



A few examples of Dark matter models

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July 1, 2023 @ **2023 Cosmology Workshop on the Crossroad of
Astrophysics and Particle physics: dark matter**

Two triumphs in 20th century: **General Relativity** & **The Standard Model**

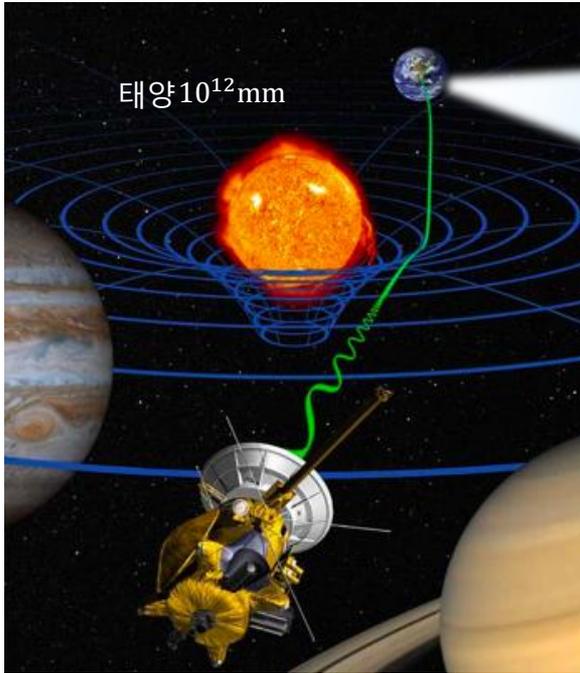


Image from NASA, Cassini spacecraft



지구 10^{10} mm

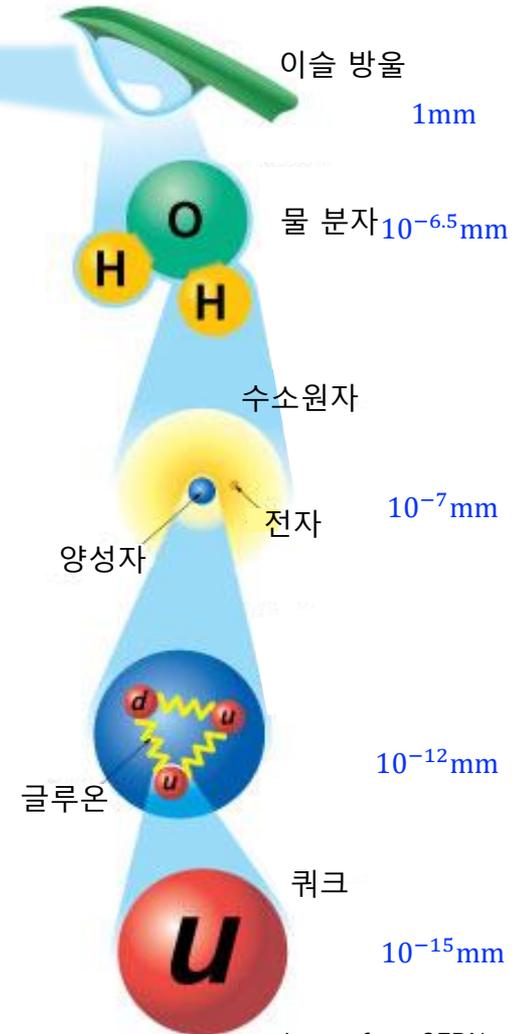
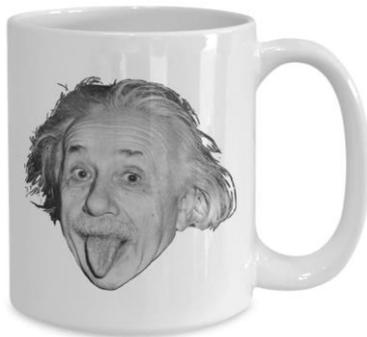
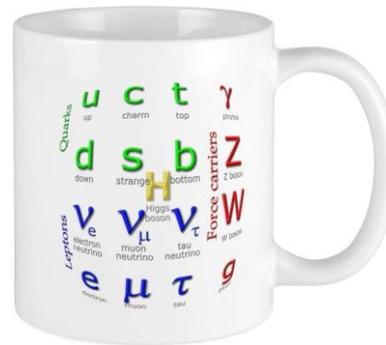


Image from CERN



gravity = curved spacetime



elementary particles = quark, lepton, gauge bosons, Higgs

Evolution of the Universe from GR + the SM

Successful in Hubble-Lemaître law, Big Bang Nucleosynthesis, Stellar Evolution, and so on.

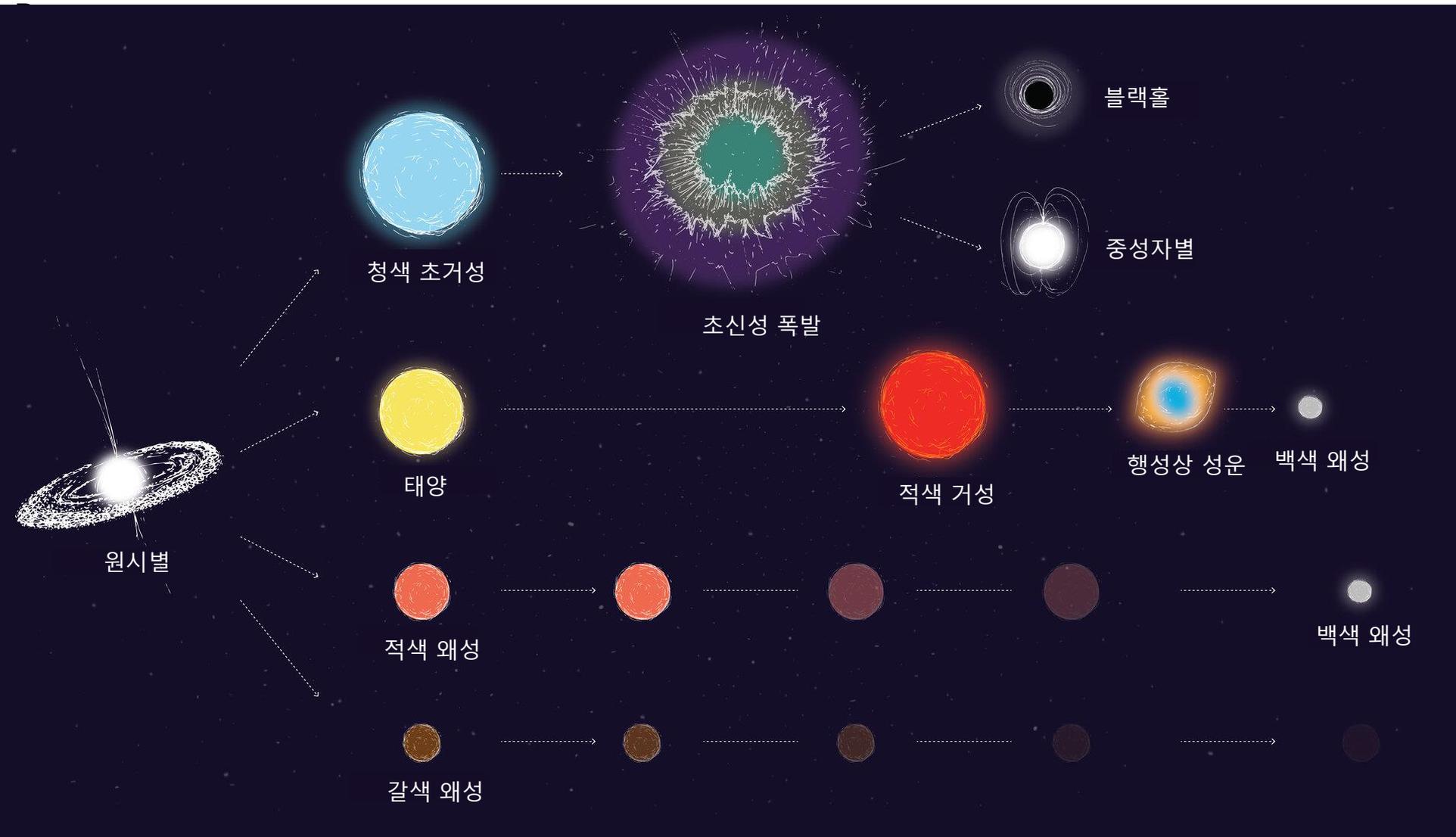
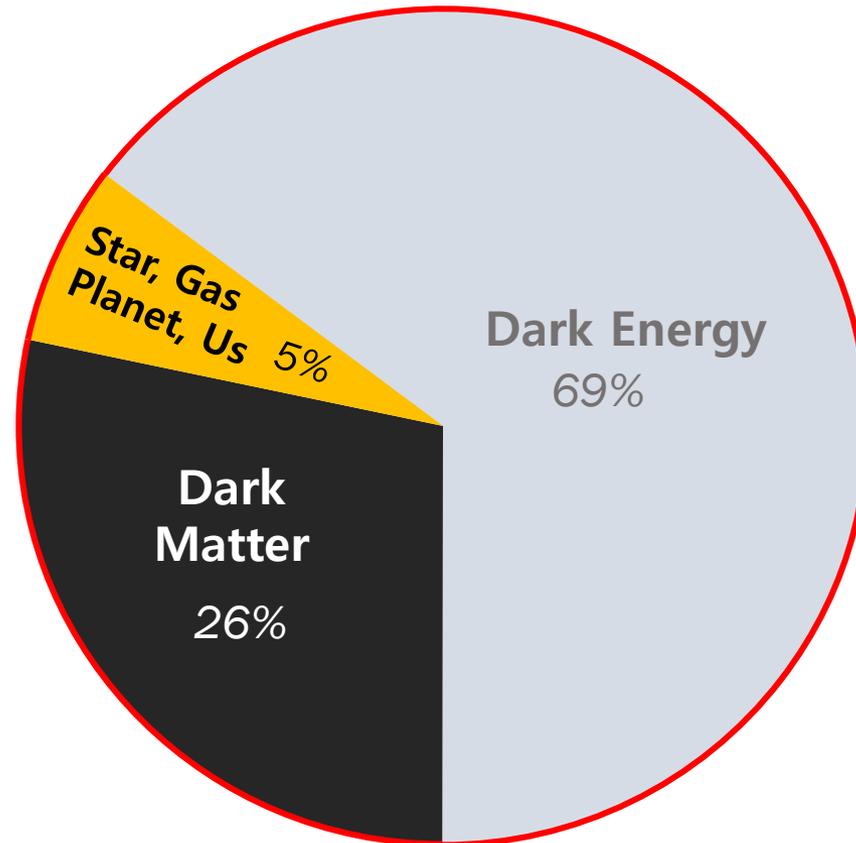


Image from ESA

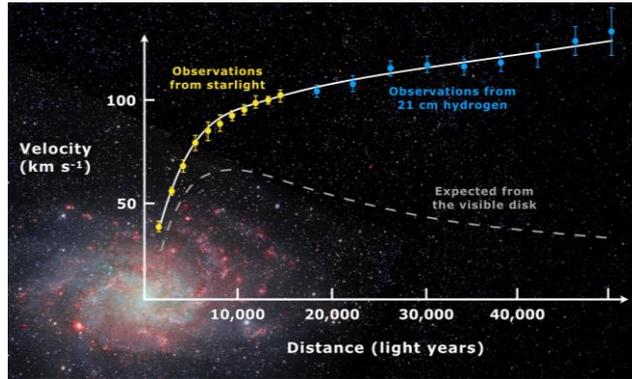
Content of the Universe



It is very difficult to properly understand the origin of the each content from **GR** and the list of particles of **the SM**

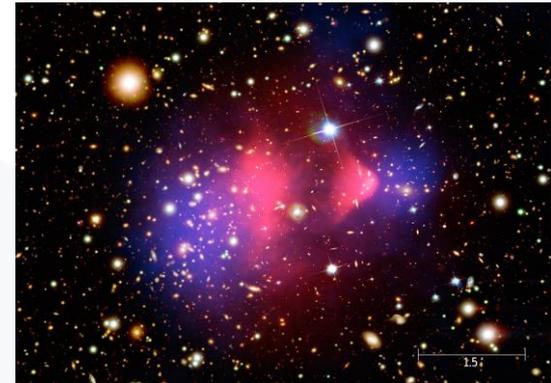
Content of the Universe - DM

Image of Galaxy Messier 33



Galaxy Scale

Image of Bullet Cluster 1E 0657-558



Galaxy Cluster Scale

Dark
Matter
26%

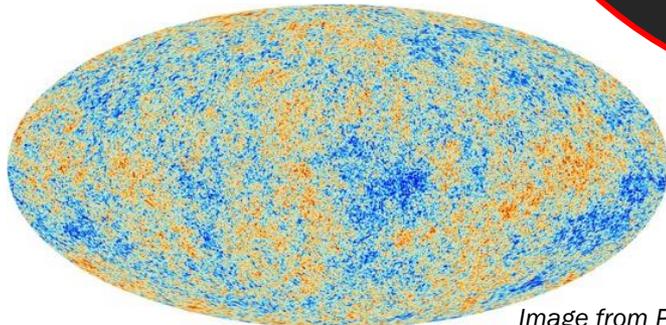


Image from PLACK

Cosmic Microwave Background

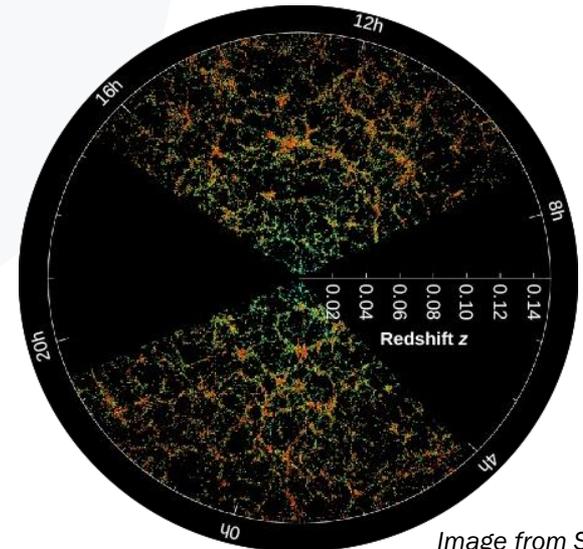
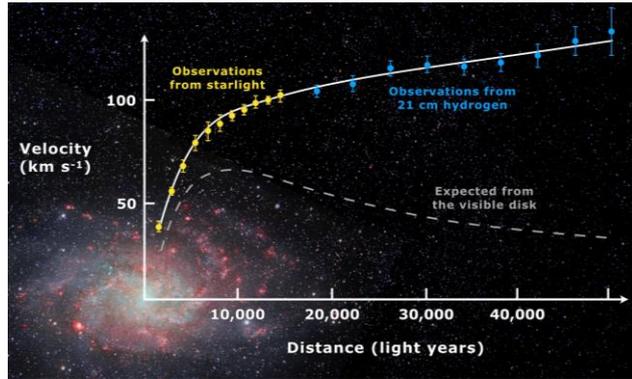


Image from SDSS

Large Scale Structure of the Universe

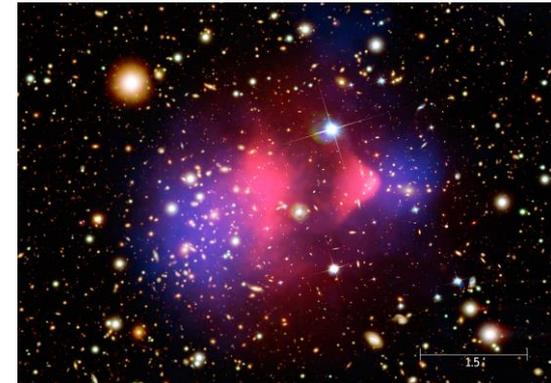
Content of the Universe - DM

Image of Galaxy Messier 33



Galaxy Scale

Image of Bullet Cluster 1E 0657-558



Galaxy Cluster Scale

<Dark Matter>
Feels Gravity, Cosmologically Stable,
No Light Emission, No EM Charge
CANNOT be explained by the particle contents of the SM

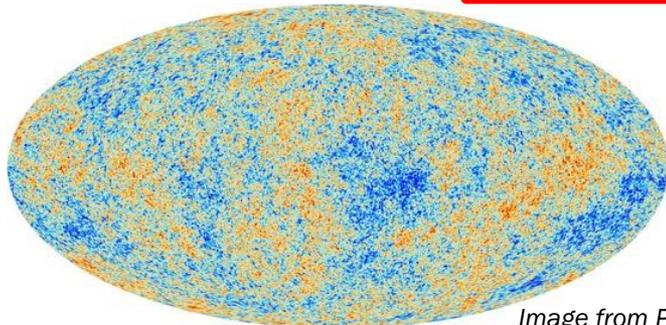


Image from PLACK

Cosmic Microwave Background

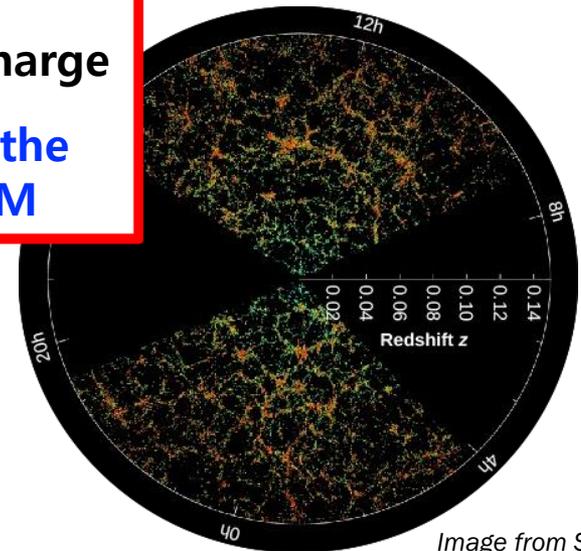
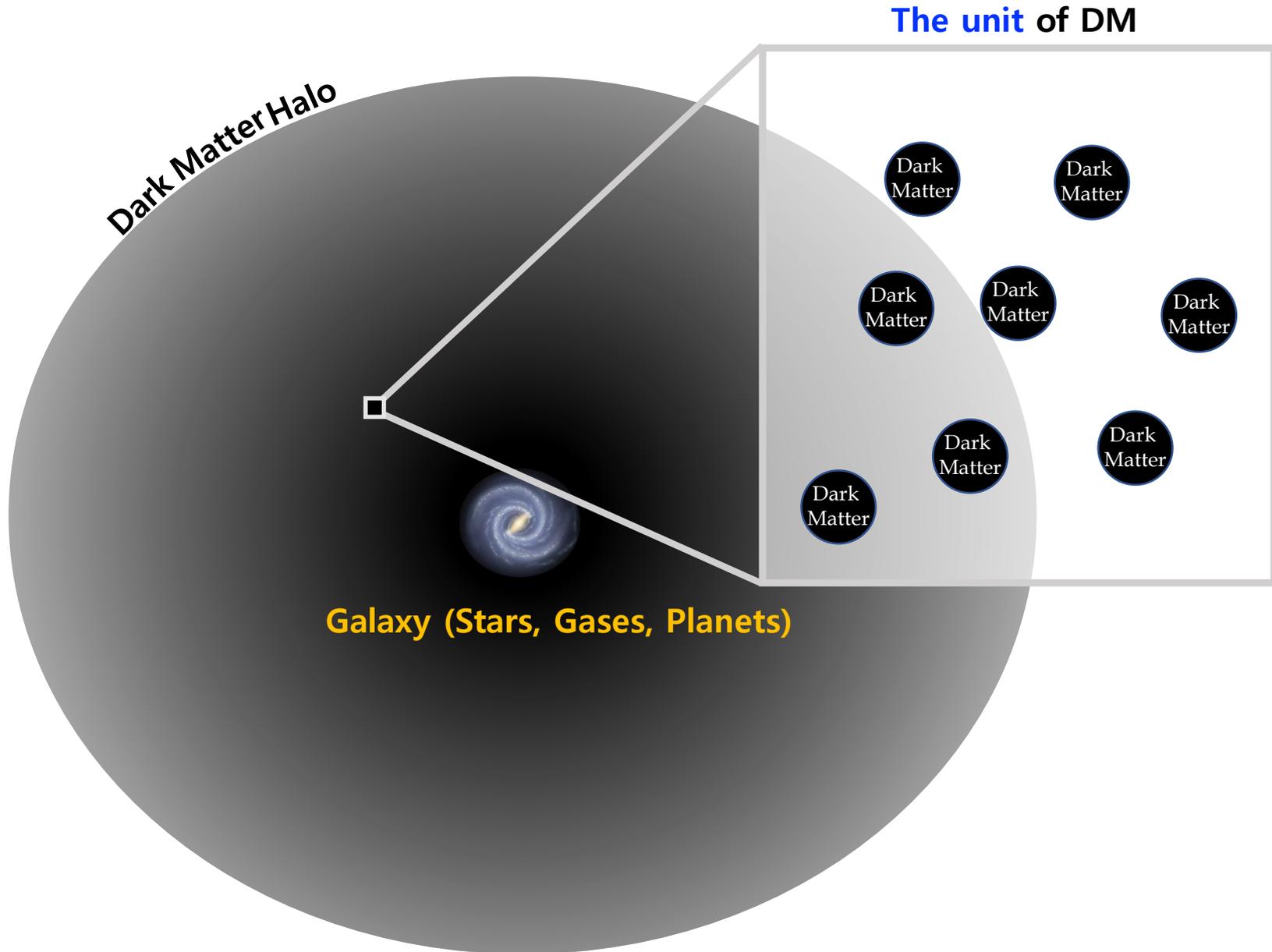


Image from SDSS

Large Scale Structure of the Universe

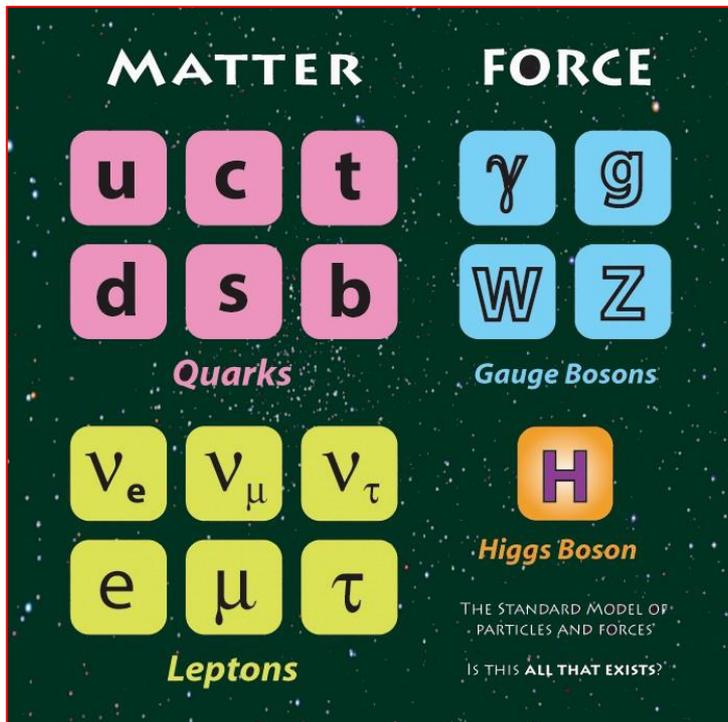
What is **the nature** of dark matter?



