeV hadron collider
1	Di-photon trigger condition, ≥ 2 isolated photons with $P_T > 30$ GeV, $ \eta < 5$
2	≥ 2 isolated photons with $P_T > 40$ GeV, $ \eta < 3$, $\Delta R_{j\gamma} > 0.4$
3	≥ 2 jets identified as b-jets with leading(subleading) $P_T > 50(40)$ GeV, $ \eta < 3$
4	Events are required to contain ≤ 5 jets with $P_T > 40$ GeV within $ \eta < 5$
5	No isolated leptons with $P_T > 40$ GeV, $ \eta < 3$
6	$0.4 < \Delta R_{b\bar{b}} < 3.0$, $0.4 < \Delta R_{\gamma\gamma} < 3.0$
7	$122.5 < M_{\gamma\gamma}/\text{GeV} < 127.5$ and $90 < M_{b\bar{b}}/\text{GeV} < 150$
8	$P_T^{\gamma\gamma} > 100$ GeV, $P_T^{b\bar{b}} > 100$ GeV

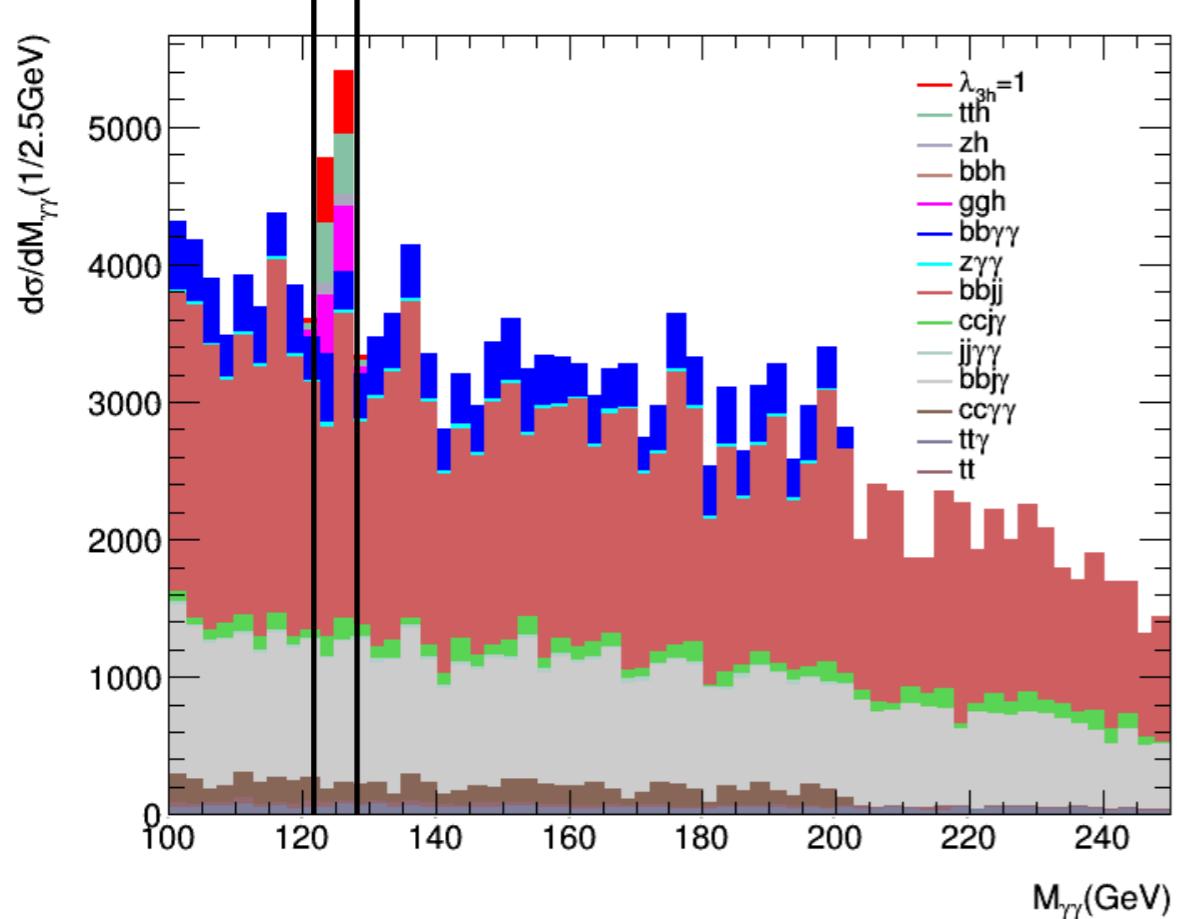


λ_{3H}	-4		0		1		2		6		10	
Cross section (fb)	46.97		8.99		4.62		2.32		13.61		57.78	
Cuts	Eff.%	No.#	%	No.#	%	No.#	%	#	%	#	%	#
1. diphoton trigger	56.06	78988	57.78	15582	58.99	8176	60.00	4176	53.44	21818	53.82	93293
2. ≥ 2 isolated photons	36.31	51158	39.21	10575	41.29	5722	43.40	3021	32.39	13225	32.94	57105
3-1. jet candidates	29.07	40965	32.77	8838	35.36	4901	37.94	2641	23.87	9746	24.74	42881
3-2 ≥ 2 two b-jet	9.57	13492	11.41	3076	12.75	1767	14.18	987	7.31	2986	7.65	13252
4. no. of jets ≤ 5	9.03	12724	10.60	2860	11.79	1634	13.04	907	6.99	2856	7.29	12638
5. lepton veto	9.03	12724	10.60	2860	11.79	1634	13.04	907	6.99	2856	7.29	12637
6. $\Delta R_{\gamma\gamma,bb}$ cut	8.32	11730	10.08	2718	11.34	1572	12.57	875	5.92	2419	6.39	11023
7-1. Higgs mass window $M_{\gamma\gamma}$	7.78	10968	9.35	2523	10.51	1456	11.57	805	5.55	2268	5.97	10341
7-2. Higgs mass window M_{bb}	6.14	8650	7.32	1974	8.23	1140	9.08	632	4.48	1830	4.77	8264
8. $p_T_{\gamma\gamma}, p_T_{bb}$ cuts	3.98	5604	5.61	1514	6.79	941	8.01	557	1.84	753	2.21	3838
other/barrel ratio	31.64%		30.14%		30.05%		29.18%		33.03%		31.26%	

