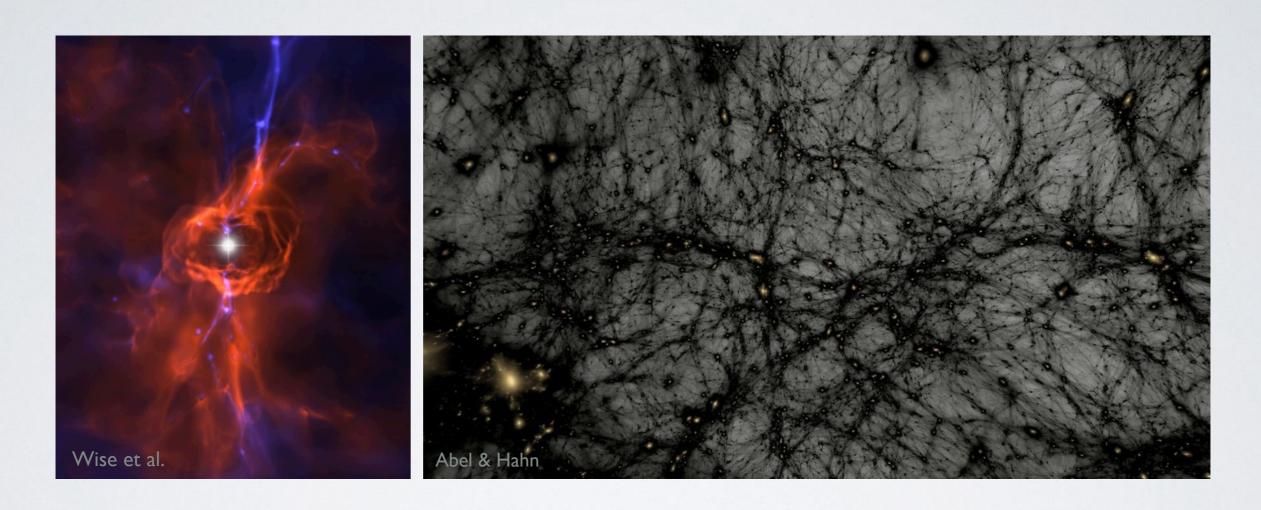
# KIAS Astrophysics Summer School Lecture #1 Introduction to Computational Astrophysics



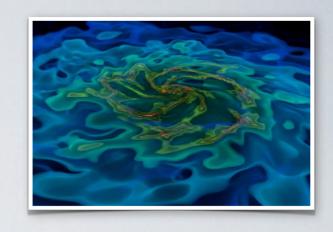
Ji-hoon Kim (Seoul National University)

## Today's Lecture: Outline

Computational Astrophysics: Need and Examples

Computational Astrophysics: Methodology

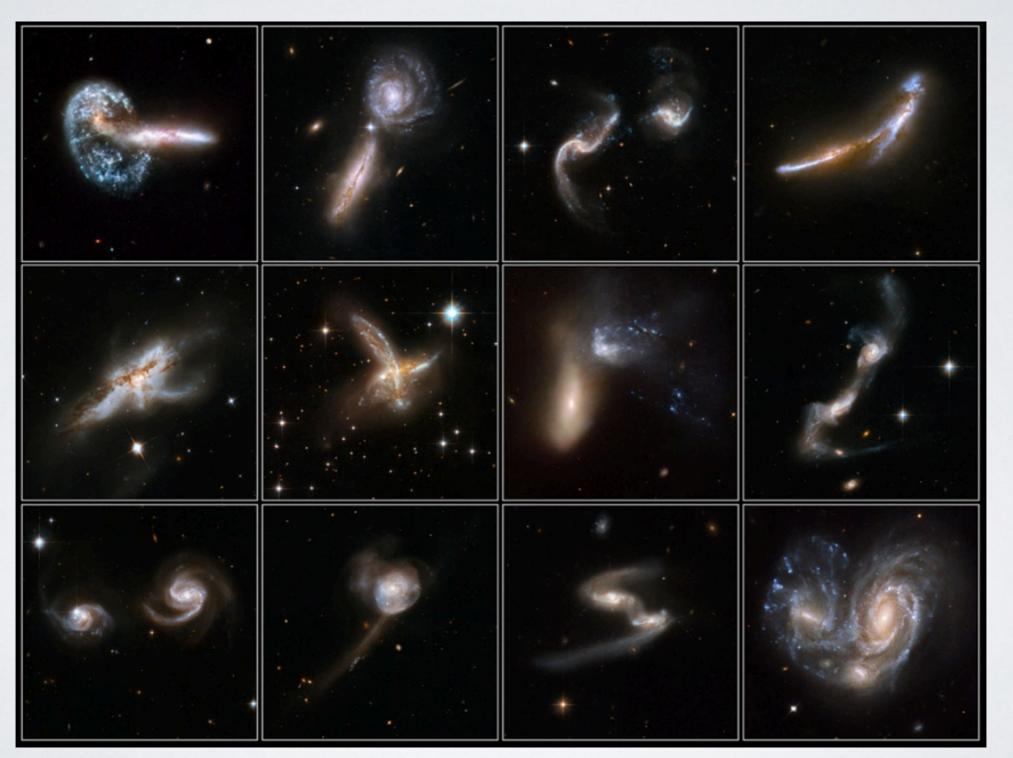
Computational Astrophysics: Future Ahead