Particle physics approach for DM

Dark matter is a stable object from dark sector interactions and interactions with SM particles.

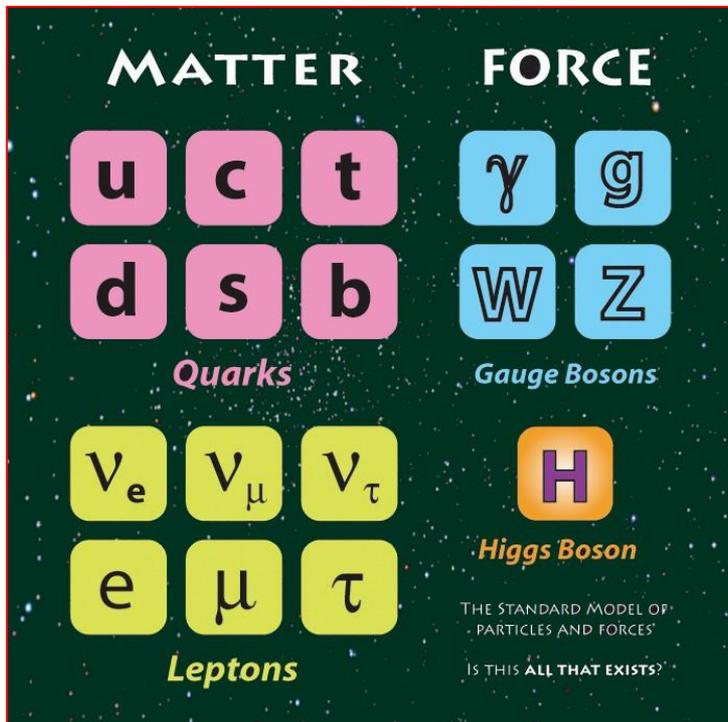
The Standard Model



Particle physics approach for DM

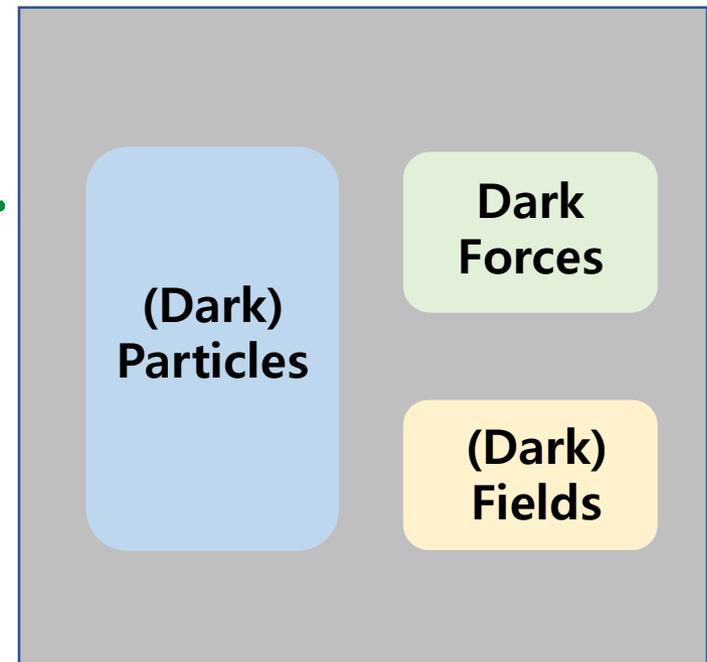
Dark matter is a stable object from dark sector interactions and interactions with SM particles.

The Standard Model



(new) interactions

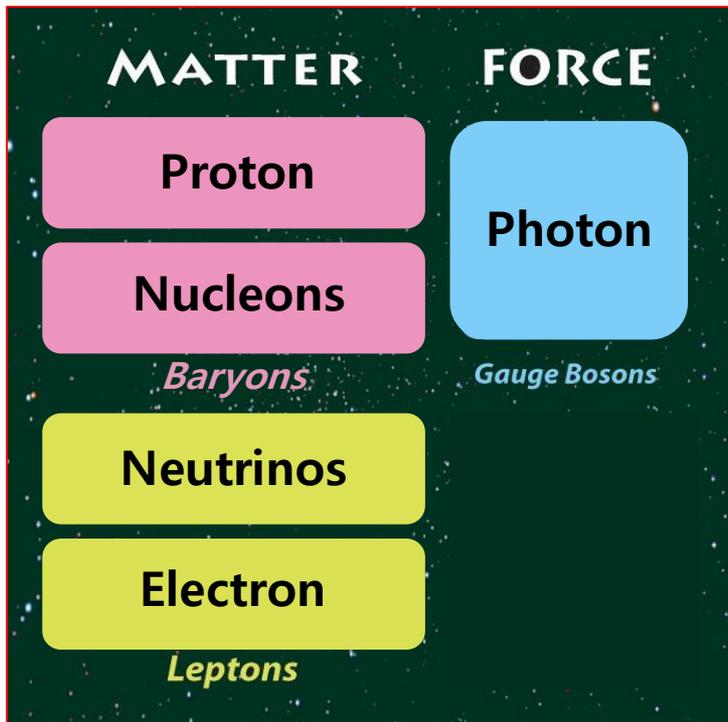
Dark (Hidden) Sector



Particle physics approach for DM

Dark matter is a stable object from dark sector interactions and interactions with SM particles.

The Standard Model **at Low Energy**




(new)
interactions

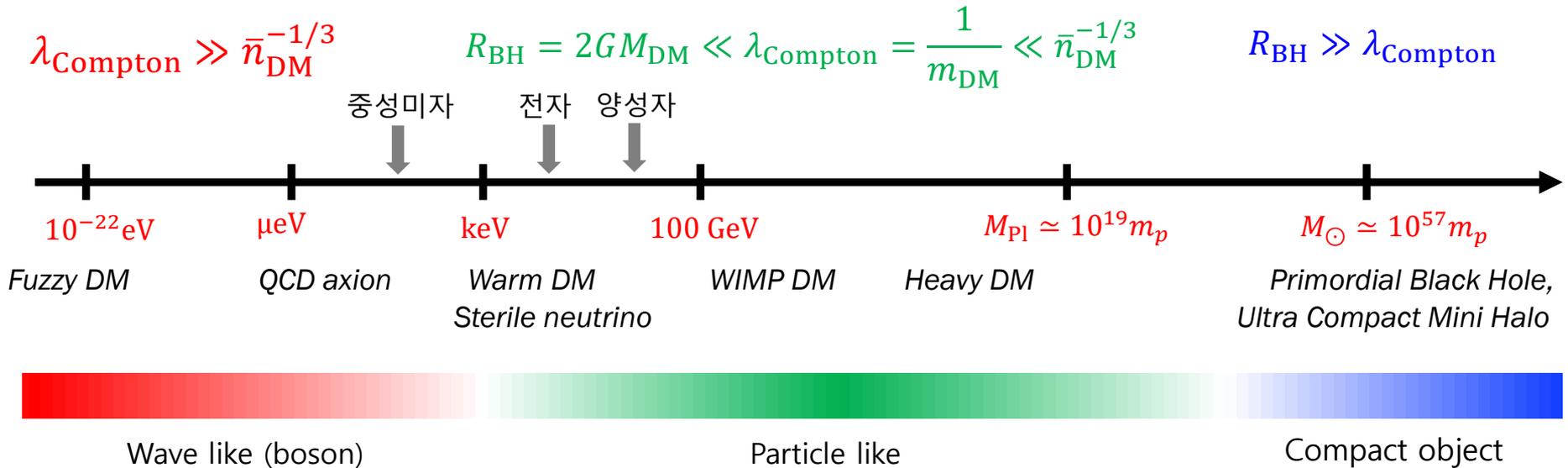
Dark Sector **at Low Energy**



Candidates of DM for its mass

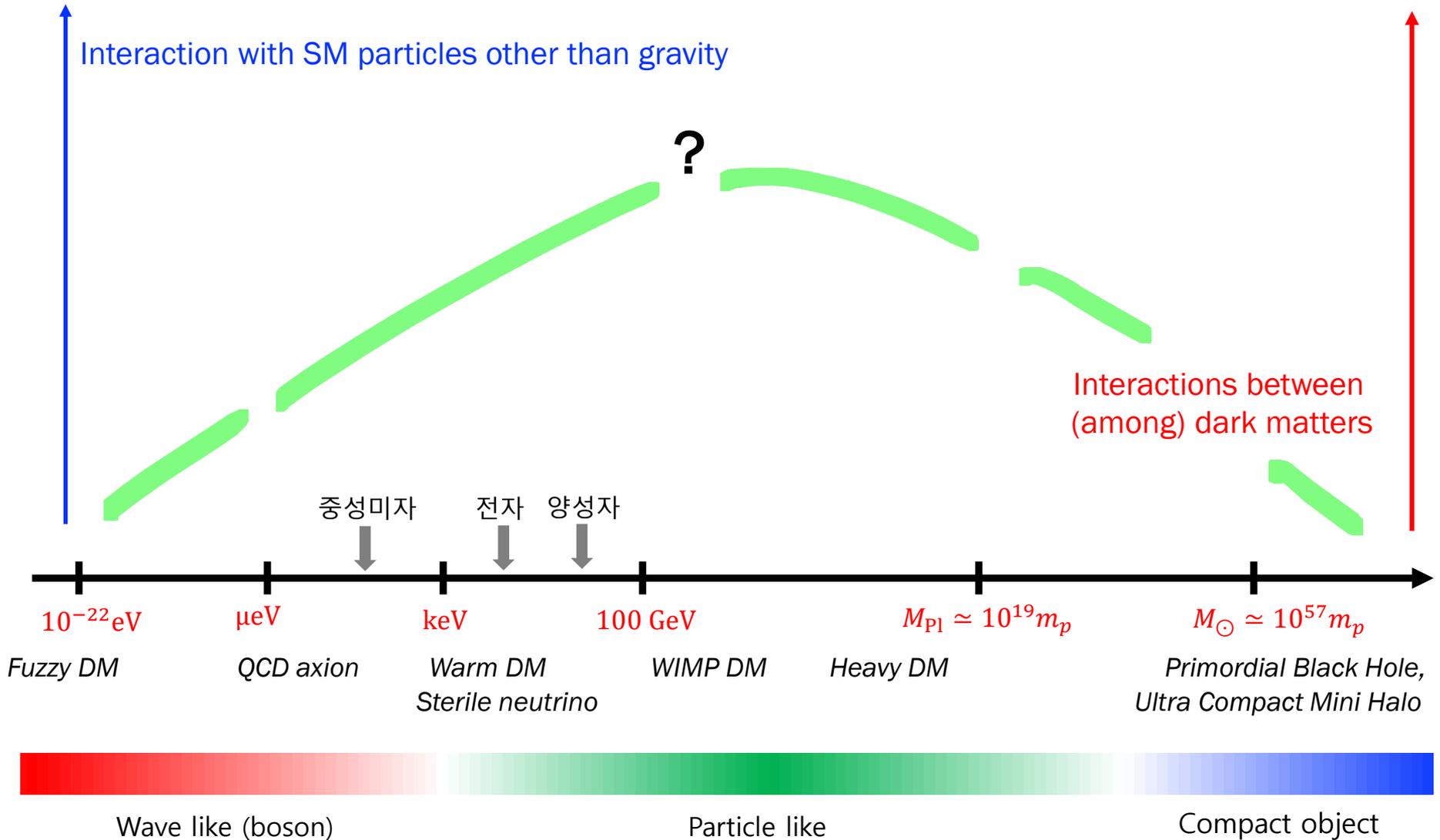
$$\bar{\rho}_{\text{DM}} = M_{\text{DM}} \bar{n}_{\text{DM}} = (0.25 - 0.27) \bar{\rho}_{\text{tot}} \simeq 1.2 \times 10^{-6} \text{GeV/cm}^3$$

$$G = \frac{1}{M_{\text{Pl}}^2} \left(M_{\text{Pl}} = \sqrt{\frac{\hbar c}{G}} \simeq 1.22 \times 10^{19} \text{GeV} \right)$$



Candidates of DM for its mass and interactions

$$\bar{\rho}_{\text{DM}} = M_{\text{DM}} \bar{n}_{\text{DM}} = (0.25 - 0.27) \bar{\rho}_{\text{tot}} \simeq 1.2 \times 10^{-6} \text{GeV/cm}^3$$



Candidates of DM for its mass and interactions

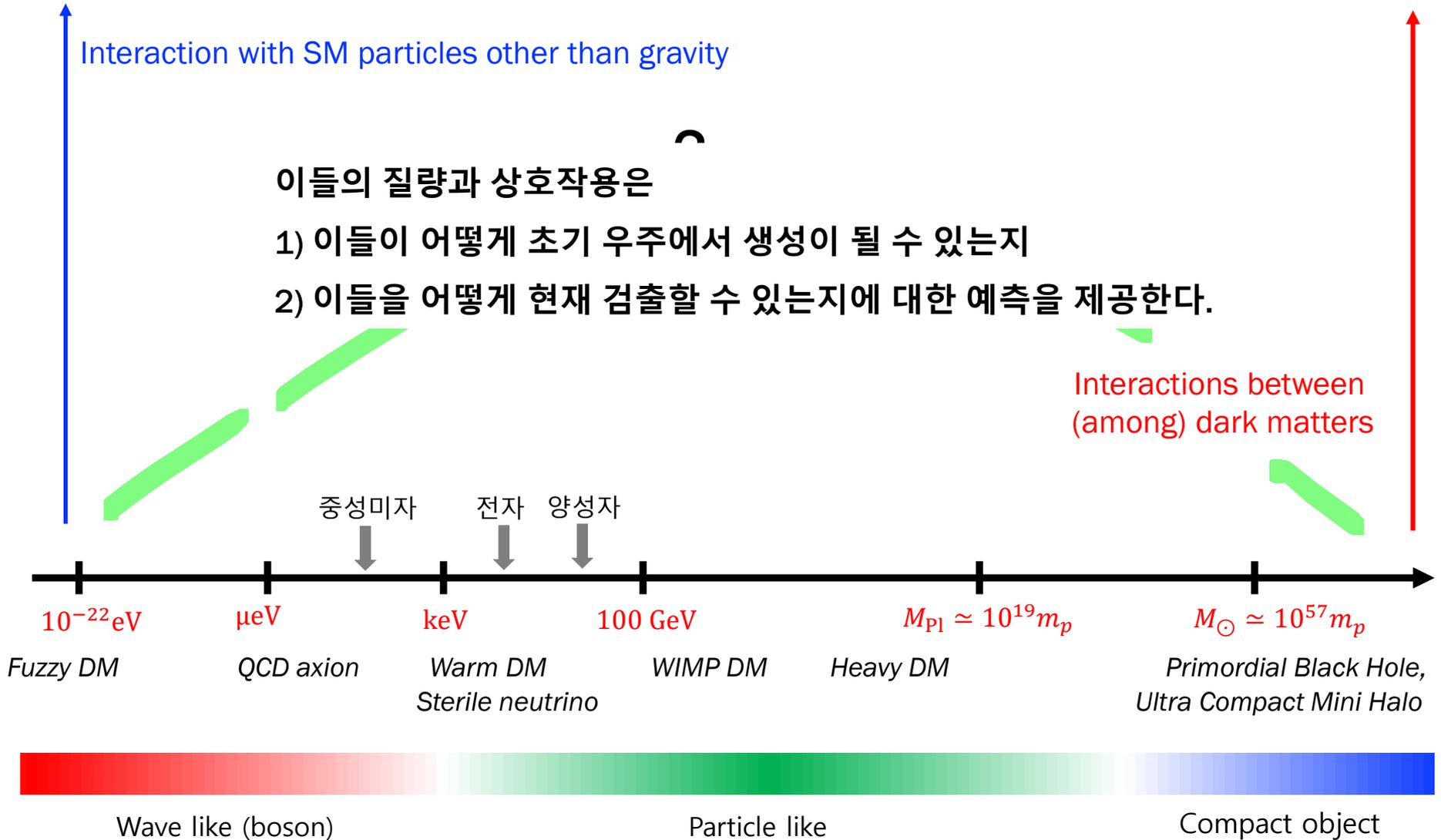
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Interaction with SM particles other than gravity

이들의 질량과 상호작용은

- 1) 이들이 어떻게 초기 우주에서 생성이 될 수 있는지
- 2) 이들을 어떻게 현재 검출할 수 있는지에 대한 예측을 제공한다.