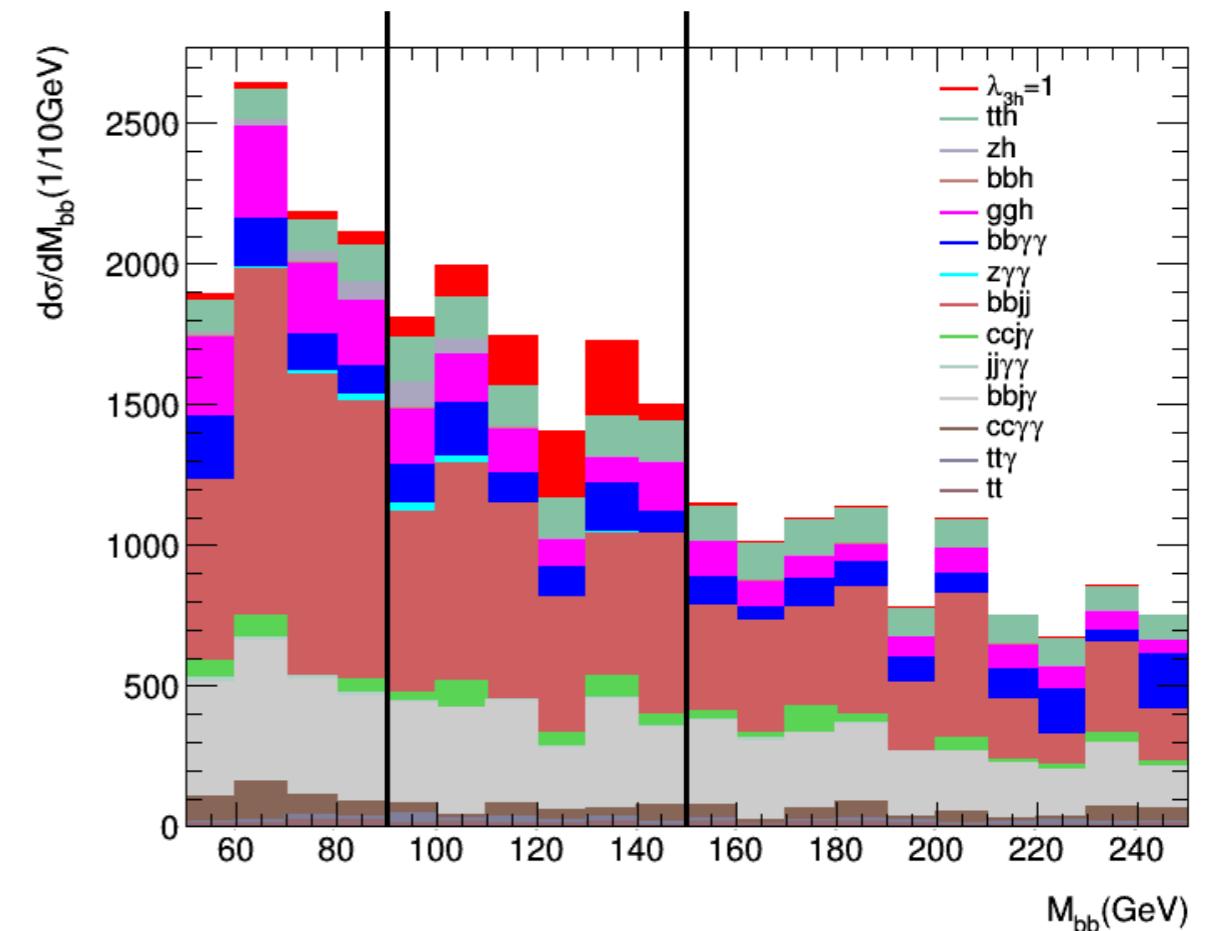
[1] : NNLO+NNLL, infinite top mass.

[2] : NNLO in FT approximation, finite top mass.