# Computational Astrophysics: Why We Need It

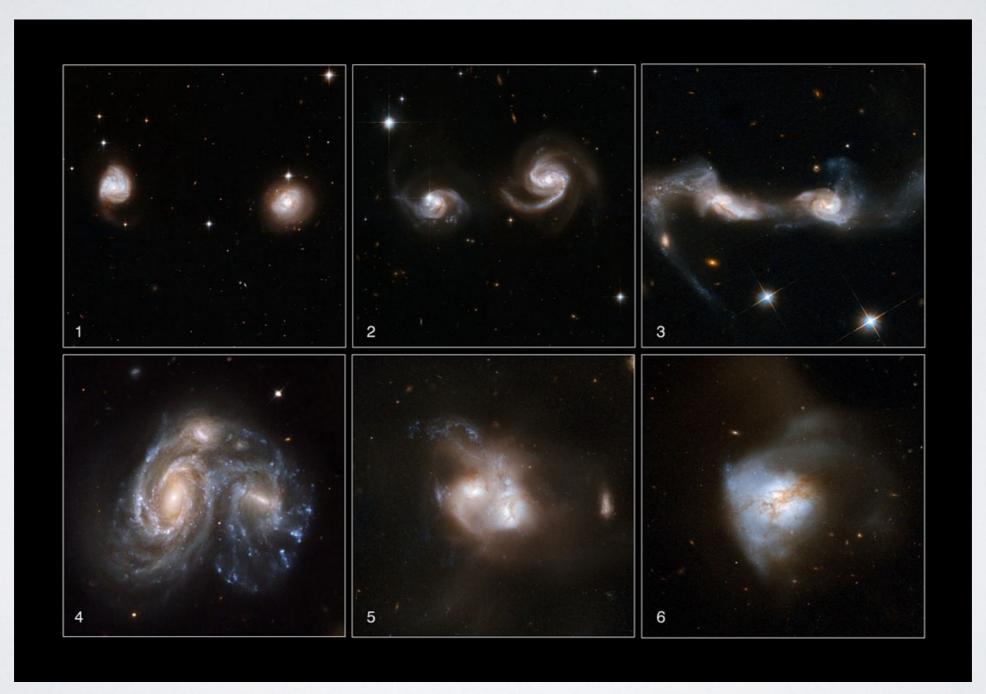
# Computational Cosmology: Need

• Observing the structure formation is humanly impossible, either.



## Computational Cosmology: Need

• Observing the structure formation is humanly impossible, either.