Interactions between (among) dark matters

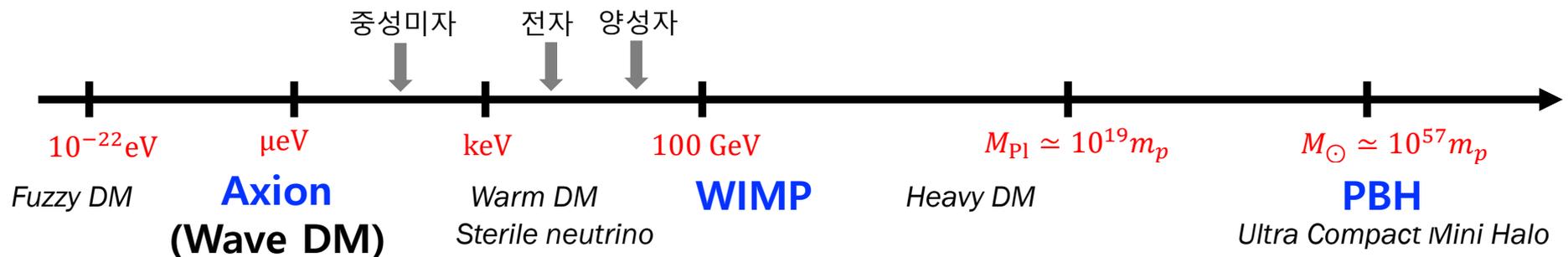


Well known candidates for each mass range

Weakly Interacting Massive Particle (WIMP) : (0.1 ~ 1000) GeV

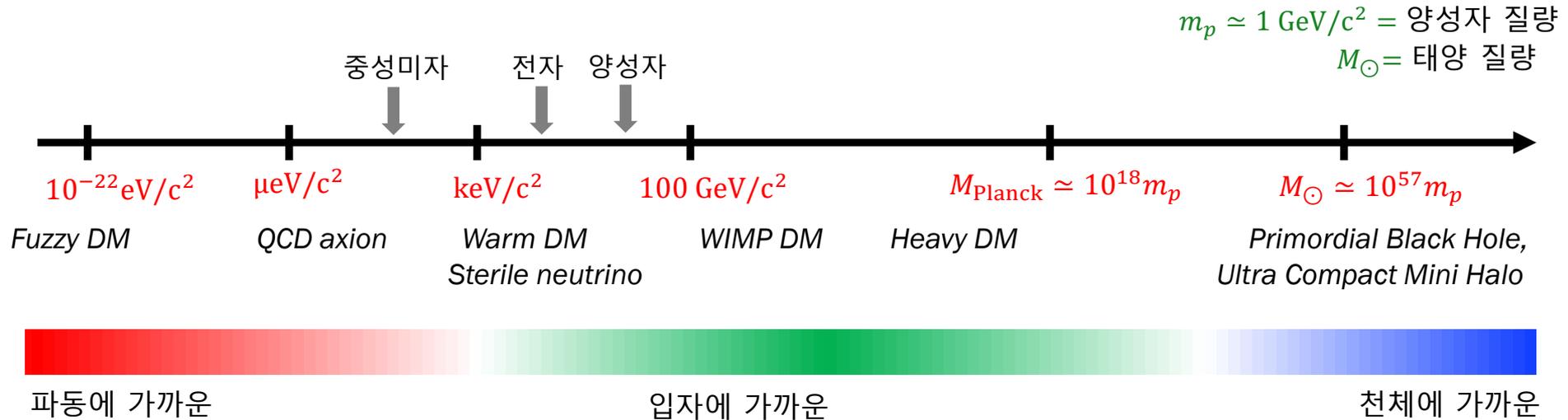
QCD Axion (Axion) : (0.0001 ~ 10) μeV

Primordial Black Hole (PBH) : (10^{-17} ~ 100) M_{\odot} = (10^{-40} ~ 10^{59}) GeV



Probing the Nature of Dark Matter

Candidates of DM for its mass

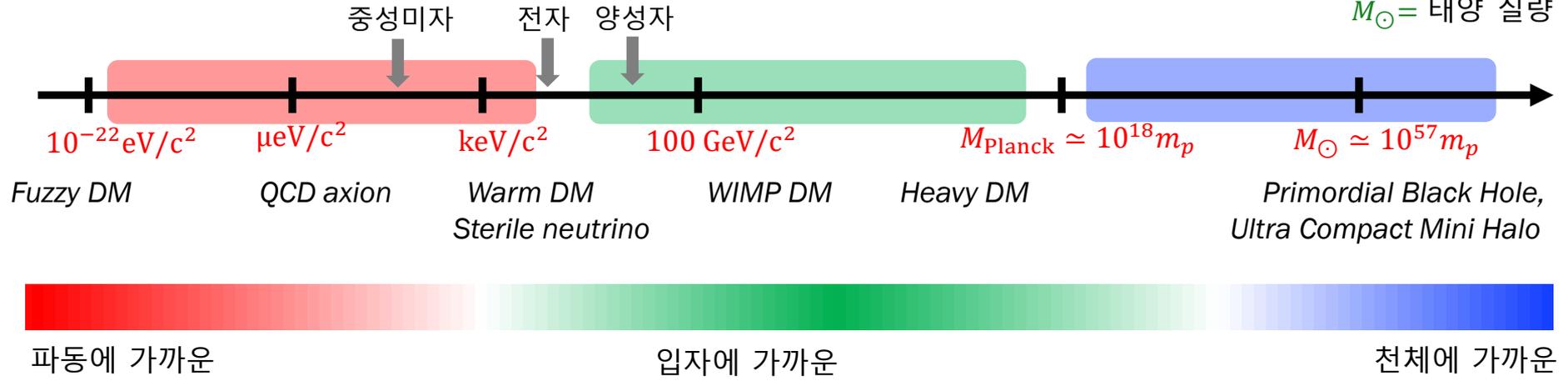


Approach for DM studies in particle physics

- (A) Taking a specific DM mass range
- (B) Taking a specific symmetry
- (C) Any new possibilities that can be probed by observations, etc.

Candidates of DM with respect to its mass

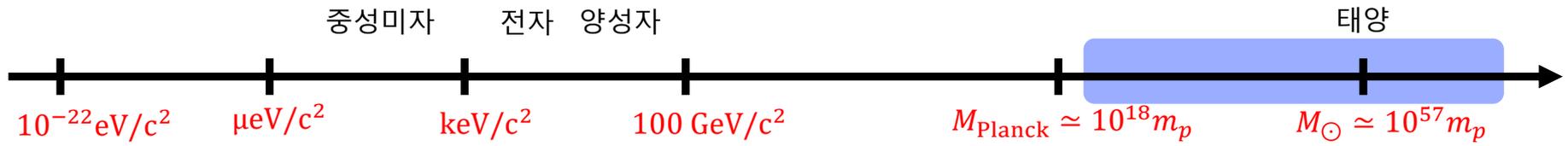
$m_p \approx 1 \text{ GeV}/c^2 = \text{양성자 질량}$
 $M_{\odot} = \text{태양 질량}$



My Approach

DM physics related with scalar field dynamics for various mass range

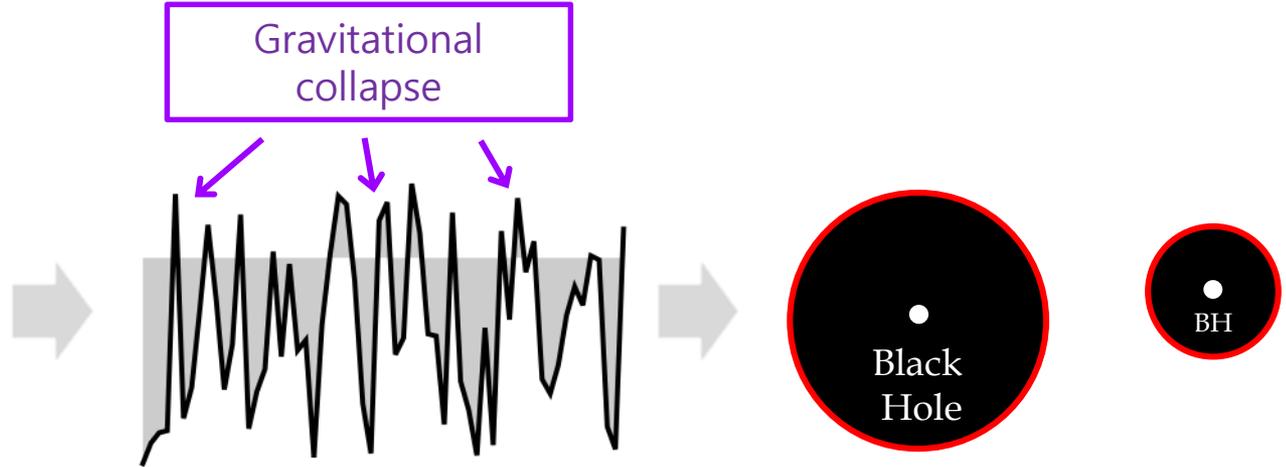
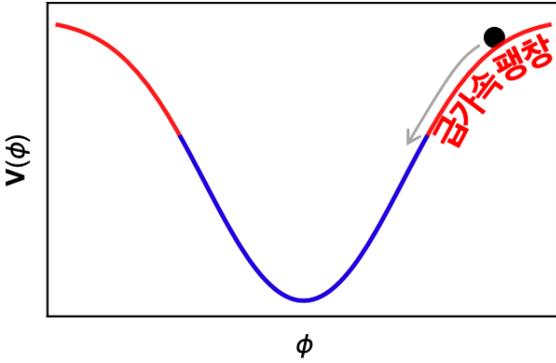
(1) Compact Dark Matter



(1) Compact Dark Matter

In the early Universe,
inflating period

Inflaton scalar field dynamics



Density fluctuation

Primordial Black Holes

Stable Scalar dynamics
In the early Universe
Early matter domination



K.-Y. Choi, J.-O. Gong, *CSS*
Phys. Rev. Lett. 115, 211302 (2015)

Searching for Compact Dark Matter

See compact dark matter through LIGO GW observatory

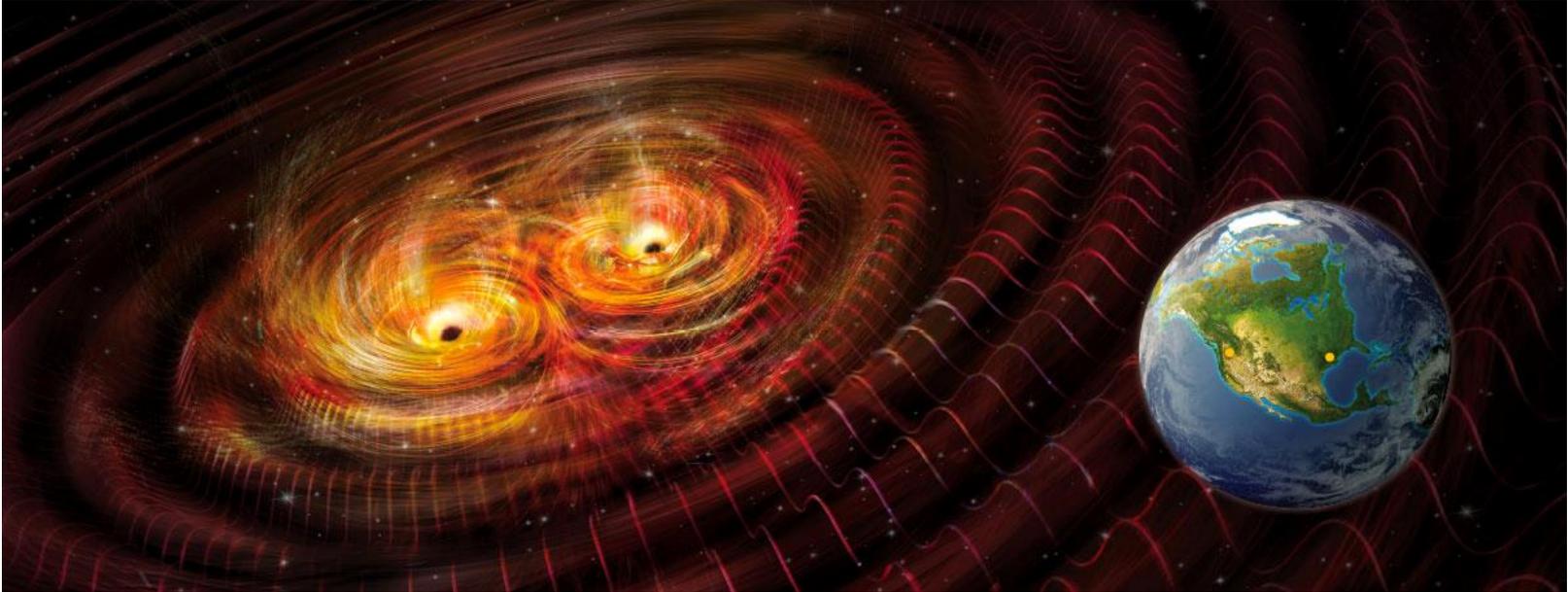


Image from sciencenews.org

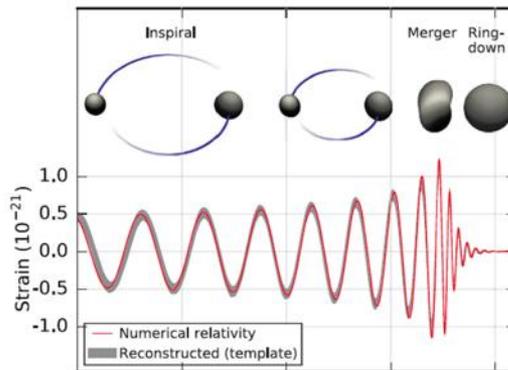
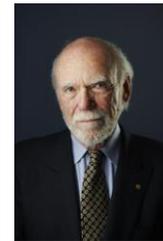


Image from LIGO

The Nobel Prize in Physics 2017



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Rainer Weiss
Prize share: 1/2

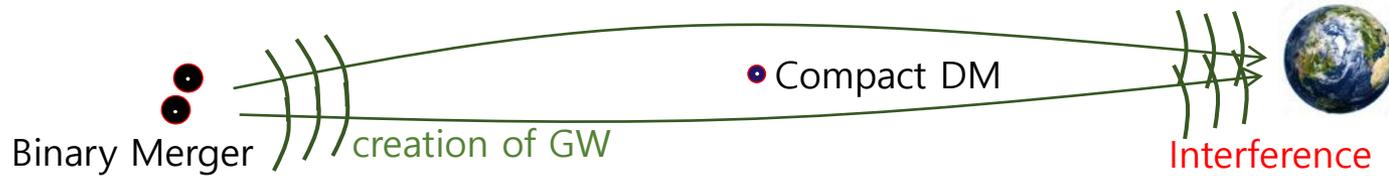


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Gravitational Wave: Telescope for DM

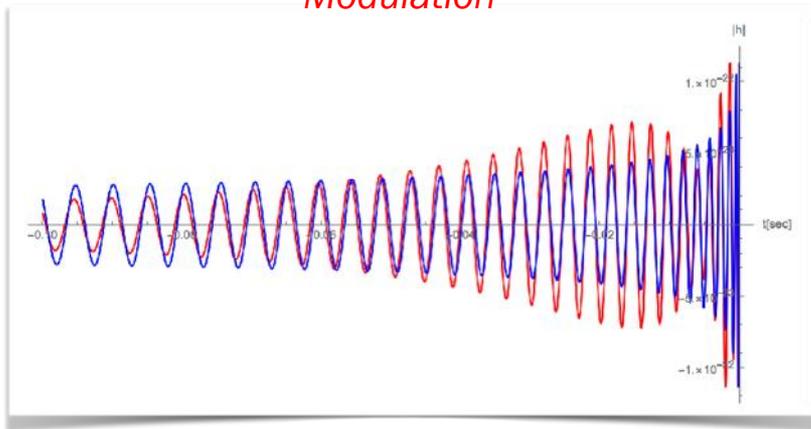


Femto-Lensing effect by compact DM →

Deformation of waveform at LIGO

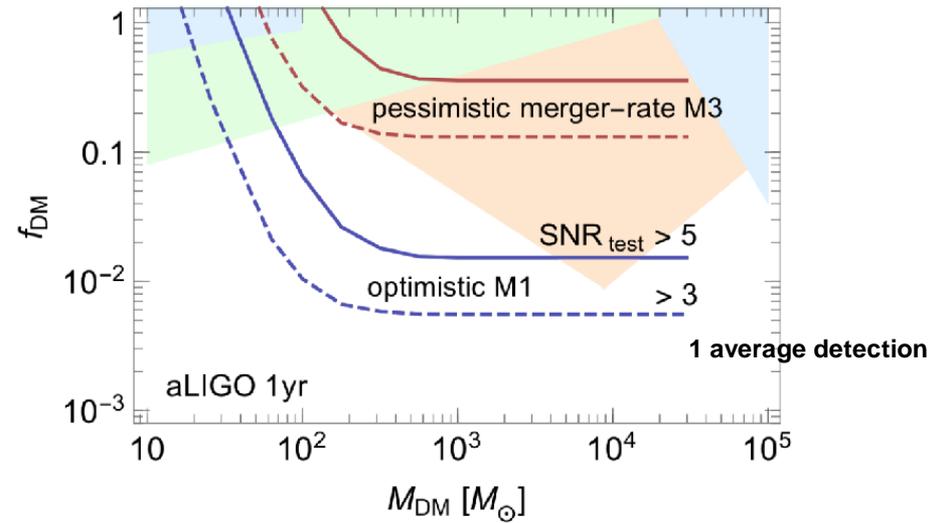
→ **Evidence of Compact DM**

Modulation



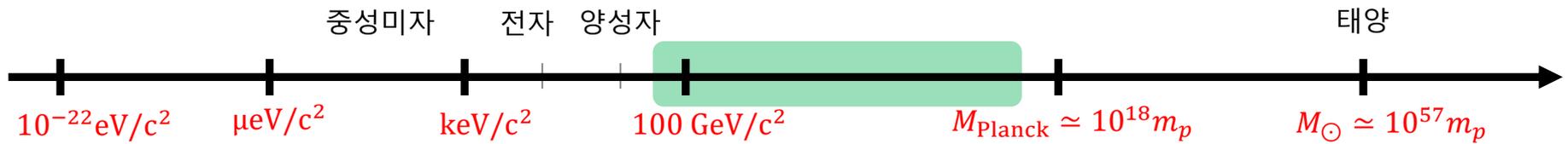
chirp signal with fringes

S. Jung, CSS Phys. Rev. Lett. 122, 041103 (2019)



(2) Particle Dark Matter: Source of GW

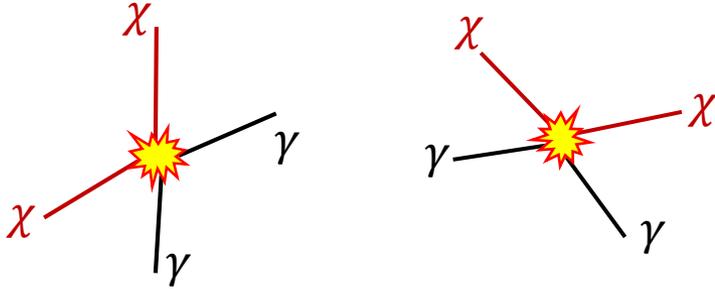
(A deeper connection between Gravitational Wave and Dark Matter)



Particle-like Dark Matter

Thermal Dark Matter

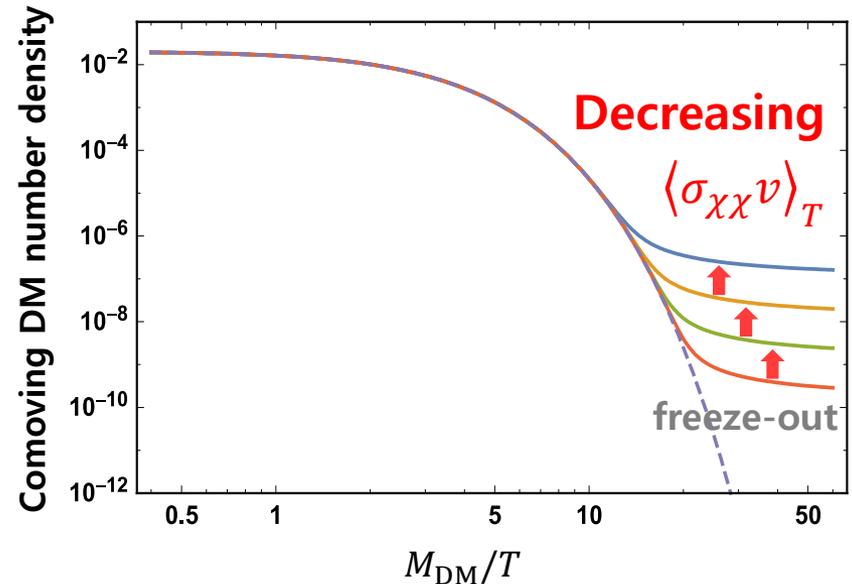
Dark matter density is determined by its annihilation cross-section



$$\Omega_{\text{DM}} h^2 = 0.1 \left(\frac{3 \times 10^{-26} \text{ cm}^3/\text{s}}{\langle \sigma_{\chi\chi} v \rangle_T} \right)$$

WIMP ($M_{\text{DM}} \sim 100 \text{ GeV}$, $\alpha_{\chi} \sim 0.01$)
is one of the best candidates for DM