122.5 - 127.5 GeV



90 - 150 GeV



Expected yields (3000 fb^{-1})	Total	Barrel-barrel	Other (End-cap)	Ratio (O/B)	# of Gen. Events
Samples					
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = -4$	5604.46 ± 63.36	4257.36 ± 57.90	1347.10 ± 23.22	0.32 ± 0.007	3×10^5
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = 0$	1513.56 ± 14.81	1163.04 ± 14.09	350.52 ± 3.57	0.30 ± 0.005	3×10^5
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = 1$	941.37 ± 7.65	723.86 ± 6.64	217.51 ± 3.66	0.30 ± 0.006	3×10^5
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = 2$	557.36 ± 1.93	431.45 ± 1.87	125.91 ± 1.21	0.29 ± 0.003	3×10^5
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = 6$	753.18 ± 6.02	566.18 ± 5.59	187.00 ± 5.33	0.33 ± 0.010	3×10^5
$H(b\bar{b})H(\gamma\gamma), \lambda_{3H} = 10$	3838.33 ± 36.82	2924.25 ± 32.11	914.08 ± 28.01	0.31 ± 0.010	3×10^5
$gg H(\gamma\gamma)$	890.47 ± 72.91	742.97 ± 58.43	147.50 ± 20.51	0.20 ± 0.03	10^6
$t\bar{t} H(\gamma\gamma)$	868.73 ± 8.53	659.33 ± 12.94	209.40 ± 7.04	0.32 ± 0.01	9.63×10^5
$Z H(\gamma\gamma)$	168.86 ± 5.91	122.91 ± 4.68	45.95 ± 1.69	0.37 ± 0.02	10^6
$b\bar{b} H(\gamma\gamma)$	9.82 ± 0.59	7.00 ± 0.58	2.82 ± 0.25	0.40 ± 0.05	10^6
$b\bar{b}\gamma\gamma$	770.42 ± 23.48	514.96 ± 20.81	255.46 ± 15.10	0.50 ± 0.04	1.1×10^7
$c\bar{c}\gamma\gamma$	222.88 ± 40.55	111.44 ± 32.55	111.44 ± 26.92	1.00 ± 0.38	1.1×10^7
$jj\gamma\gamma$	32.28 ± 3.23	20.98 ± 3.99	11.30 ± 2.34	0.54 ± 0.15	10^7
$b\bar{b}j\gamma$	1829.13 ± 75.08	1288.34 ± 45.27	540.79 ± 49.79	0.42 ± 0.04	1.1×10^7
$c\bar{c}j\gamma$	293.81 ± 40.11	216.49 ± 36.71	77.32 ± 32.97	0.36 ± 0.16	1.1×10^7
$b\bar{b}jj$	3569.73 ± 209.93	2294.83 ± 207.69	1274.90 ± 189.68	0.56 ± 0.10	3.43×10^6
$Z(b\bar{b})\gamma\gamma$	54.87 ± 3.79	35.72 ± 3.36	19.15 ± 2.02	0.54 ± 0.08	10^6
$t\bar{t} (\geq 1 \text{ leptons})$	59.32 ± 7.40	38.32 ± 5.79	21.00 ± 5.61	0.55 ± 0.17	1.1×10^7
$t\bar{t}\gamma (\geq 1 \text{ leptons})$	105.68 ± 8.22	62.53 ± 5.07	43.15 ± 7.95	0.69 ± 0.14	10^6
Total Background	8876.00 ± 243.07	6115.82 ± 227.41	2760.18 ± 202.67	0.45 ± 0.04	
Significance Z	9.823	9.082	4.087		
Combined significance			9.959		