# Galaxy Merger Simulations

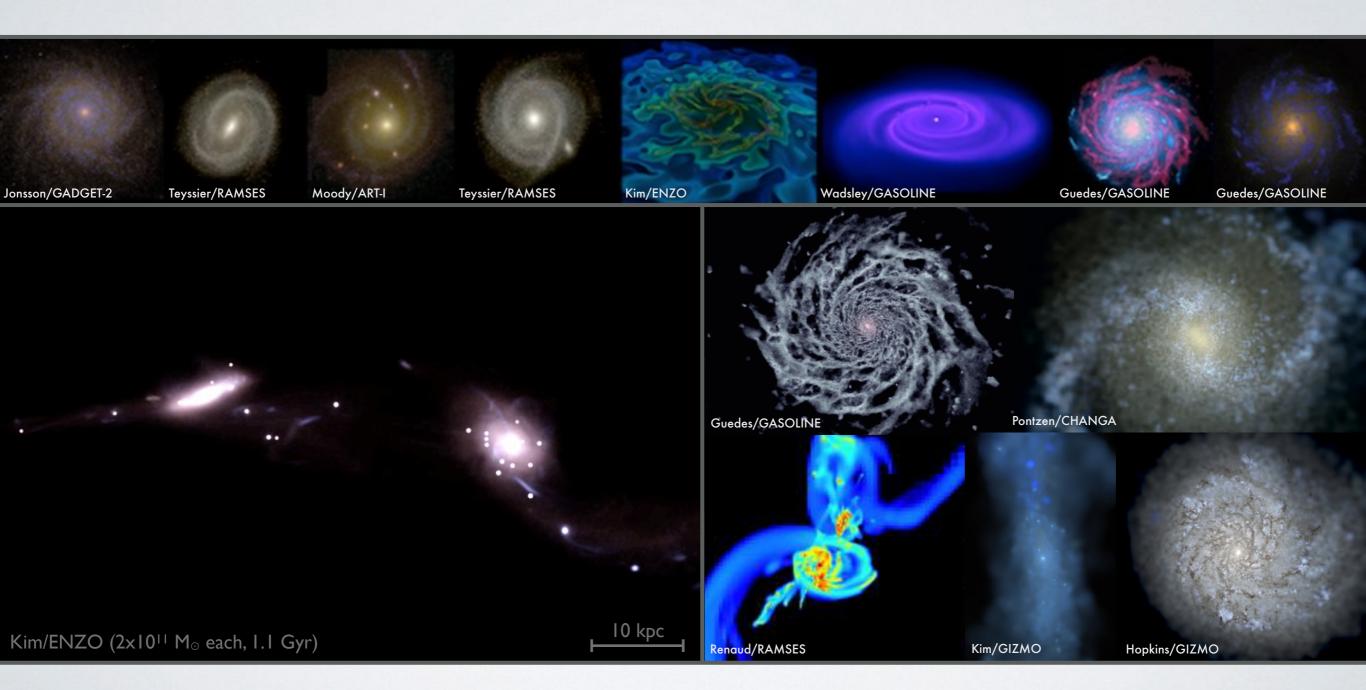
• If you want to see the whole process of galaxy mergers occurring in front of your eye, numerical simulation is the only way.

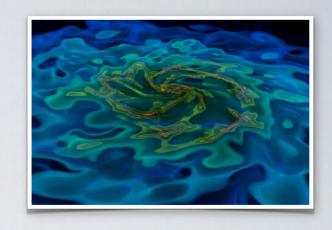




# Computational Cosmology: Need

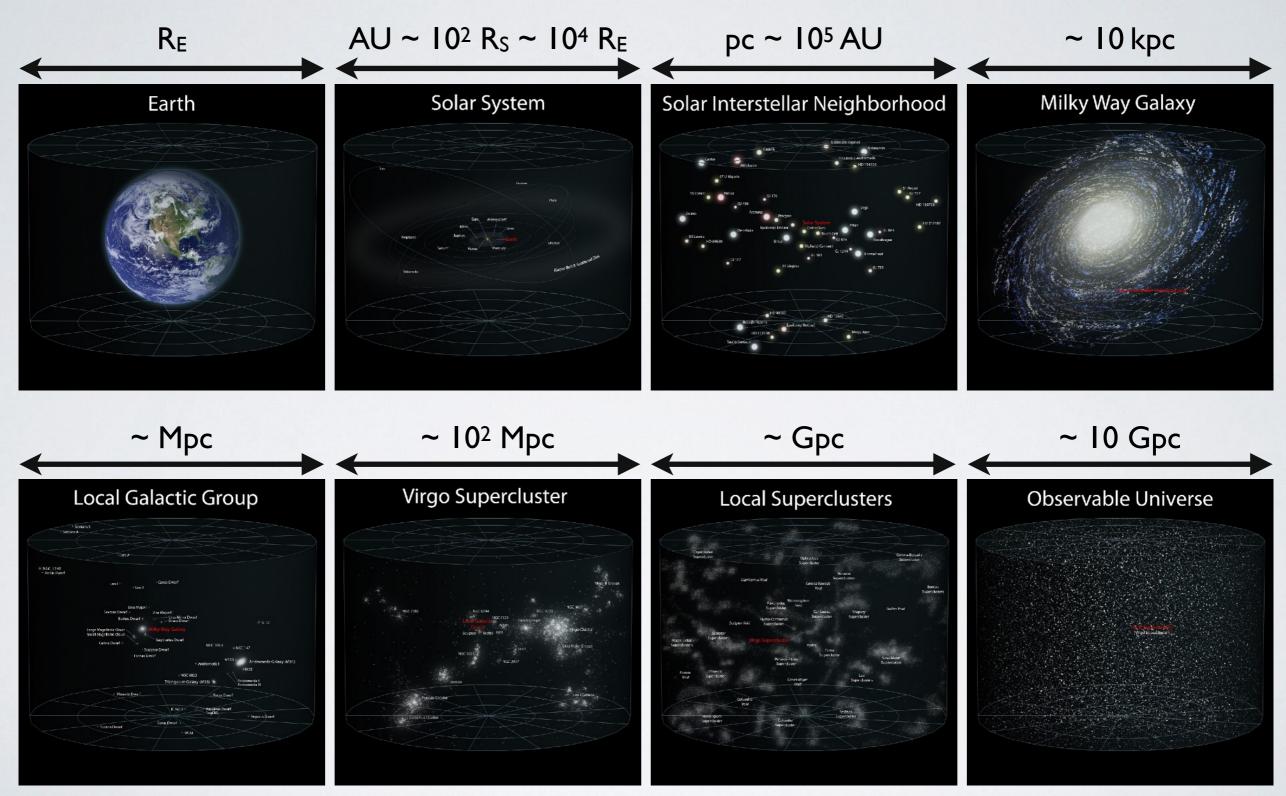
 Numerical experiment essential due to nonlinear nature of structure formation → only tool to test theory against observations