HOWEVER,
No hints for WIMP DM so far:
Strong motivation of
the beyond WIMP paradigm



Dark matter cross-section is limited by its mass and the velocity

The Unitarity bound: $\langle \sigma_{\chi\chi} v \rangle_T \leq \frac{4\pi}{M_{\text{DM}}^2 \langle v \rangle_T}$

Thermal DM **Beyond** the Unitarity Bound

How can the Unitarity bound be overcome to allow various DM masses?

$$\Omega_{\text{DM}} h^2 \geq 0.1 \left(\frac{M_{\text{DM}}}{130 \text{ TeV}} \right)^2$$

- **WIMPZilla, Superheavy DM, gravitational production etc.**
- One can think the origin or dark matter mass tightly related with production mechanism : **These days, various approaches along this direction are actively studied**

Origin of Mass for particle DM: Expectation value of scalar field



Higgs field (giving mass to the elementary particles)

Nonzero expectation value of the scalar field imposes DM mass



Scalar Field (giving DM Mass)

Temperature drops: 수증기 → 이슬



Universe expands → Temperature decreases → **Bubbles of scalar condensation form!**



Origin of Mass for particle DM: Expectation value of scalar field



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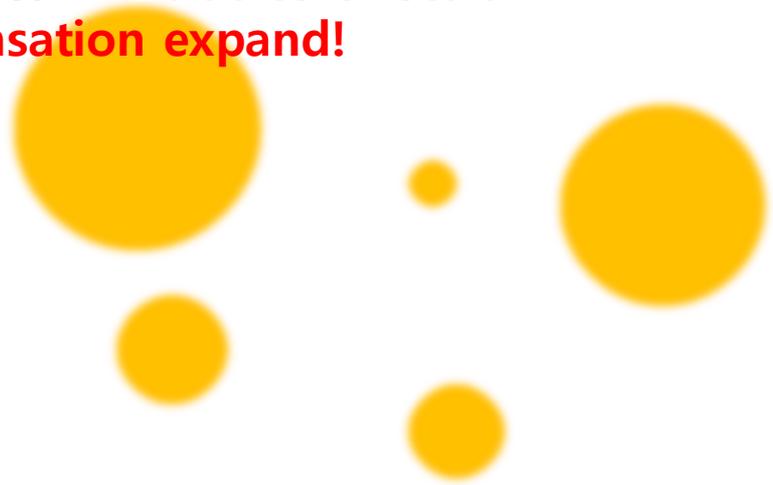


Scalar Field (giving DM Mass)

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Scalar Field (giving DM Mass)

Temperature drops: 수증기 → 이슬



Universe expands → Temperature decreases → **Bubbles of scalar condensation collide!**

Origin of Mass for particle DM: Expectation value of scalar field



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Nonzero expectation value of the scalar field imposes DM mass



Scalar Field (giving DM Mass)

Temperature drops: 수증기 → 이슬

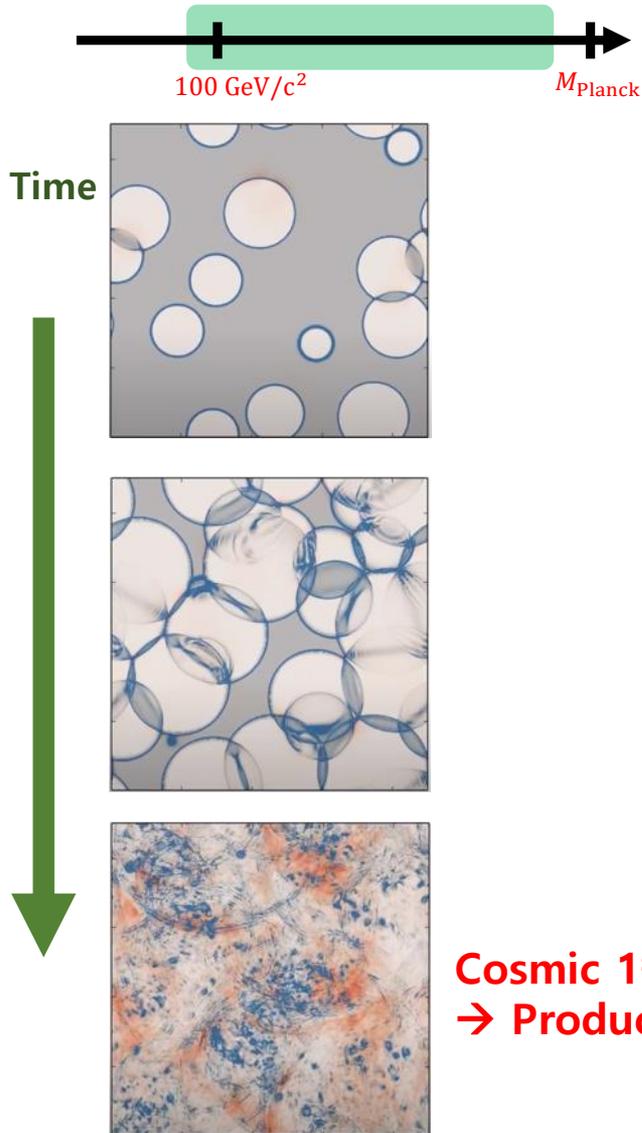


Universe expands → Temperature decreases → **Bubbles of scalar condensation fill the Universe**
→ **Cosmic 1st order phase transition**

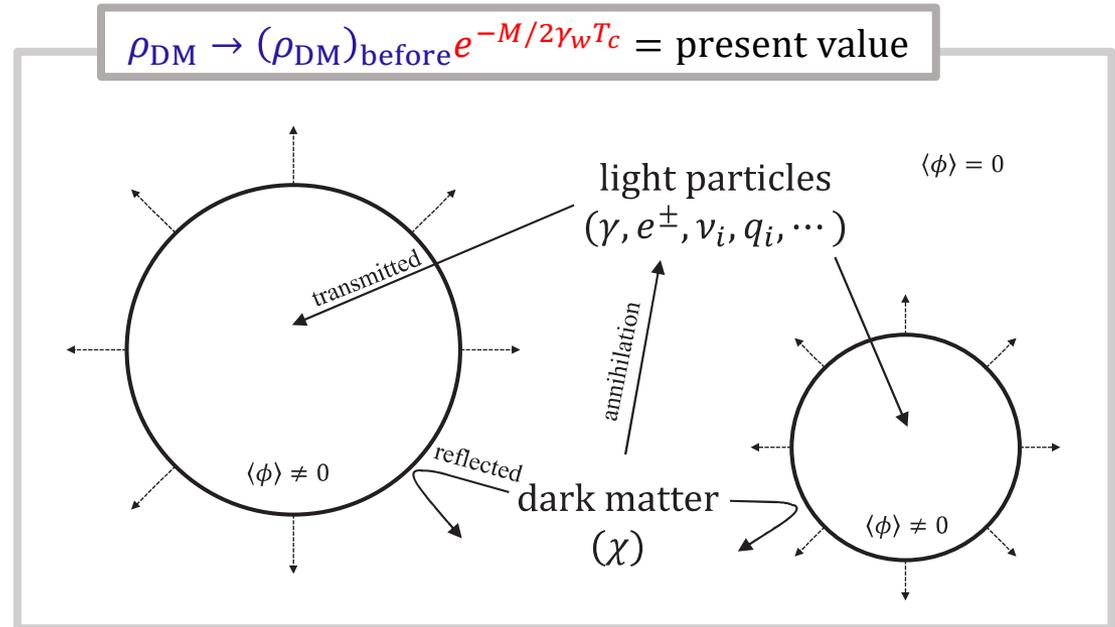
Origin of DM mass & its abundance

Proposing the mechanism working in a wide range of DM mass

D. Chway, T. H. Jung, *CSS*
Phys. Rev. D 101, 095019 (2020)



Filtering-out Mechanism

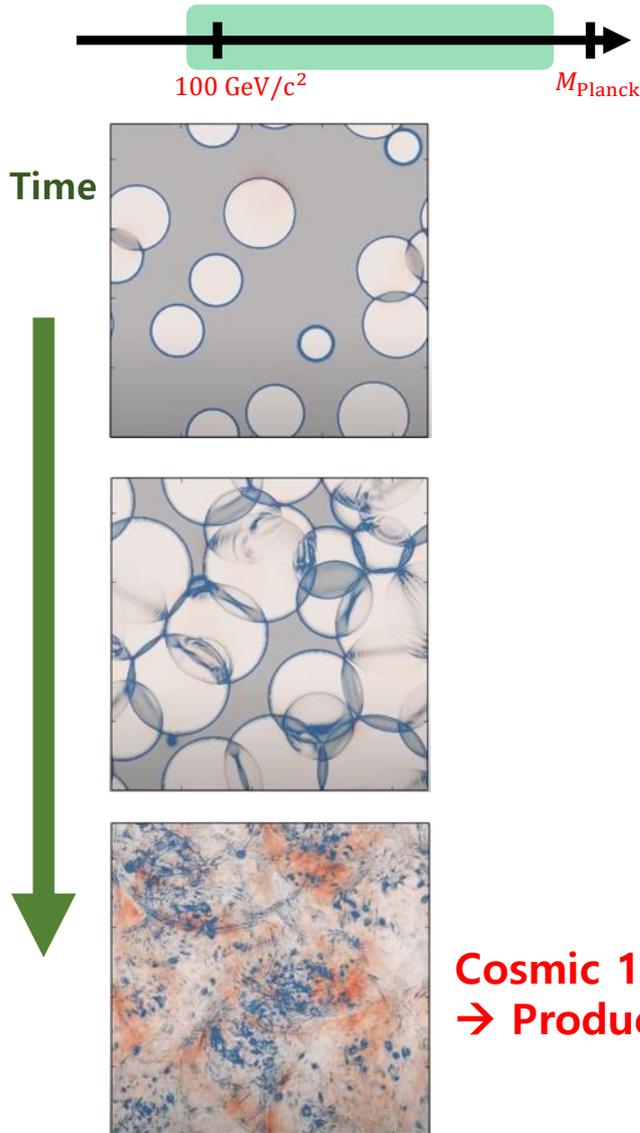


**Cosmic 1st order phase transition
 → Production of Gravitational Waves**

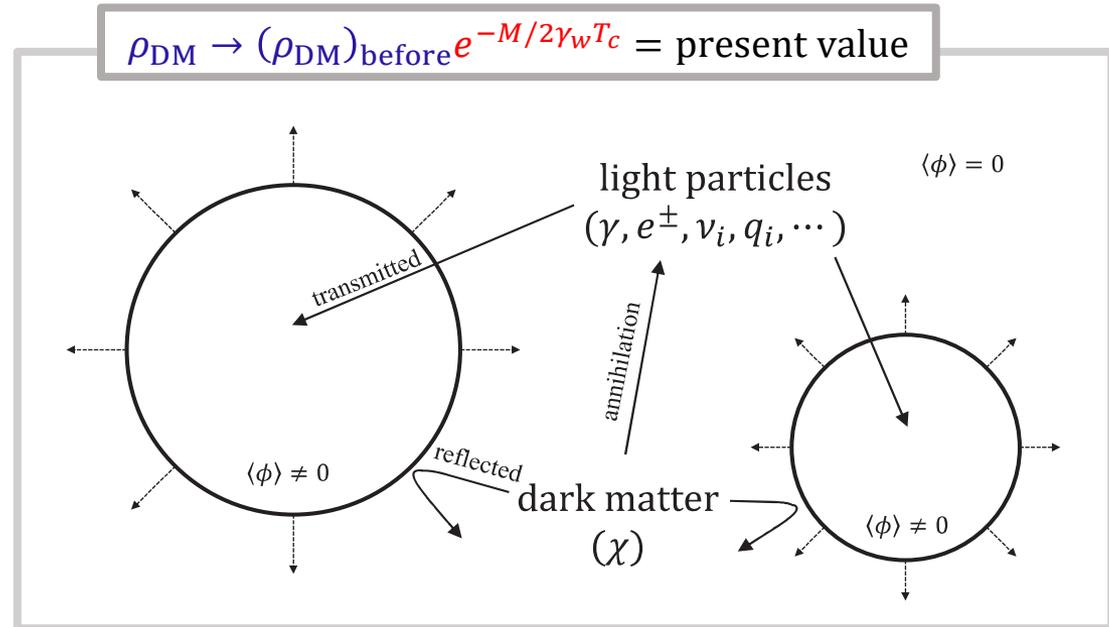
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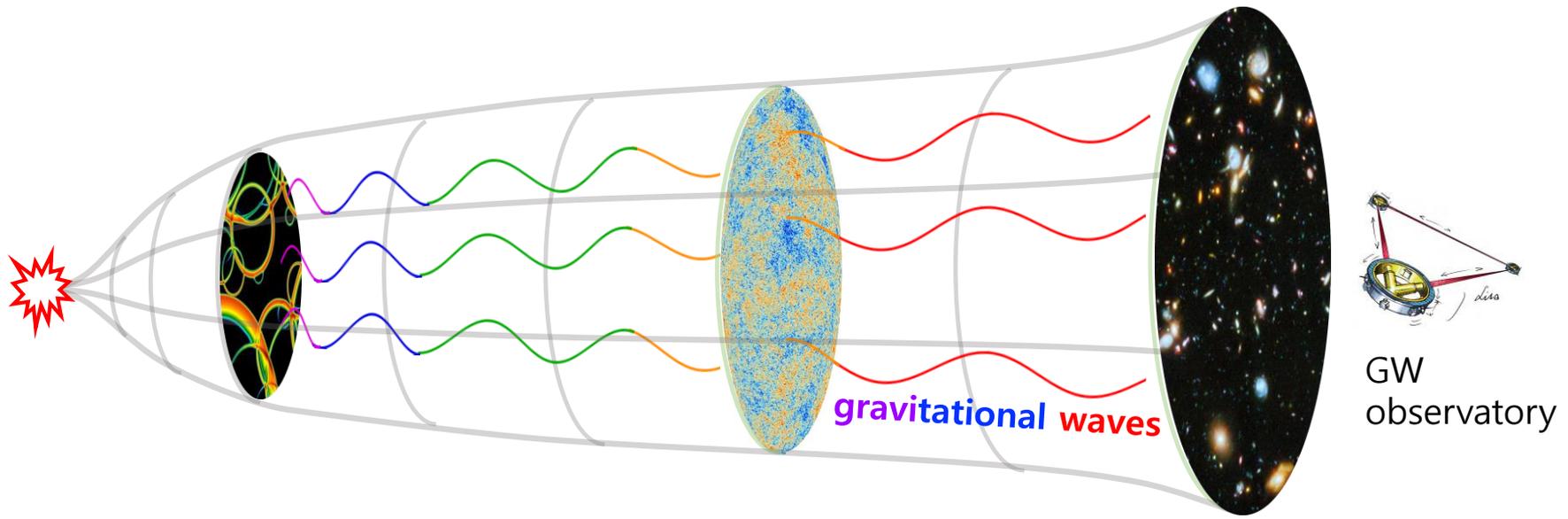
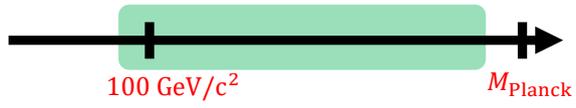


**Cosmic 1st order phase transition
 → Production of Gravitational Waves**

**2) Understanding the origin of DM
 by GW observations**

Stochastic Gravitational Waves

Proposing the mechanism working in a wide range of DM mass



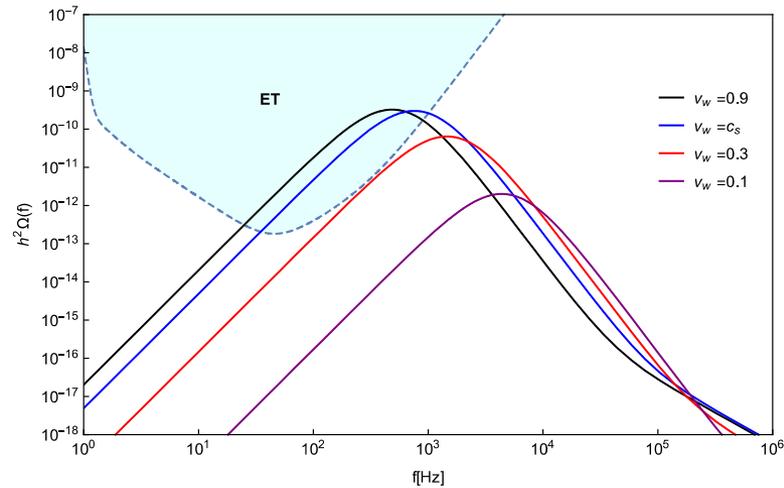
2) Understanding the origin of DM by GW observations

Origin of DM mass & GW observations

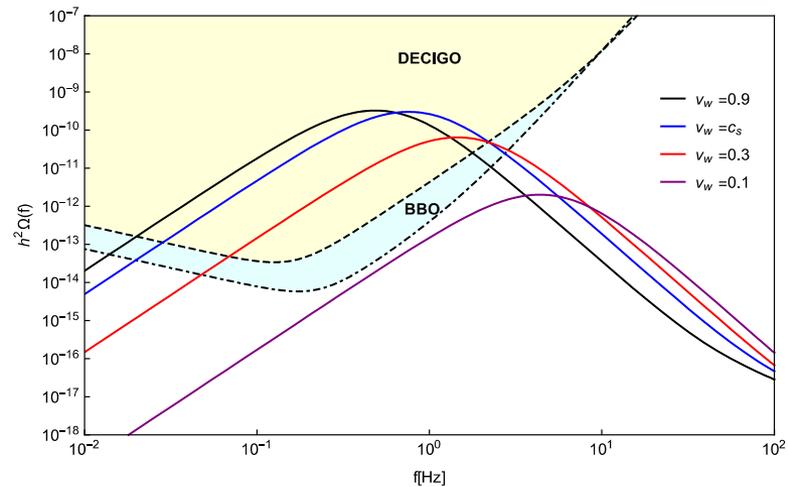
Proposing the mechanism working in a wide range of DM mass



Mass=100PeV



Mass=100TeV

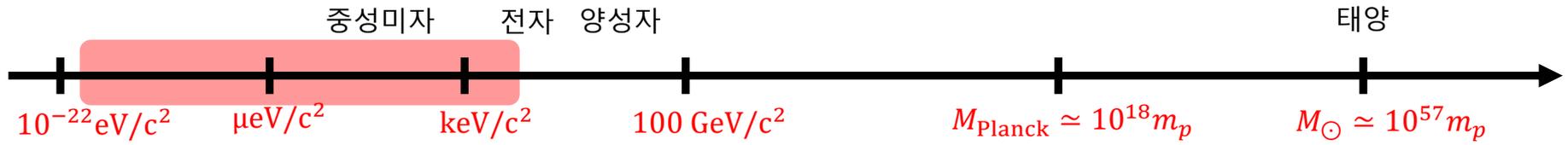


중력파 관측소

M. Ahmadvand 2108.00958

2) Understanding the origin of DM by GW observations

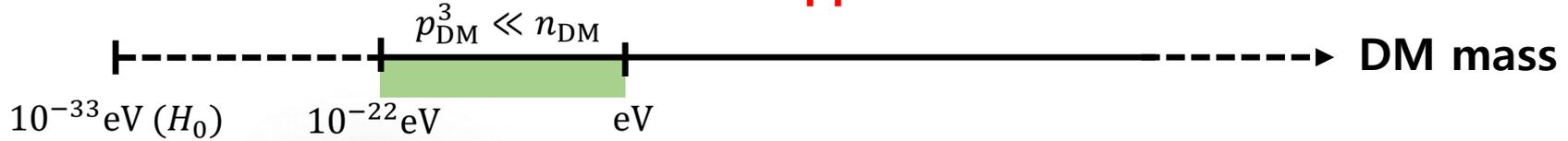
(3) Wave Dark Matter



Wave Dark Matter

Ultra-light scalar dark matter: High occupation number \rightarrow Wave feature

\rightarrow Suppression of small scale structure



Dark Matter

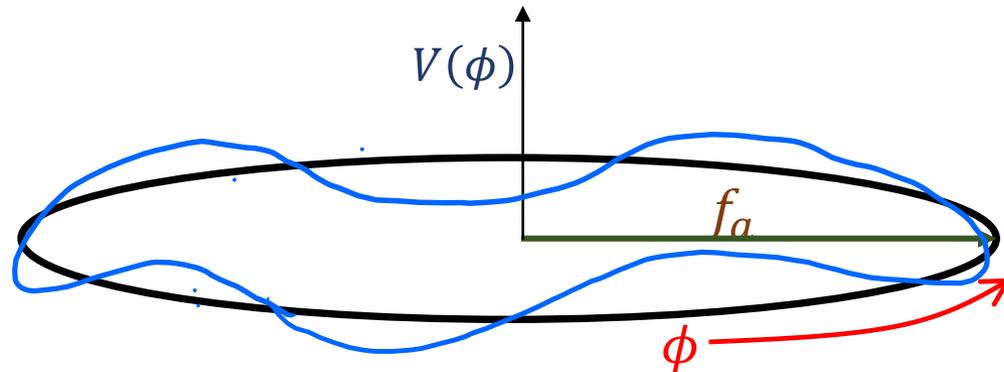
$$\lambda_{dB} = \frac{2\pi}{M_{DM} v_{vir}} \sim \text{kpc} \left(\frac{10^{-22} \text{eV}}{M_{DM}} \right)$$