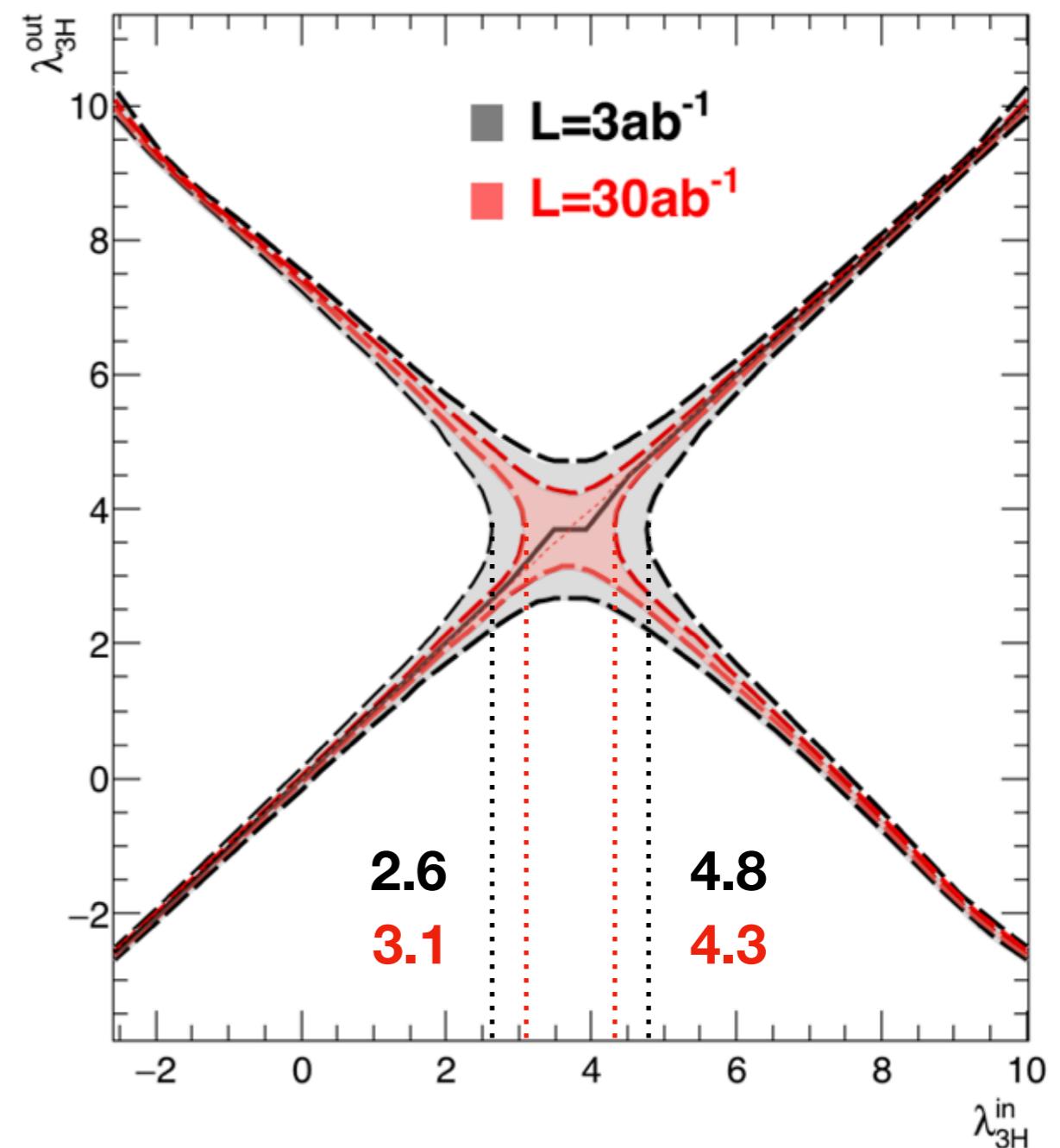
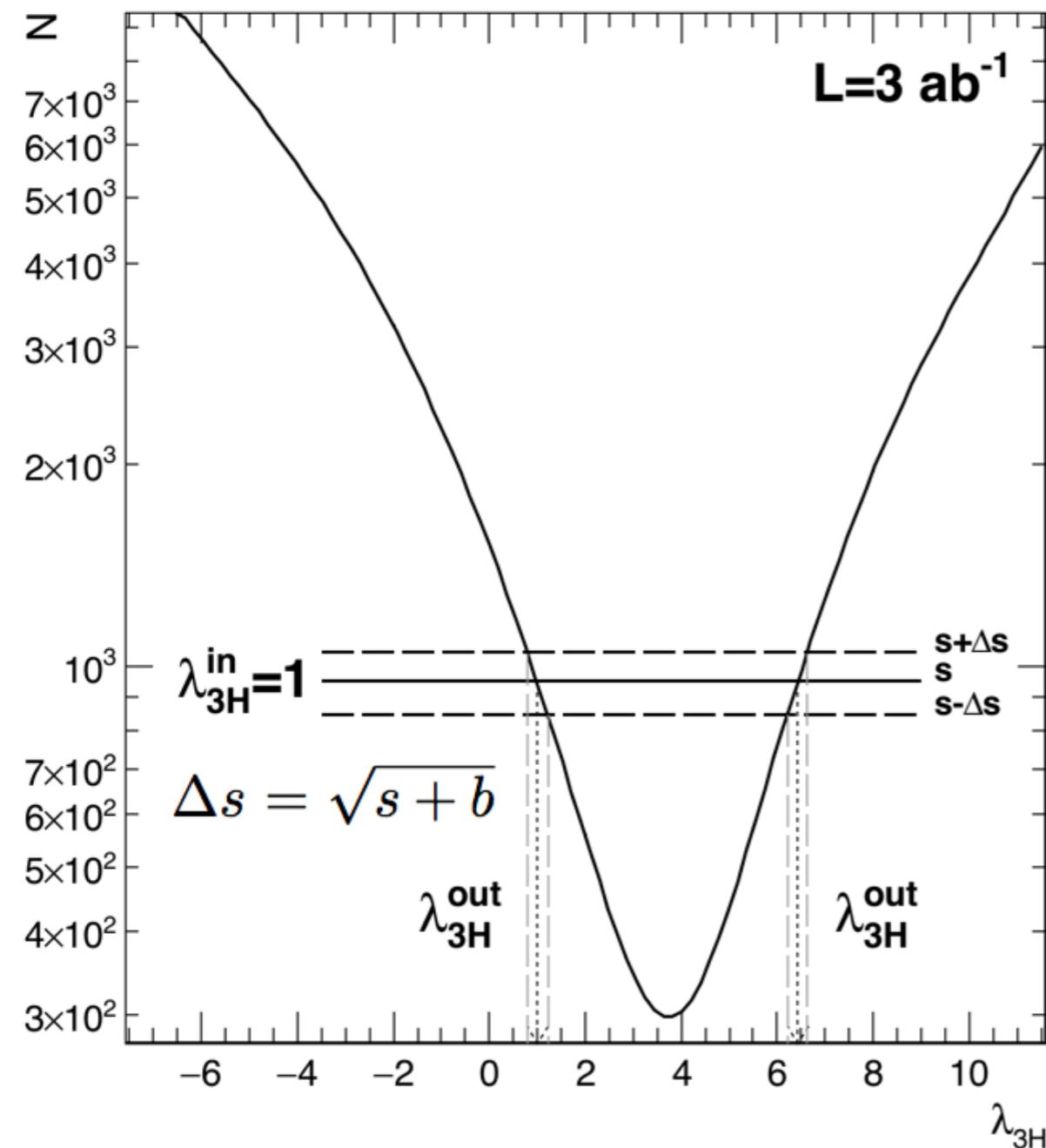
$\lambda_{3H} = 1$

λ_{3H}	-4	0	1	2	6	10
Z[1]	53.766	15.416	9.681	5.770	7.770	37.726
Z[2]	38.503	10.871	6.808	4.049	5.459	26.856