Coherent Waves ($p_{DM}^3 \ll n_{DM}$)



- One of the well known example of wave dark matter is

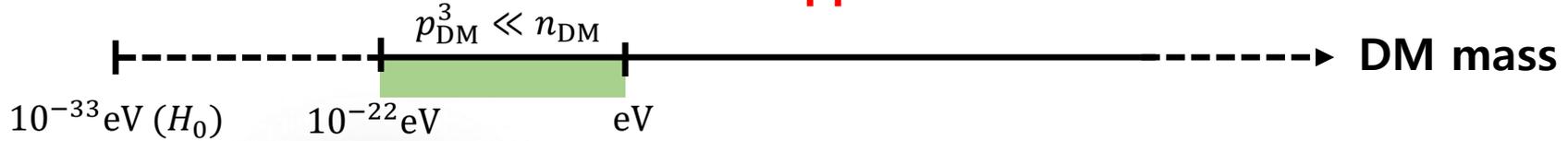
(QCD) Axion



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Dark Matter

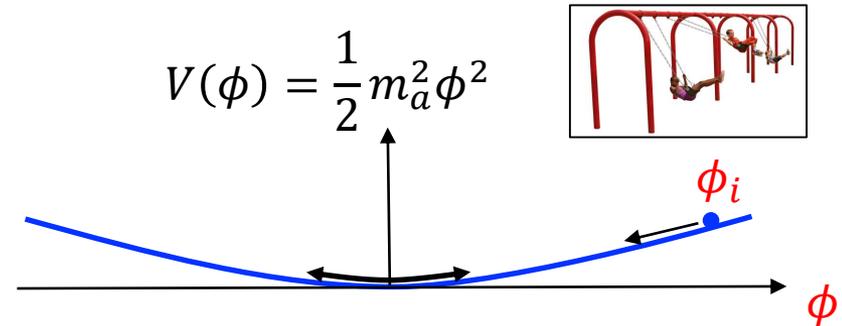
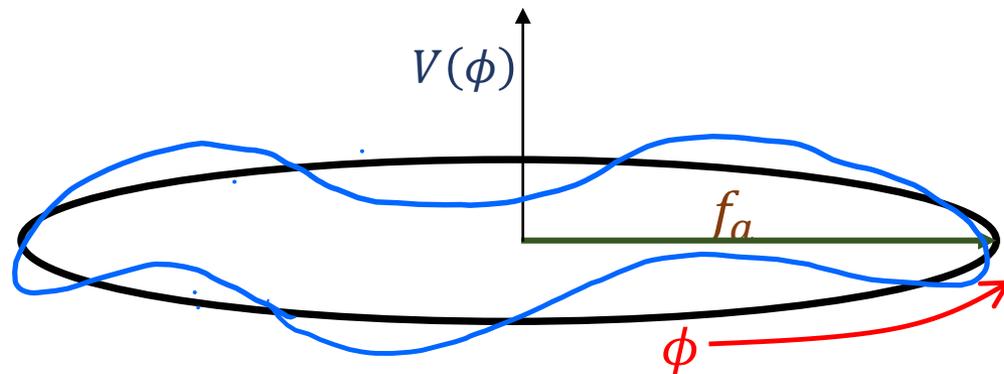
$$\lambda_{\text{dB}} = \frac{2\pi}{M_{\text{DM}} v_{\text{vir}}} \sim \text{kpc} \left(\frac{10^{-22} \text{eV}}{M_{\text{DM}}} \right)$$

Coherent Waves ($p_{\text{DM}}^3 \ll n_{\text{DM}}$)



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(QCD) Axion

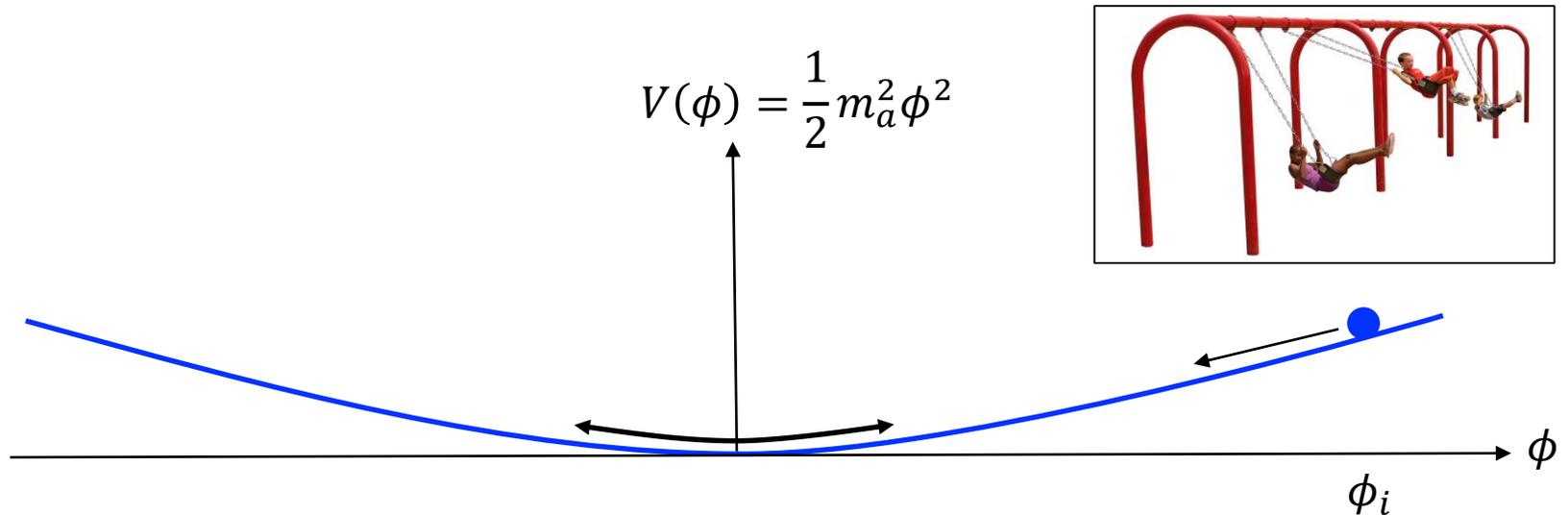


$$V(\phi) = \frac{1}{2} m_a^2 \phi^2$$

QCD Axion

초기 액시온 장이 공간적으로 매우 균일하게 분포하고, Coherent 한 Oscillation 이 이뤄지는 경우, 비록 액시온의 질량이 매우 작더라도 큰 스케일에서 **차가운 암흑물질**과 같은 형태로 움직임을 확인할 수 있다.

$$\ddot{\phi}(t) + 3H(t)\dot{\phi}(t) + m_a^2\phi(t) = 0 \quad (H(t) = \text{주어진 시간에서의 허블 파라미터})$$



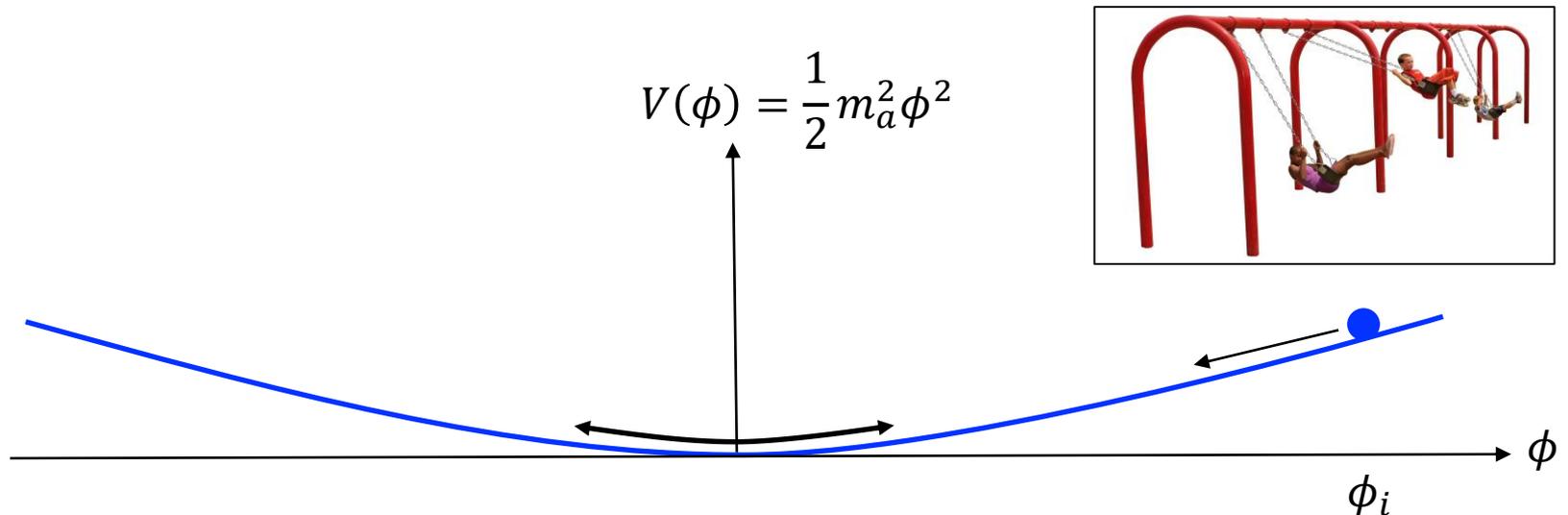
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이러한 이유로 액시온 혹은 ultralight boson field 는 well motivated 된 암흑물질후보로 다뤄진다.

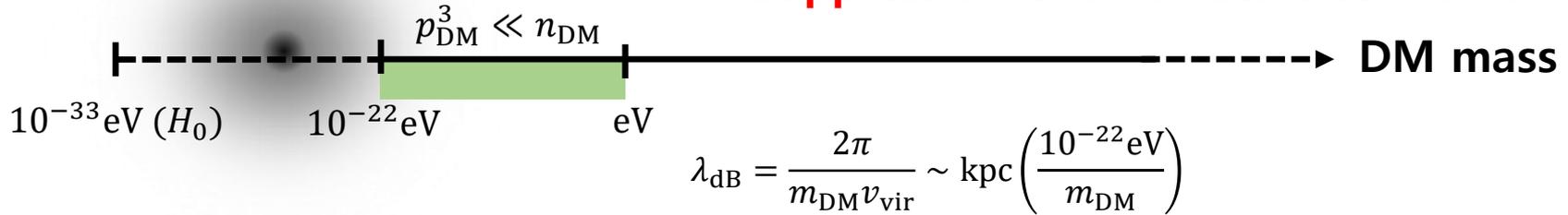
$$\left(\frac{\rho_{DM}}{\rho_{tot}}\right) \simeq 0.25 \left(\frac{f_a}{10^{12}\text{GeV}}\right)^{\frac{7}{6}} \left(\frac{\phi_i}{f_a}\right)$$



Ly-alpha & 21cm Forest For Wave Dark Matter

Ultra-light scalar dark matter: High occupation number \rightarrow Wave feature

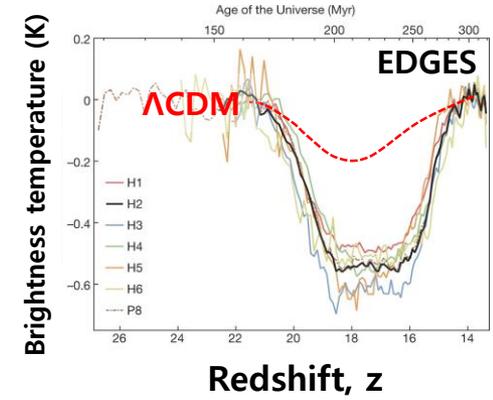
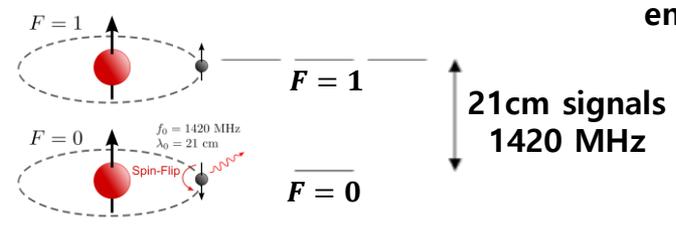
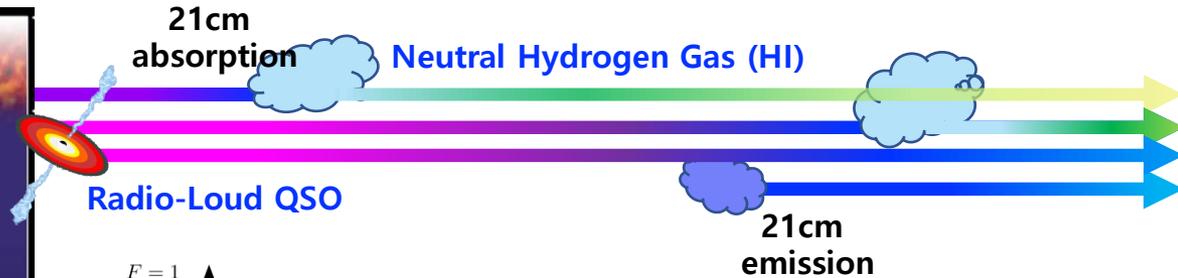
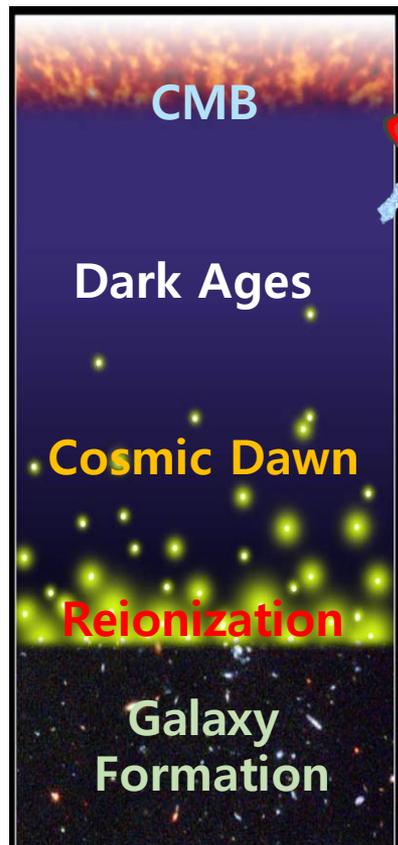
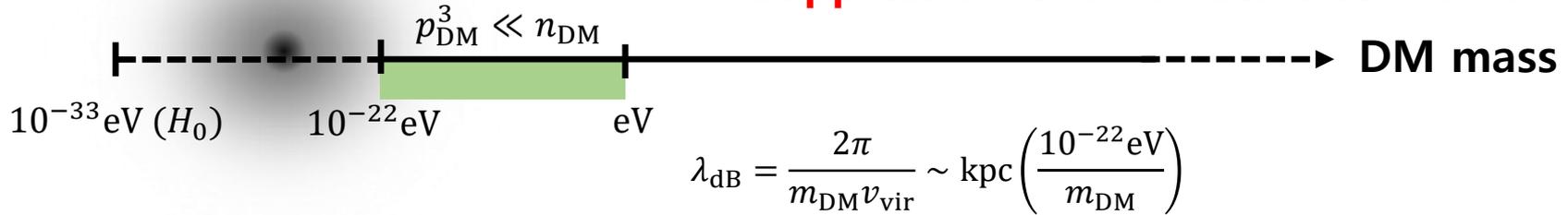
\rightarrow Suppression of small scale structure



Ly-alpha & 21cm Forest For Wave Dark Matter

Ultra-light scalar dark matter: High occupation number \rightarrow Wave feature

\rightarrow **Suppression of small scale structure**



Taken from Nature 555, 67–70 (2018)

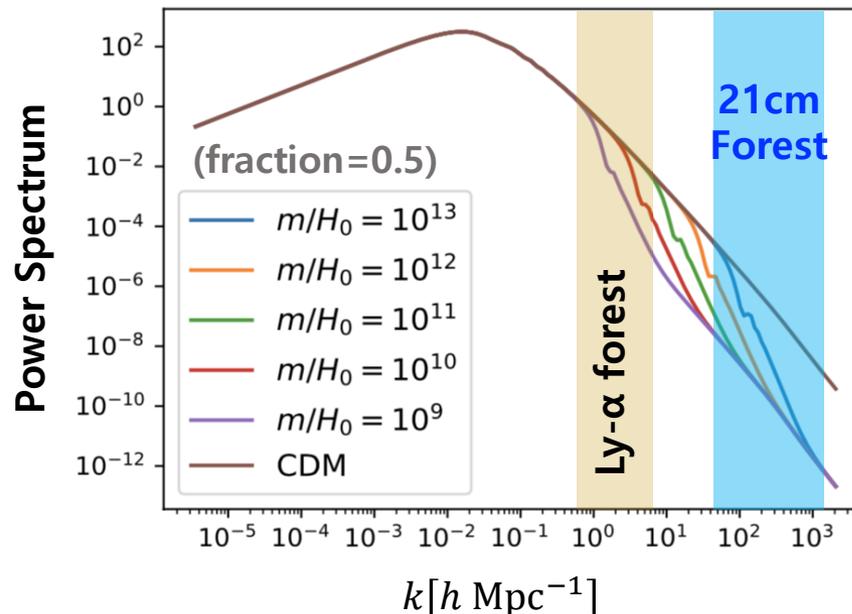
Ly-alpha & 21cm Forest For Wave Dark Matter

The Ly-alpha forest gives the strong constraint on wave DM for a certain mass range

The 21cm forest could be **more powerful to constrain wave dark matter** with a higher mass range than using the Lyman alpha forest [Shimabukuro, Ichiki, Kadota Phys. Rev. D 101 (2020) 4, 03516]

Ly- α forest: $M_{\text{DM}} \gtrsim 10^{-21} \text{eV}$

21cm forest: $M_{\text{DM}} \gtrsim 10^{-18} \text{eV}$

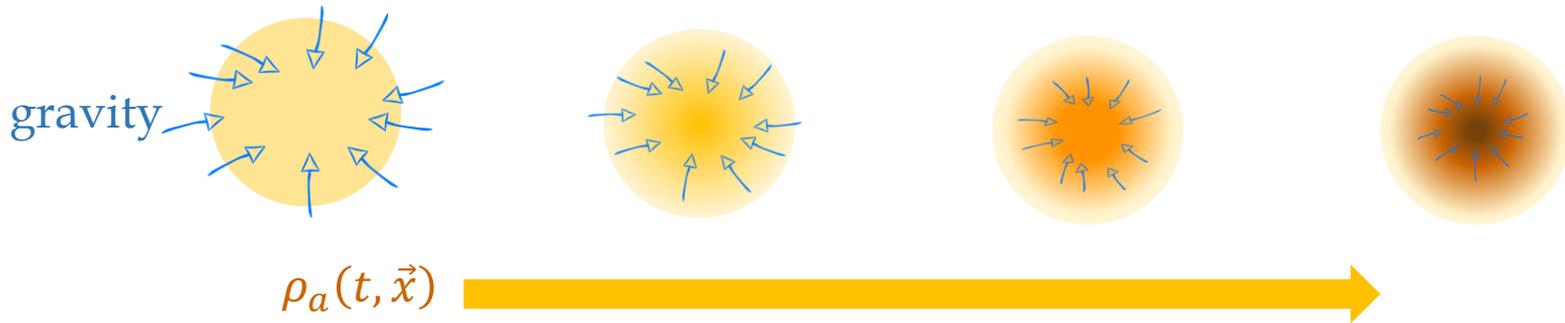


Wave dark Matter: Soliton core, quasiparticles

The homogenous evolution of the axion will eventually be destroyed by gravity:

Starting from $\rho_a(t, \vec{x}) \simeq \frac{1}{2}(\dot{\phi}^2 + (\nabla\phi)^2 + m_a^2\phi^2) = \bar{\rho}_a(t)(1 + \delta_a(t, \vec{x}))$ $(\delta_a(t, \vec{x}) \ll 1)$

$\delta_a(t, \vec{x})$ can grow by self-gravity and becomes $\delta_a(t, \vec{x}) = O(1) \rightarrow$ nonlinear evolution



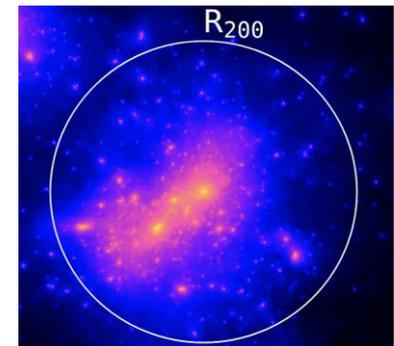
For usual cold dark matter case, clump does not directly collapse to black hole

Instead, it is virialized as $2\langle K \rangle \simeq -\langle V \rangle$ for

$$K = \sum \frac{1}{2} m_i v_i^2, \quad V = - \sum \frac{G m_i m_j}{r_{ij}}$$

Roughly for a halo mass M_h , with a size R , virial velocity:

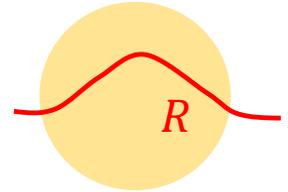
$$v_{vir}^2 \sim \frac{GM_h}{R}$$



Wave dark Matter: Soliton core, quasiparticles

For a **gravitationally bound** object made by axion field with a mass M_h and a size R , there is one more ingredient: **irreducible gradient energy by its size**

$$\rho_a \simeq \frac{1}{2} (\dot{\phi}^2 + (\nabla\phi)^2 + m_a^2\phi^2) \sim \frac{1}{2} m_a^2\phi^2 + O(m_a^2 a^2 v_{vir}^2) + \frac{\phi^2}{2R^2}$$



Including gravity, total energy becomes

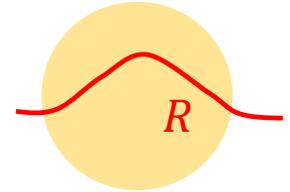
$$E_h = \left(\int d^3x \rho_a \right) - \frac{GM_h^2}{R} = M_h + M_h \left(O(v_{vir}^2) + \frac{1}{2m_a^2 R^2} - \frac{GM_h}{R} \right)$$

rest mass energy

Wave dark Matter: Soliton core, quasiparticles

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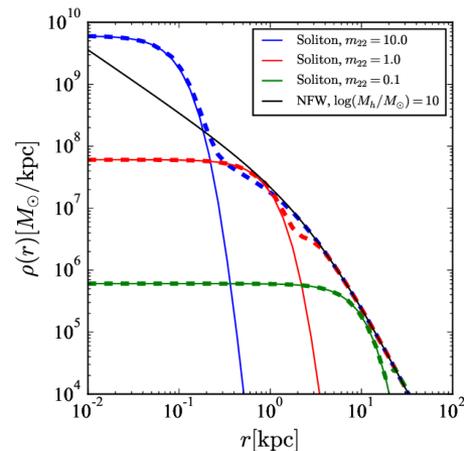
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rest mass energy

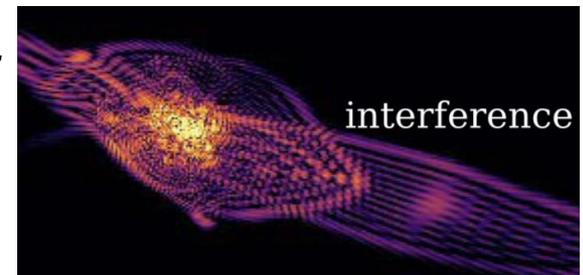
Like a hydrogen atom, the pressure by the gradient energy (“quantum pressure by uncertainty principle”) provide the minimum size of the halo: **Solitonic bound state**

$$\frac{1}{m_a^2 R^2} \lesssim v_{vir}^2 \sim \frac{GM_h}{R} \rightarrow R_{soliton} = \frac{1}{m_a^2 GM_h} \lesssim R \left(M_h \sim \frac{M_{Pl}^2}{m_a} v_{vir} \right)$$



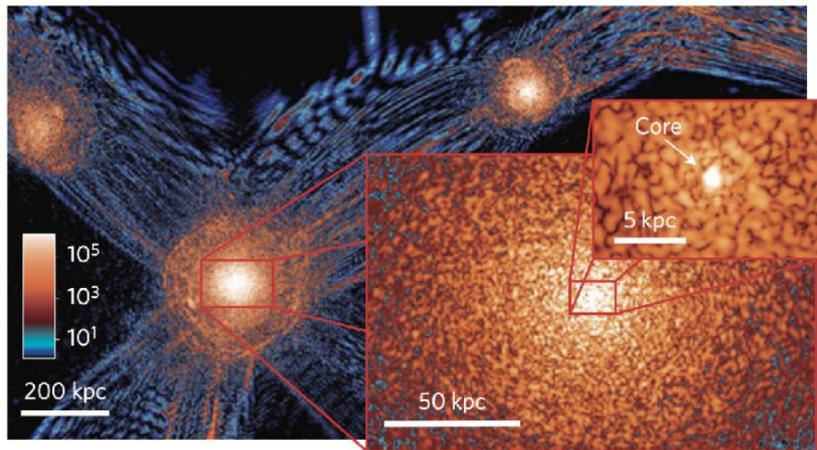
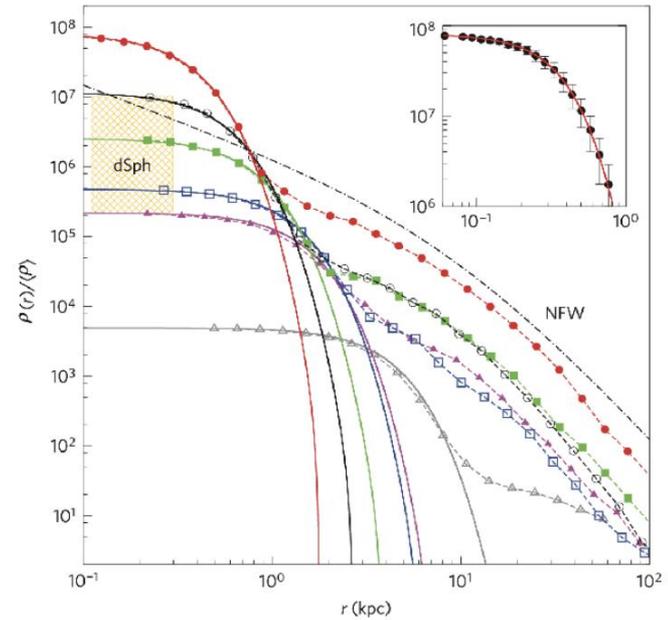
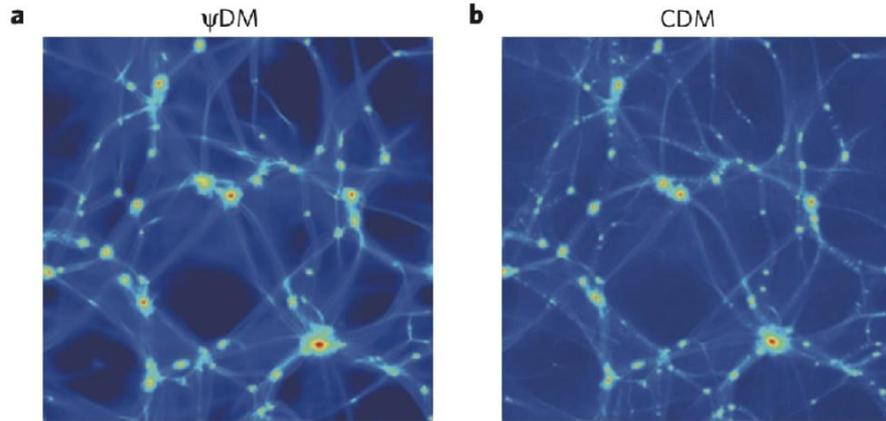
Astrophysical “de Broglie wavelength”

$$\lambda_{dB} = \frac{2\pi}{m_a v_{vir}} \sim kpc \left(\frac{10^{-22} eV}{m_a} \right)$$



Wave DM simulation

Schive, Chiueh, Broadhurst (14)



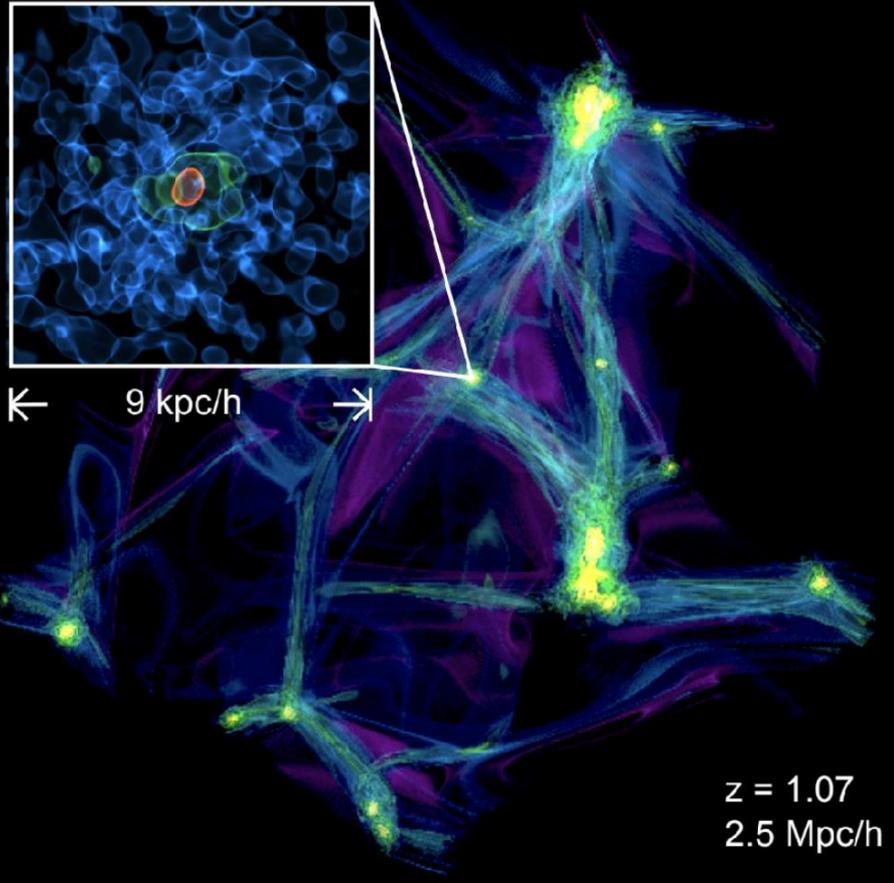
* characteristic *soliton* at the center has been observed

* small scale structures are erased

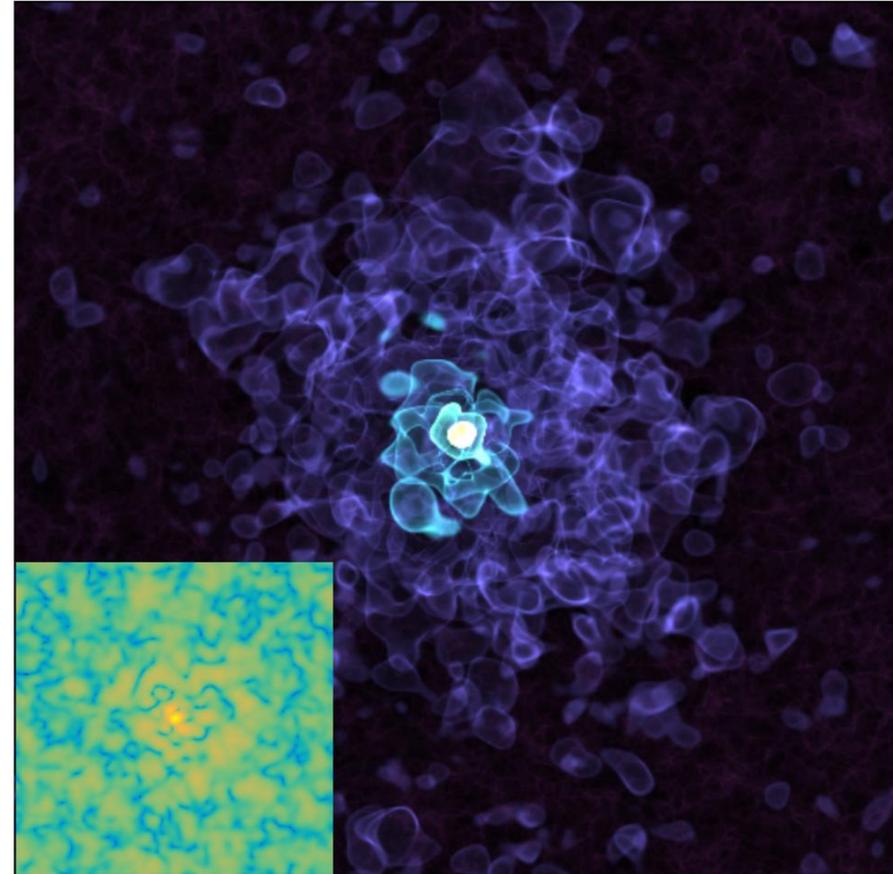
From H. Kim's slide in NPFI workshop

Wave DM simulation

Mocz et al (17)



Veltmaat, Niemeyer, Schwabe (18)



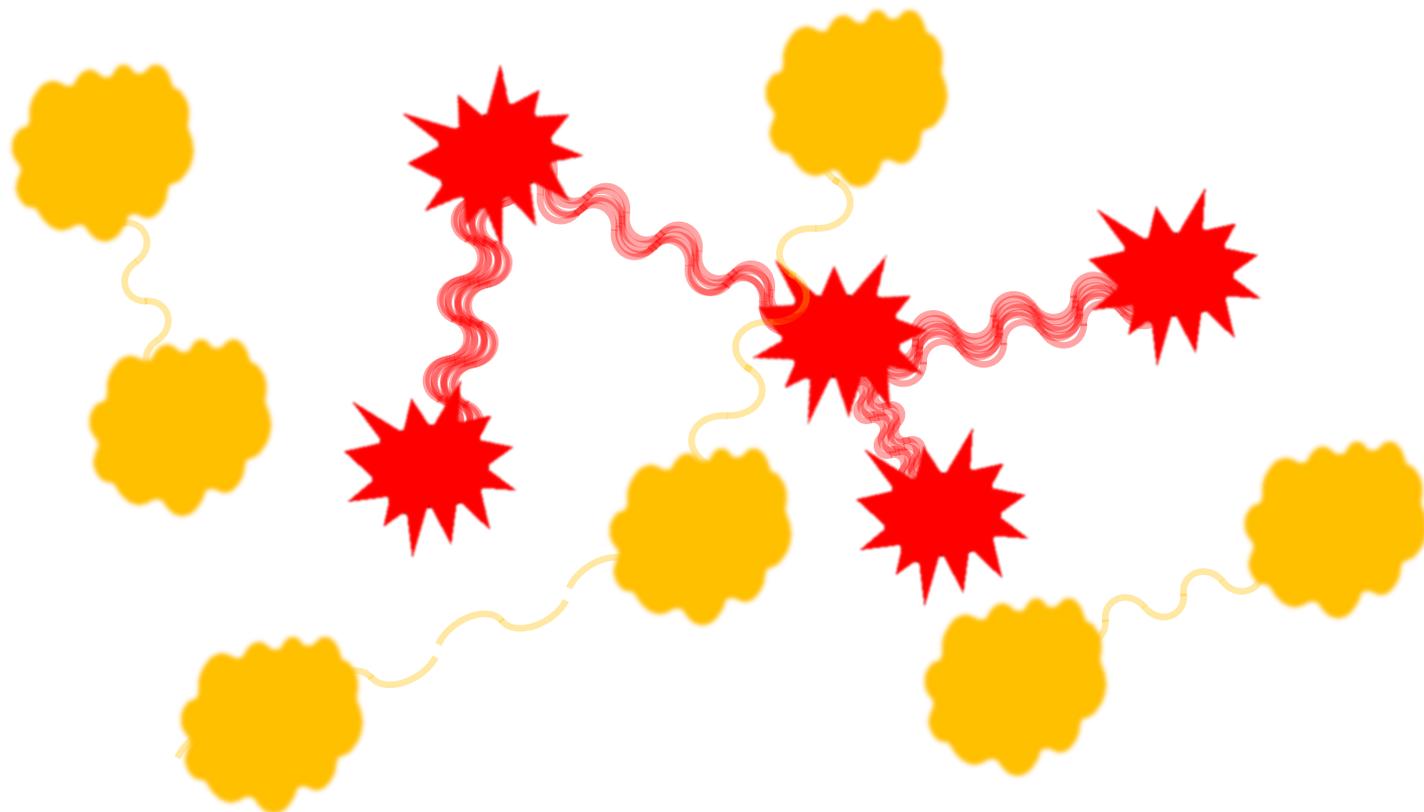
From H. Kim's slide in NPFI workshop

Wave DM + Self interacting Sub DM

Naturally light scalar dark matter

-  Axion 타입 : 가벼울수록 약하게 서로 상호작용
-  Glueball 타입 : 가벼울수록 강하게 서로 상호작용

*Bugeon Jo, Hyeontae Kim, Hyung Do Kim, CSS
Phys. Rev. D 103, 083528 (2021)*



Multi component (매우 약한 상호작용 + 매우 강한 상호작용) scalar dark matter scenario

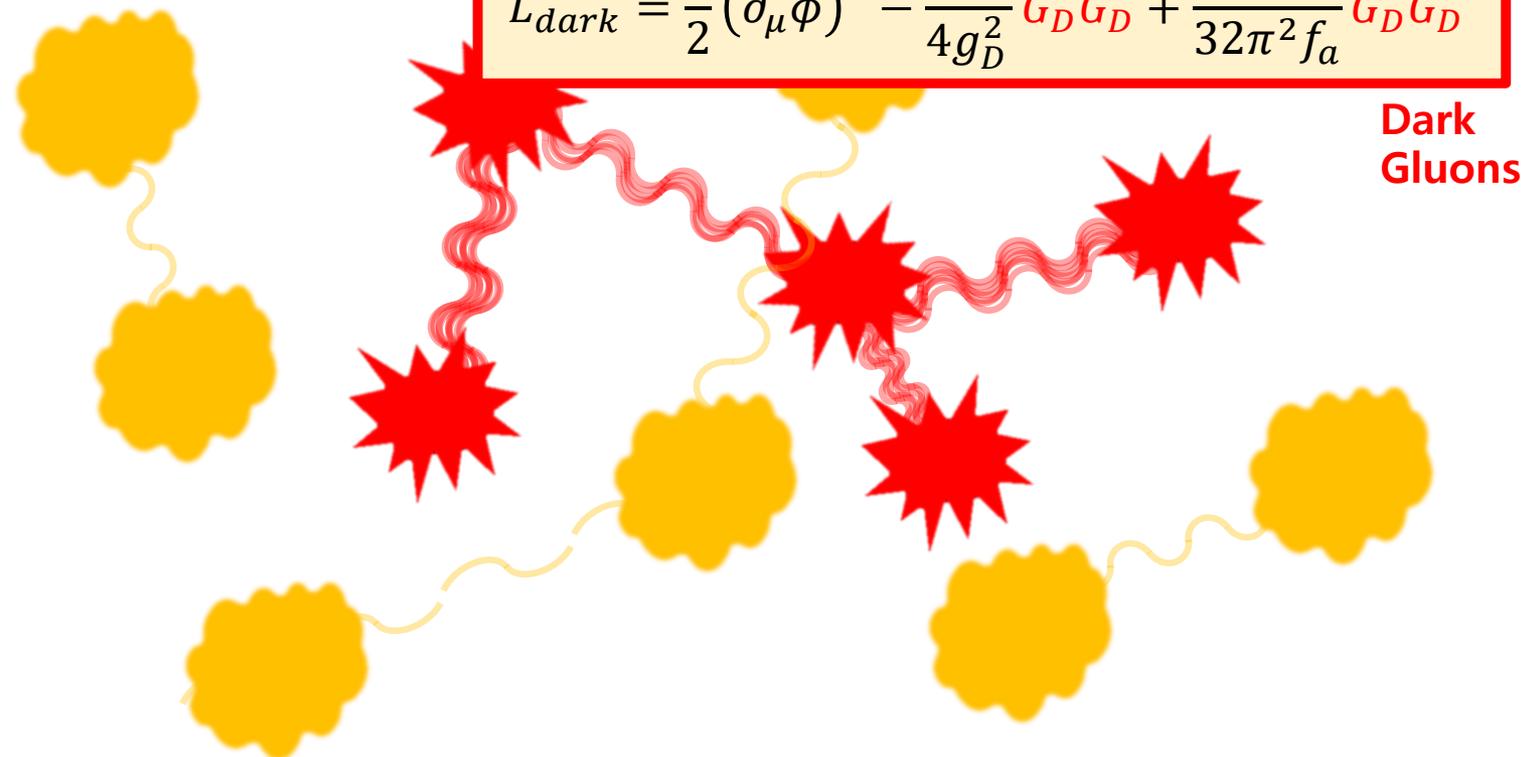
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$$L_{dark} = \frac{1}{2} (\partial_\mu \phi)^2 - \frac{1}{4g_D^2} G_D G_D + \frac{\phi}{32\pi^2 f_a} G_D \tilde{G}_D$$



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**Dark
Gluons**

$$L_{eff} = \frac{1}{2} (\partial_\mu \varphi_g)^2 - \frac{1}{2} m_g^2 \varphi_g^2 + \frac{a_3}{3!} \frac{4\pi}{N} m_g \varphi_g^3 + \frac{a_4}{4!} \left(\frac{4\pi}{N}\right)^2 \varphi_g^4 + \frac{a_5}{5!} \frac{1}{m_g} \left(\frac{4\pi}{N}\right)^3 \varphi_g^5 + \dots$$

$$+ \frac{1}{2} (\partial_\mu \phi)^2 - N^2 \Lambda^4 \left(\frac{c_2}{2} \left(\frac{\phi}{N f_a}\right)^2 + \frac{c_4}{4!} \left(\frac{\phi}{N f_a}\right)^4 + \dots \right)$$

**Dark
Glueball**

Multi component (**매우 약한 상호작용** + **매우 강한 상호작용**) scalar dark matter scenario

Supermassive Black Holes (SMBH) at High z

In the 2010s, new observations of the quasars lead to the discovery of SMBHs around $z = 7$.