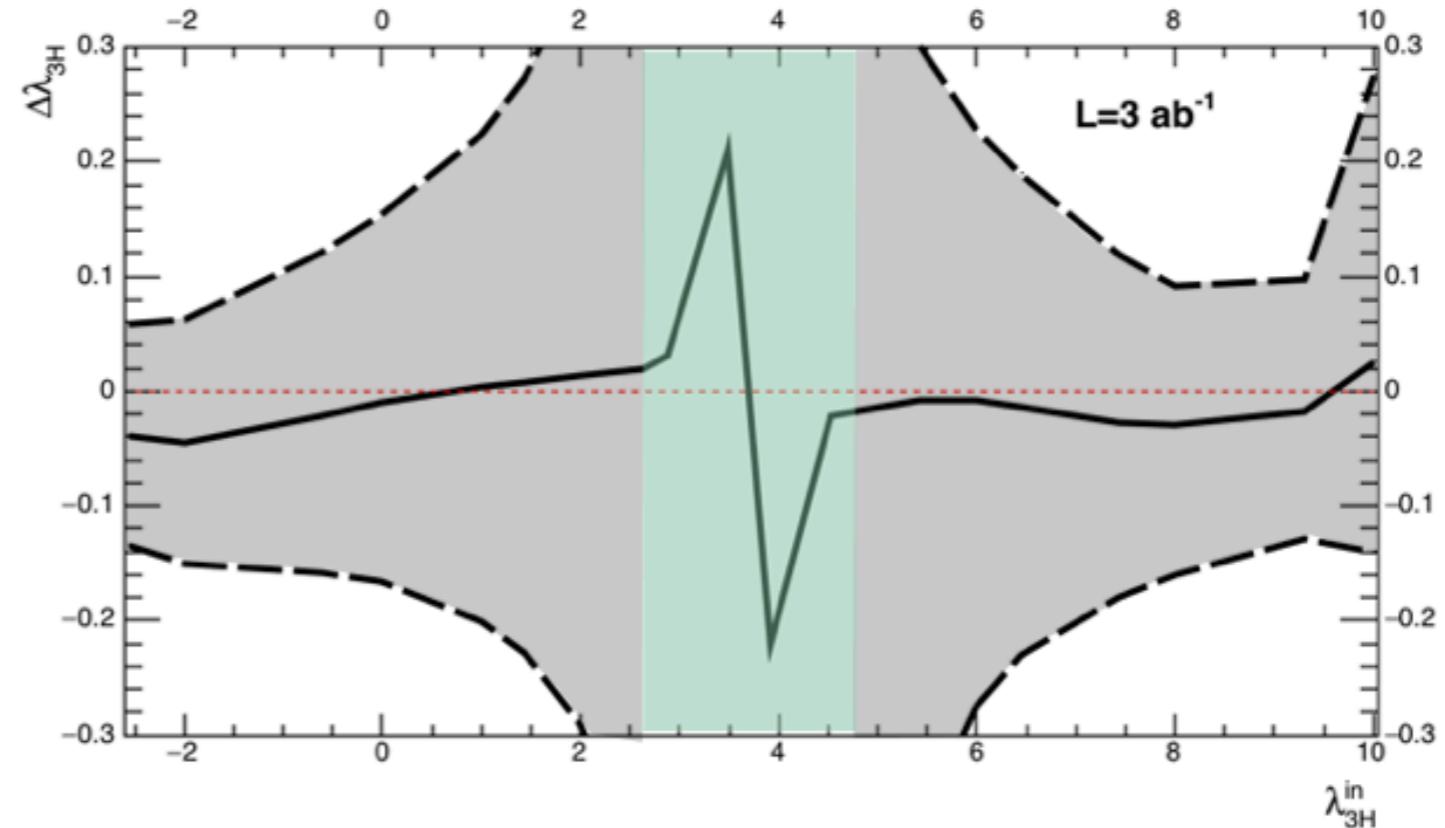
λ_{3H}	-4		0		1		2		6		10	
Cross section (fb)	46.97		8.99		4.62		2.32		13.61		57.78	
Cuts	Eff.%	No.#	%	No.#	%	No.#	%	#	%	#	%	#
1. diphoton trigger	56.06	78988	57.78	15582	58.99	8176	60.00	4176	53.44	21818	53.82	93293
2. ≥ 2 isolated photons	36.31	51158	39.21	10575	41.29	5722	43.40	3021	32.39	13225	32.94	57105
3-1. jet candidates	29.07	40965	32.77	8838	35.36	4901	37.94	2641	23.87	9746	24.74	42881
3-2 ≥ 2 two b-jet	9.57	13492	11.41	3076	12.75	1767	14.18	987	7.31	2986	7.65	13252
4. no. of jets ≤ 5	9.03	12724	10.60	2860	11.79	1634	13.04	907	6.99	2856	7.29	12638
5. lepton veto	9.03	12724	10.60	2860	11.79	1634	13.04	907	6.99	2856	7.29	12637
6. $\Delta R_{\gamma\gamma,bb}$ cut	8.32	11730	10.08	2718	11.34	1572	12.57	875	5.92	2419	6.39	11023
7-1. Higgs mass window $M_{\gamma\gamma}$	7.78	10968	9.35	2523	10.51	1456	11.57	805	5.55	2268	5.97	10341
7-2. Higgs mass window M_{bb}	6.14	8650	7.32	1974	8.23	1140	9.08	632	4.48	1830	4.77	8264
8. $p_{T_{\gamma\gamma}}, p_{T_{bb}}$ cuts	3.98	5604	5.61	1514	6.79	941	8.01	557	1.84	753	2.21	3838
other/barrel ratio	31.64%		30.14%		30.05%		29.18%		33.03%		31.26%	

[1] : NNLO+NNLL, infinite top mass.

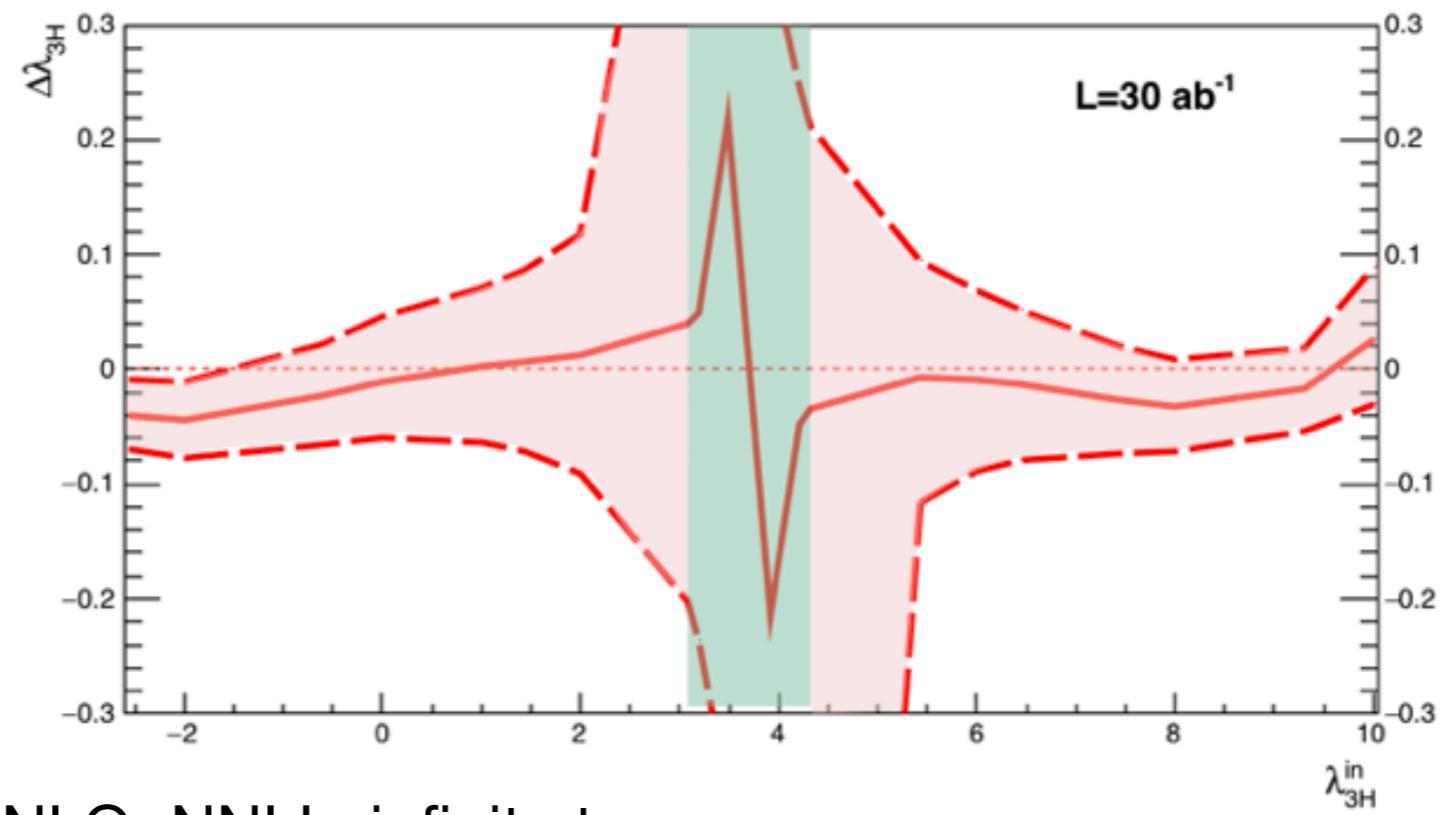
[2] : NNLO in FT approximation, finite top mass.