Around the redshift $z = 7$ ($t \simeq 770$ Myr $\sim 0.05 t_U$),

J1342+0928 ($z = 7.54, M_{BH} = 0.8 \times 10^9 M_\odot, 1712.01860$)

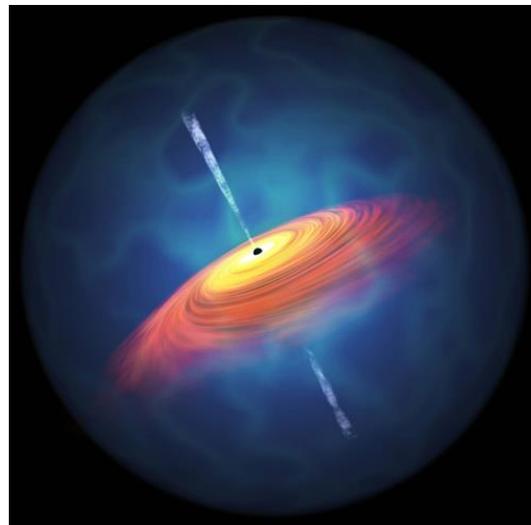
J1120+0641 ($z = 7.09, M_{BH} = 2.0 \times 10^9 M_\odot, 1106.6088$)

J2348-3054 ($z = 6.89, M_{BH} = 2.1 \times 10^9 M_\odot, 1311.3260$)

J0109-3047 ($z = 6.75, M_{BH} = 1.5 \times 10^9 M_\odot, 1311.3260$)

J0305-4150 ($z = 6.61, M_{BH} = 1.0 \times 10^9 M_\odot, 1311.3260$)

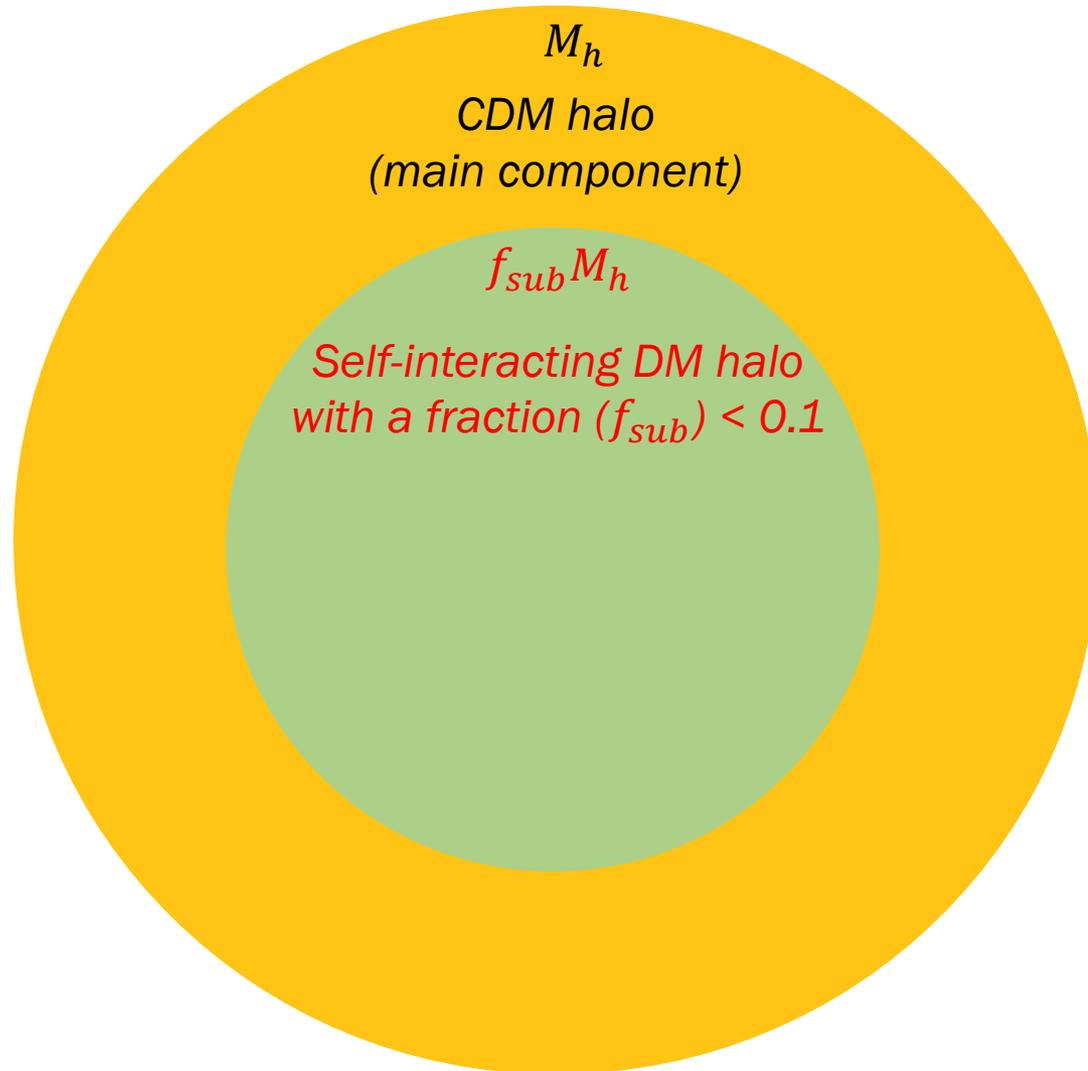
J0100+2802 ($z = 6.3, M_{BH} = 1.2 \times 10^{10} M_\odot, 1502.07418$)



The origins of these SMBHs are not clear. It may originate from strongly self-interacting subcomponent DM : **dark glueball (strongly self-interacting) subcomponent DM**

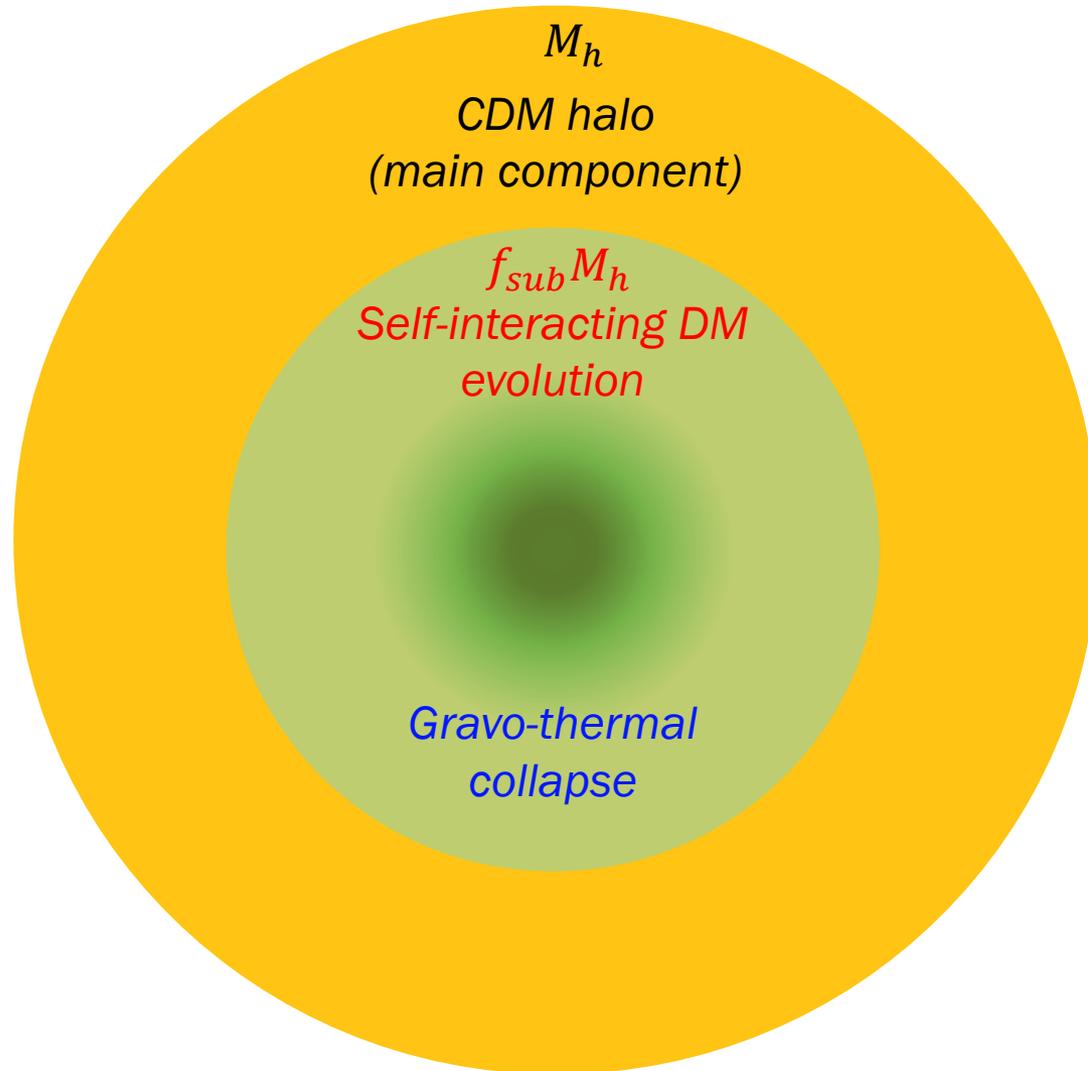
Effect of Subcomponent Self-interacting DM

Beyond the CDM framework : multi-component with strongly interacting sub-comp. DM



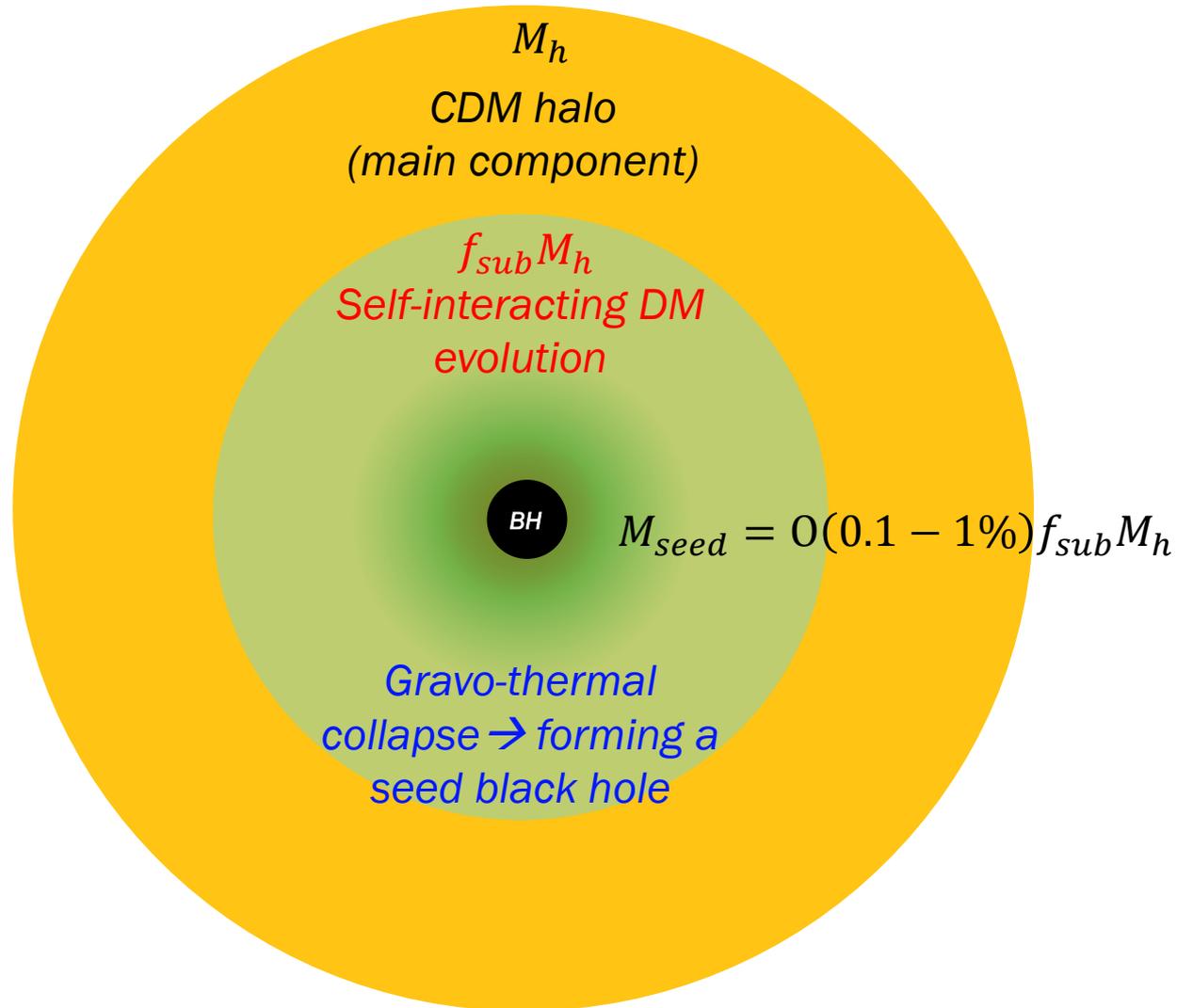
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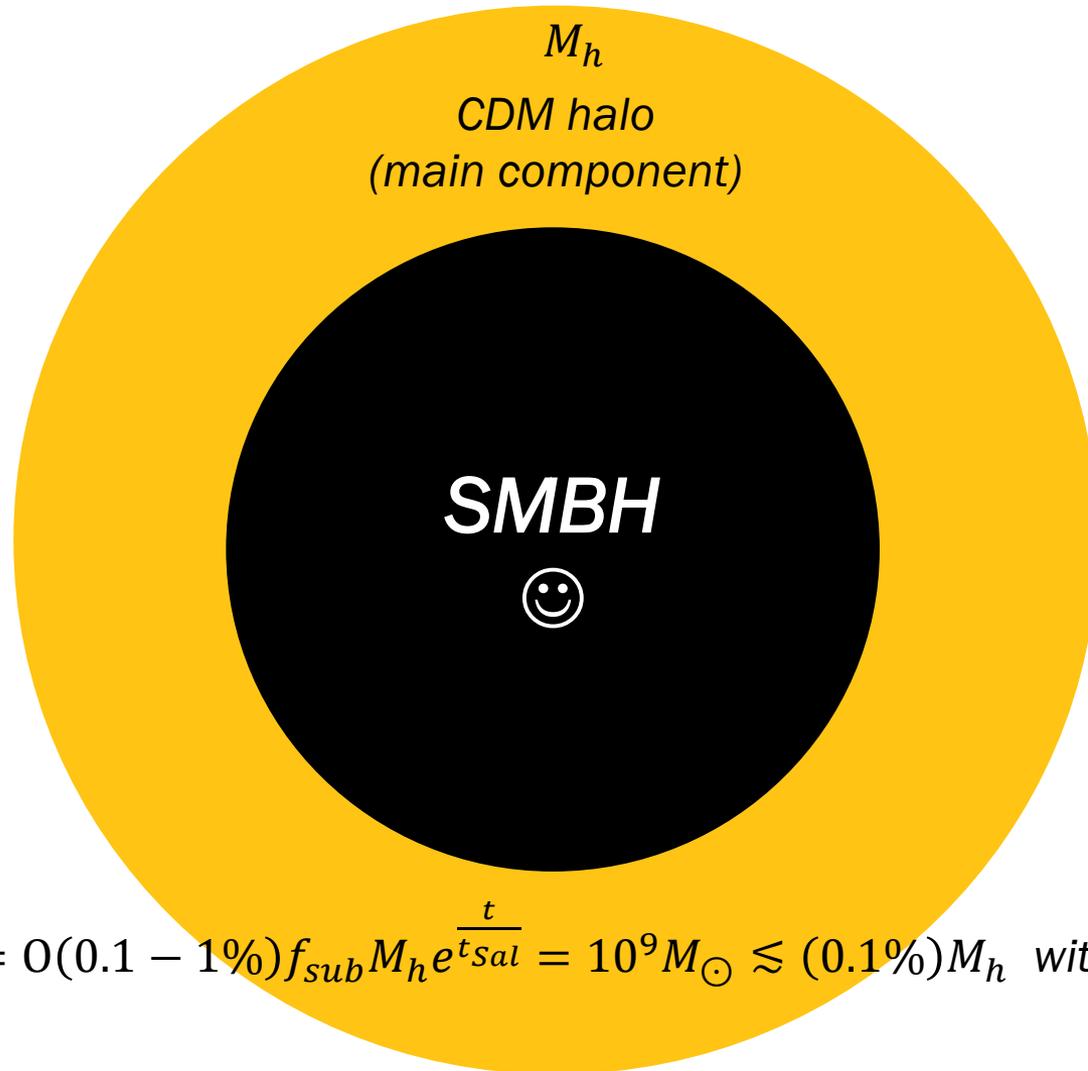
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Effect of Subcomponent Self-interacting DM

Beyond the CDM framework : multi-component with strongly interacting sub-comp. DM



$$M_{BH}(t) = 0(0.1 - 1\%)f_{sub}M_h e^{\frac{t}{t_{sal}}} = 10^9 M_{\odot} \lesssim (0.1\%)M_h \text{ with } M_h = 10^{12} M_{\odot}$$

Gravo-Thermal Collapse

Thermally equilibrated system which is bound by gravity

If the system is in equilibrium with gravity, the system has a negative specific heat capacity

$$c_T = \frac{dE}{dT} < 0$$

Why? Thermal equilibrium \rightarrow thermal energy (kinetic energy) is virialized by potential energy

$$\langle V \rangle = -2\langle K \rangle \rightarrow E = Nm + \langle V \rangle + \langle K \rangle = Nm - \langle K \rangle = Nm - NT \rightarrow \frac{dE}{dT} = -N \simeq -\frac{E}{m}$$

(c.f. black hole: $E = M_{BH}$, $T = \frac{M_P^2}{M_{BH}} = \frac{M_P^2}{E} \rightarrow \frac{dE}{dT} = -\frac{E}{T} < 0$)

Negative heat capacity \rightarrow instability

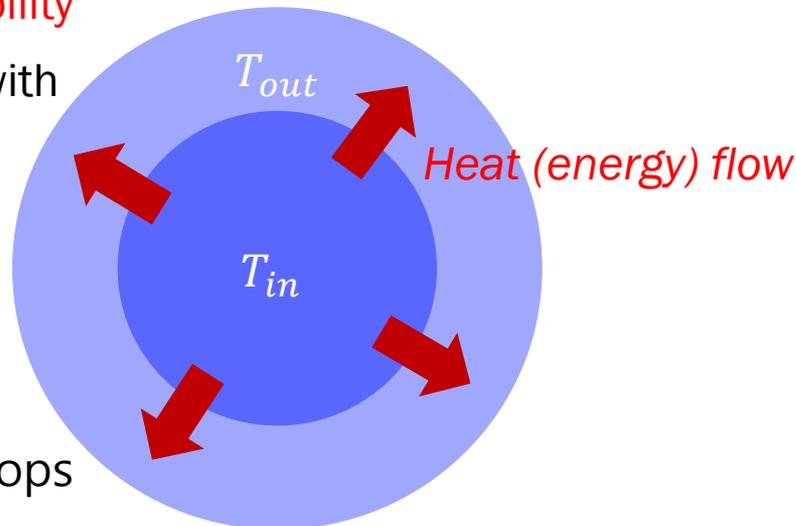
Considering the bound system with initial temperature gradient

$$T_{in} > T_{out}$$

For the positive c_T case,

T_{in} decreases, T_{out} increases

and meet at T_{eq} . Heat flow stops



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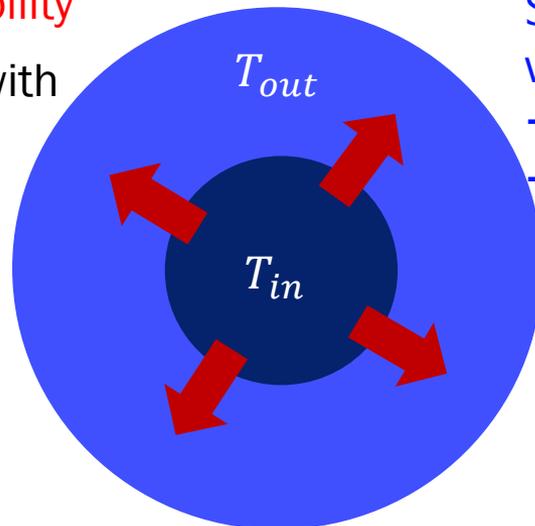
Negative heat capacity \rightarrow instability

Considering the bound system with initial temperature gradient

For the negative c_T case

Heat (energy) flow continues!