**3ab⁻¹ : $2.6 \lesssim \lambda_{3H} \lesssim 4.8$,
 $\lambda_{3H} = 1$ accuracy 20%**

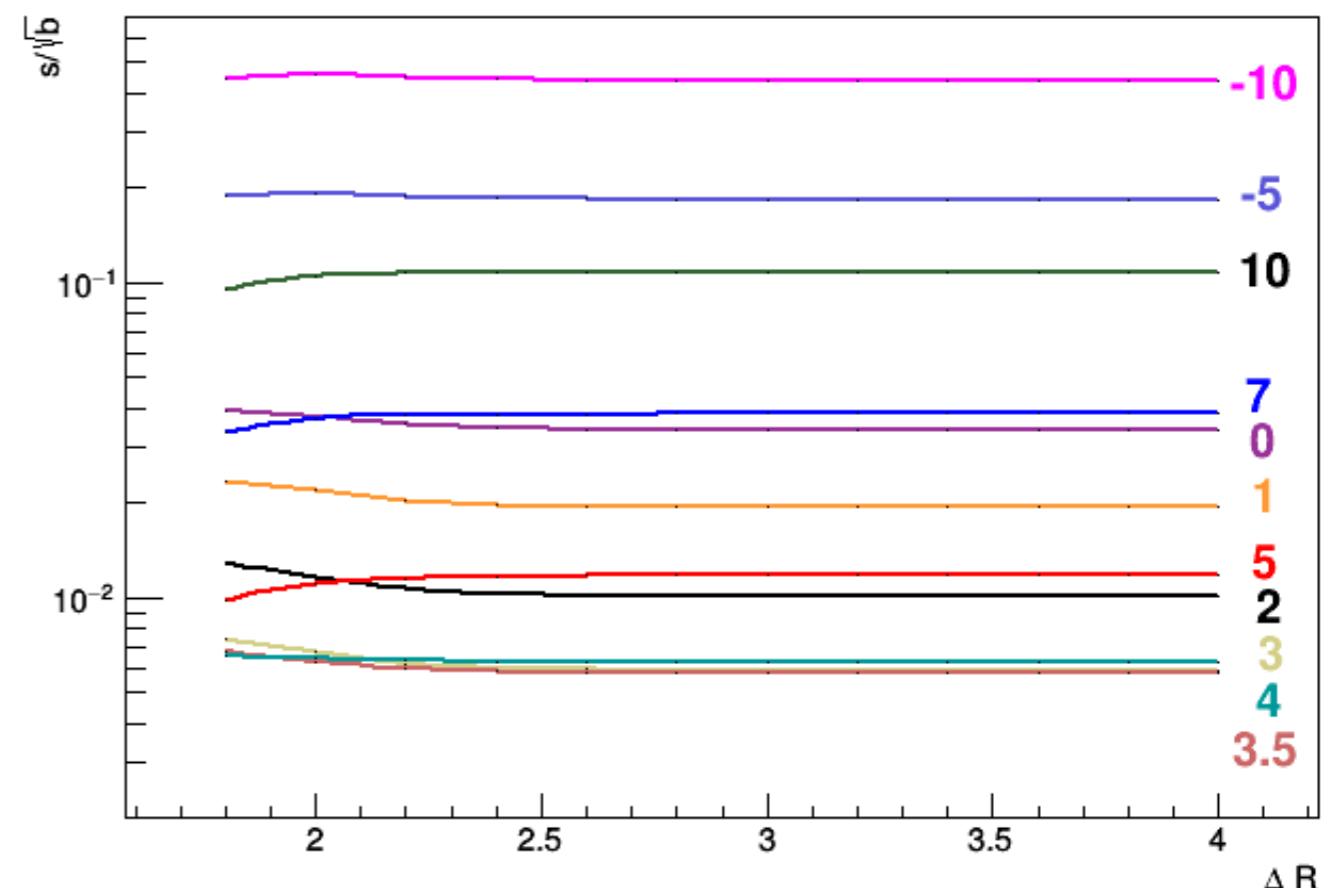
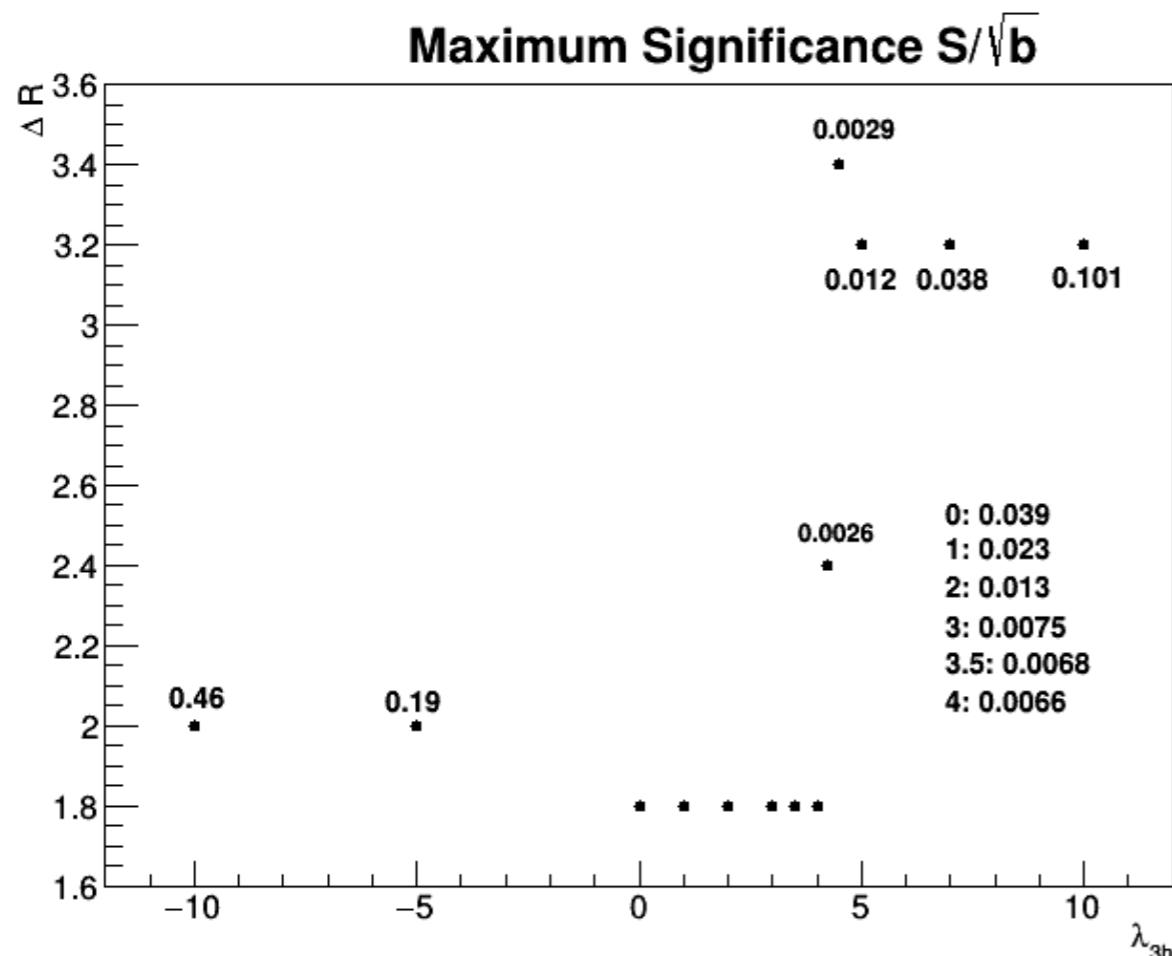