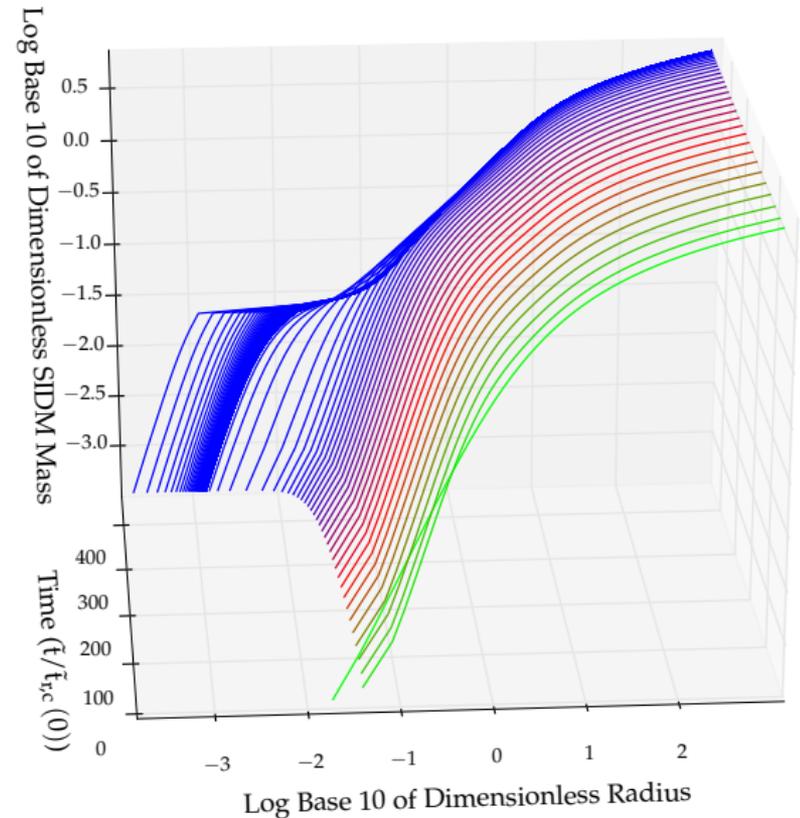
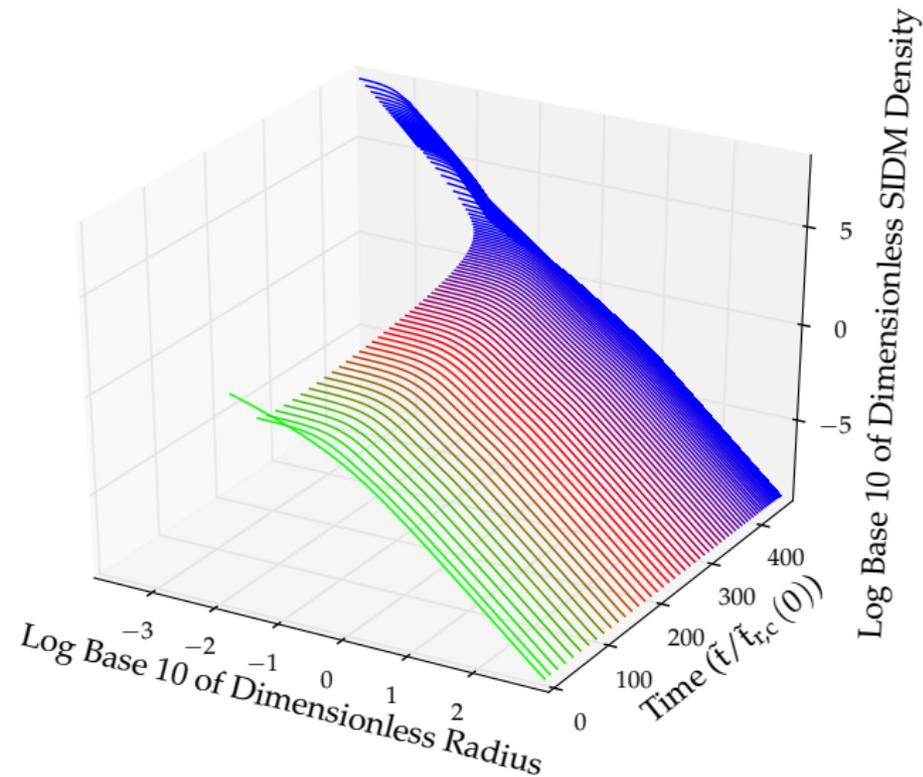
$T_{in} > T_{out}$ maintains forever!



Strongly bound system with high virial velocity \rightarrow leads to gravitational collapse \rightarrow forming a black hole

Gravo-Thermal Collapse

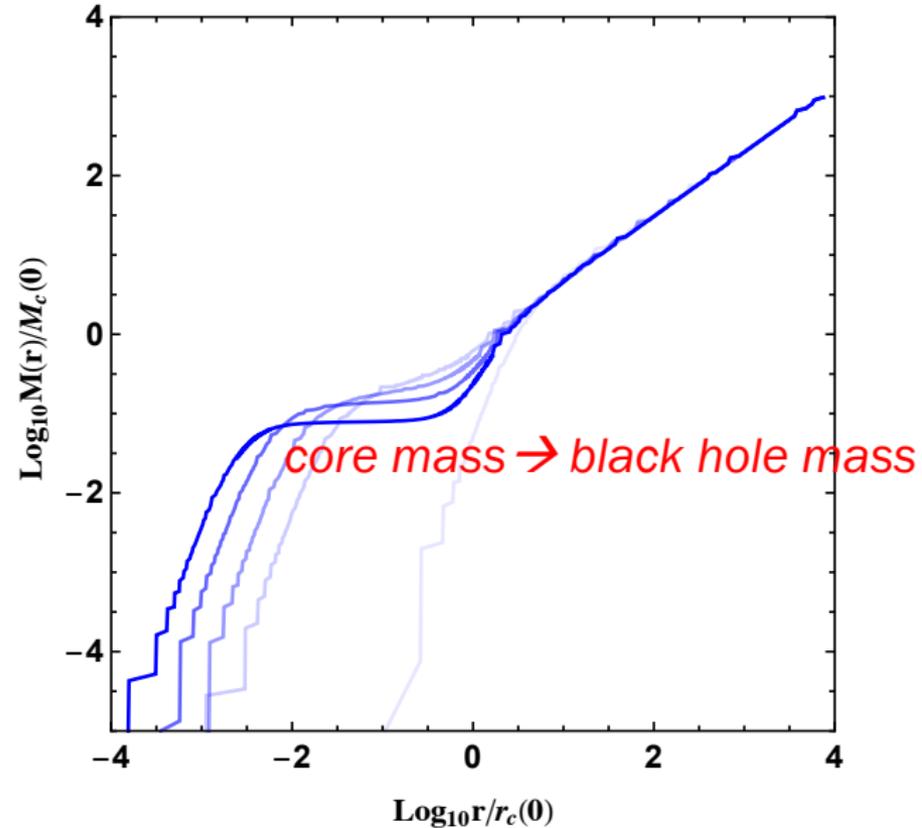
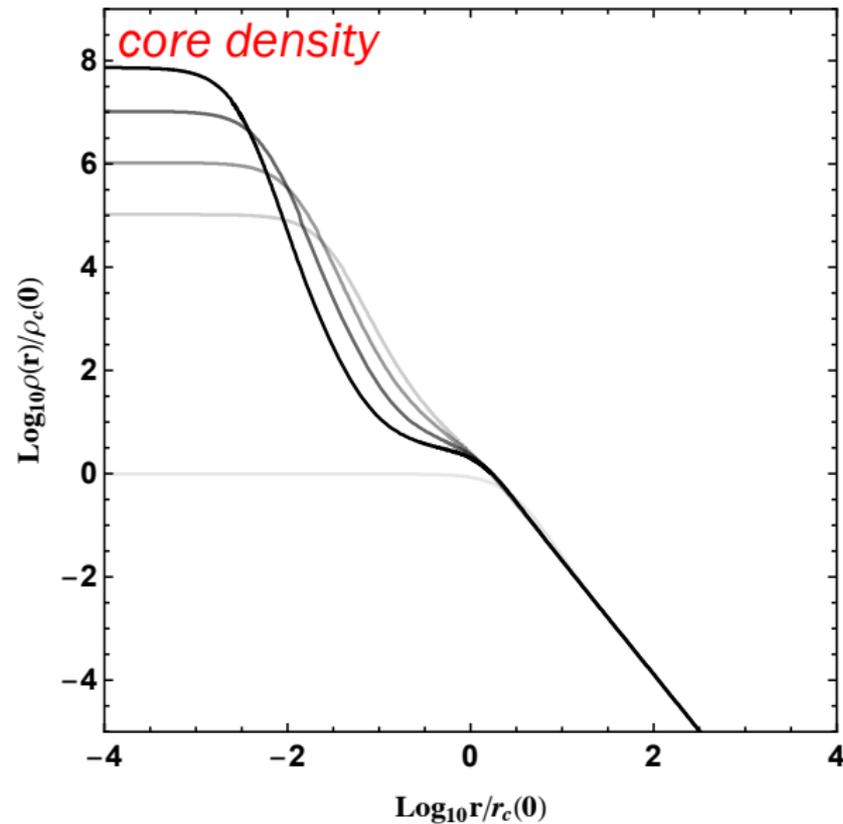
For the gravo-thermal collapse, maintaining thermal equilibrium is an important condition. Therefore the "relaxation time" should be shorter than the age of the Universe for a given z . How short? Numerical calculation is necessary



1501.00017 for the isolated halo with $f_{\text{sub}}=1$

Gravo-Thermal Collapse

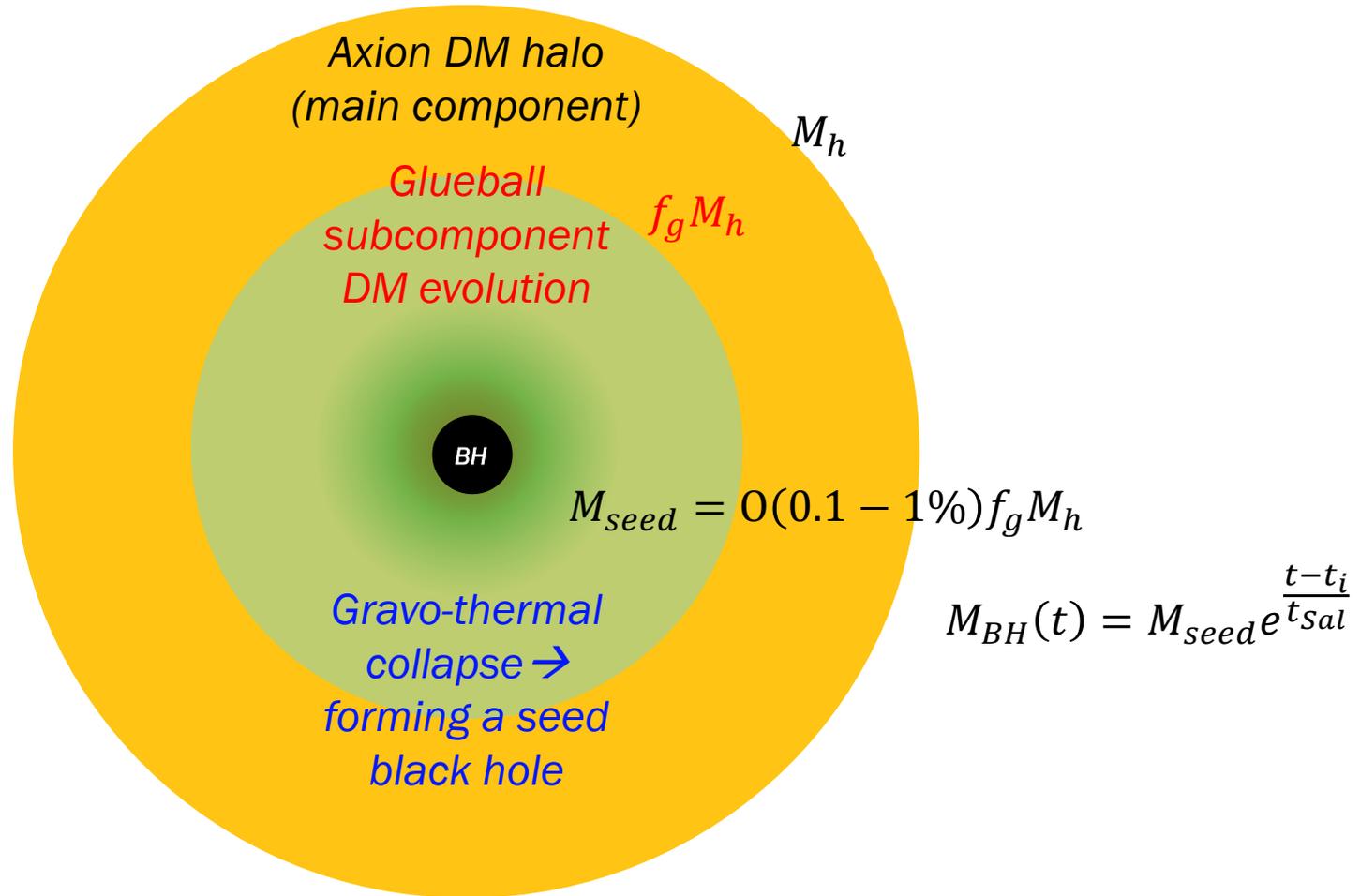
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Balberg et.al. 0110561 for the isolated halo with $f_{\text{sub}}=1$

Seed Black Hole Formation in Our Model

The large seed black hole can be made by the gravo-thermal collapse of the subcomponent glueball dark matter.

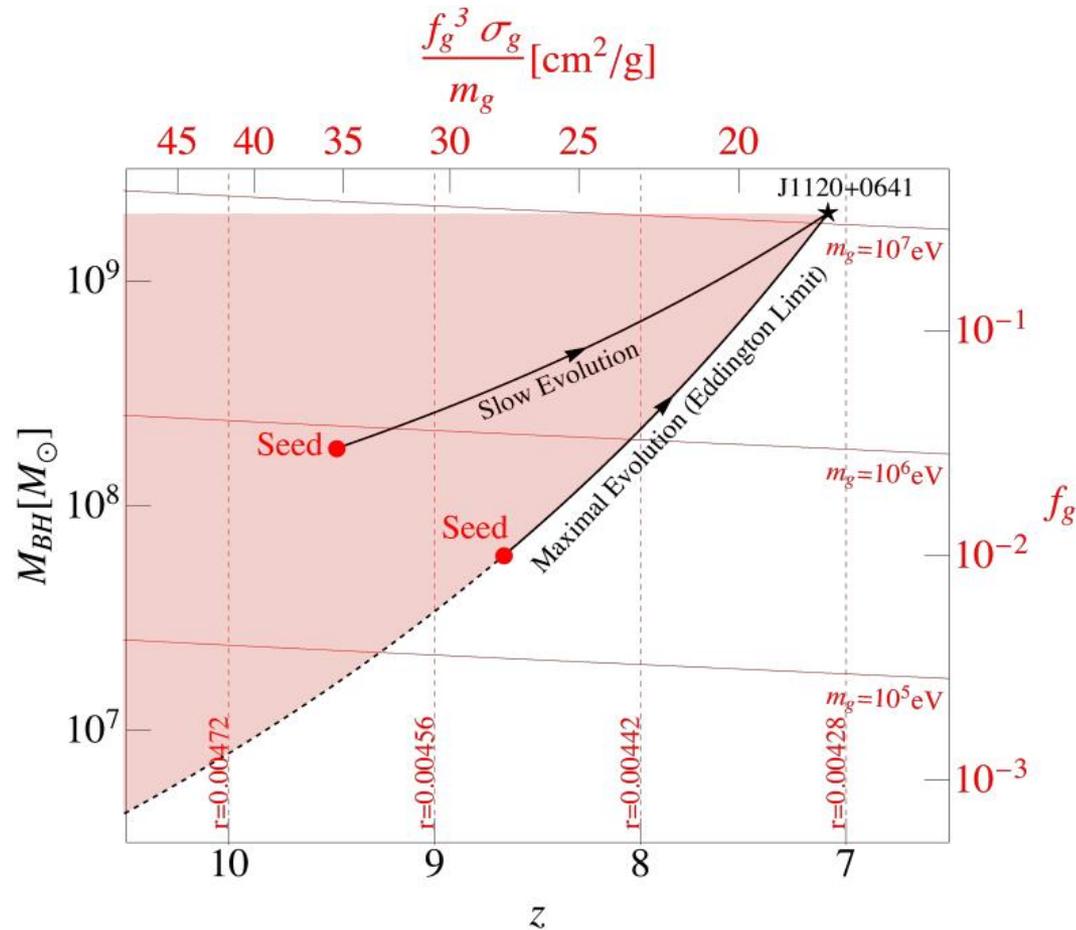


$$\Delta t_{col} \simeq \frac{480}{f_g^2} t_{relax}(t_i), \quad M_{seed} \simeq 0.006 f_g M_h$$

$$t_{relax}(t_i) = \frac{m_g}{\sigma_g f_g \rho_s(t_i) v_s(t_i)}$$

SMBH at High z for an Isolated Host Halo

The large seed black hole can be made by the gravo-thermal collapse of the subcomponent glueball dark matter.



for $M_h = 10^{12} M_{\odot}$

감사합니다.