**30ab⁻¹ : $3.1 \lesssim \lambda_{3H} \lesssim 4.3$,
 $\lambda_{3H} = 1$ accuracy 7%**

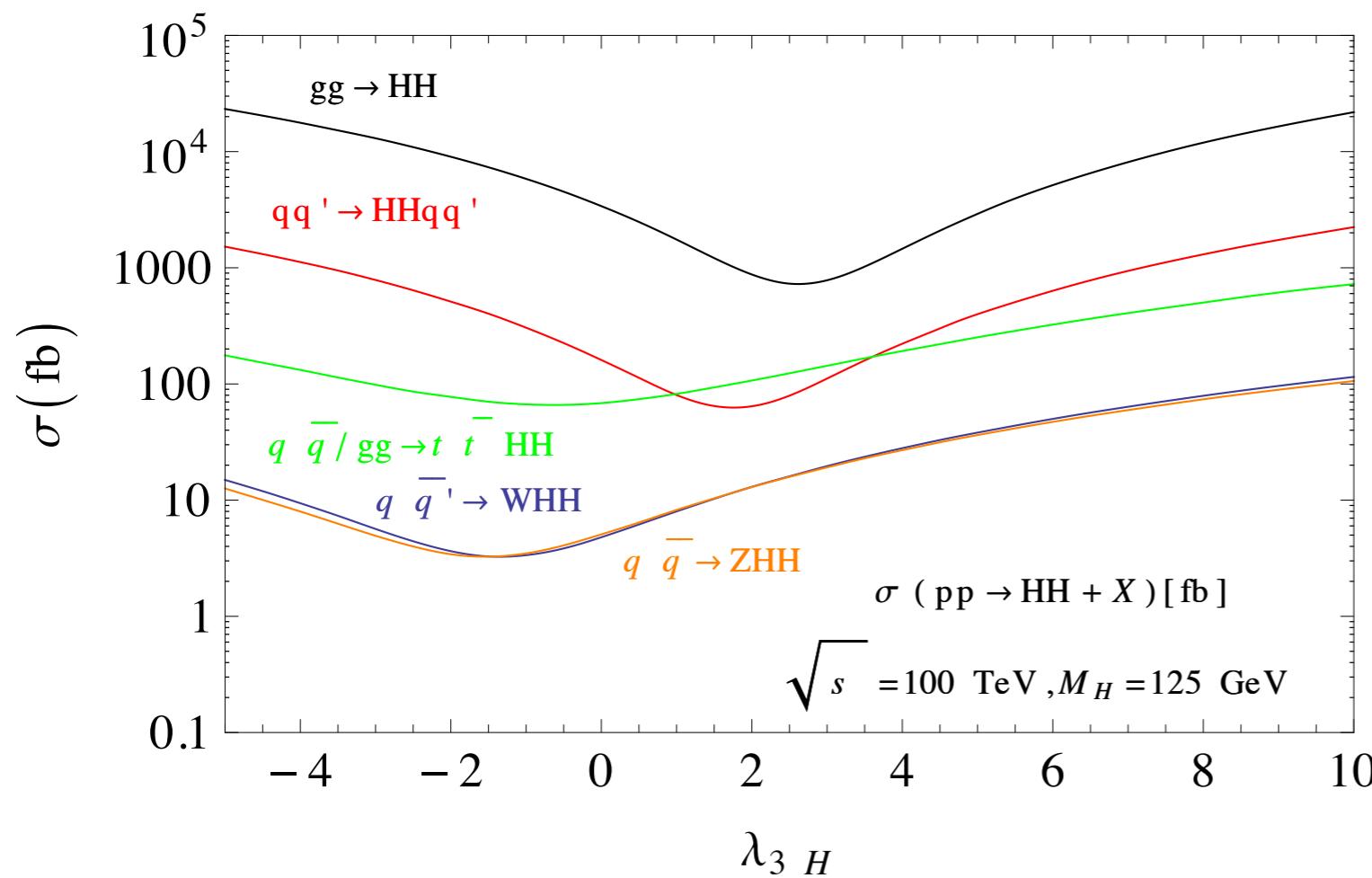


[1] : NNLO+NNLL, infinite top mass.

Significance for different λ_{3H} with varying ΔR cuts at HL-LHC



Conclusion



1. **100 TeV 3ab-1 : $2.6 \leq \lambda_{3H} \leq 4.8$, $\lambda_{3H}=1$ accuracy 20%.**
2. **the $\sigma(hh)$ minimum falls on different λ_{3H} for different production channel, i.e. VHH channel.**
3. **VBF channel cross section is $\sim O(10)$ smaller, but two energetic jet help to reduce BG.**
4. **Deep learning study can help to increase the efficiency, i.e. improve b-tagging, b-jet reconstruction.**

Thanks