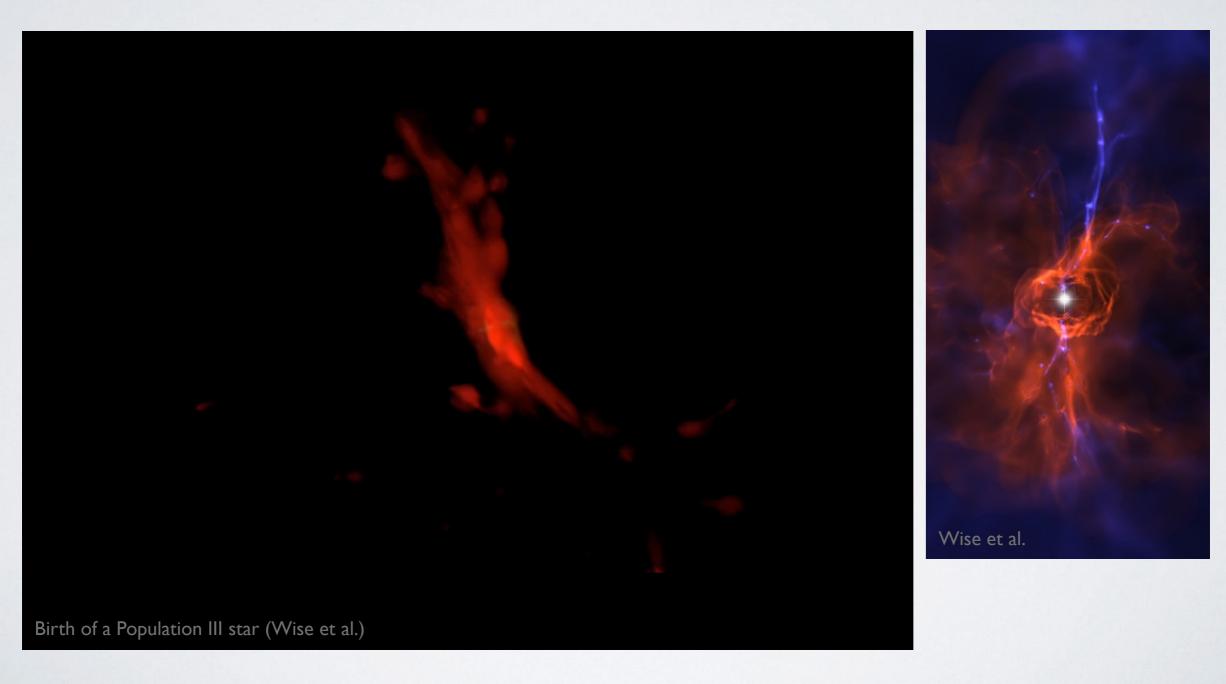
# Computational Astrophysics: Examples

# Scales of Cosmological Objects



#### First Stars and First Galaxies

• In the bottom-up structure formation scenario in which CDM produces small-scale powers, massive stars form first ( $\sim 10^2 M_{\odot}$ ).



#### First Stars and First Galaxies

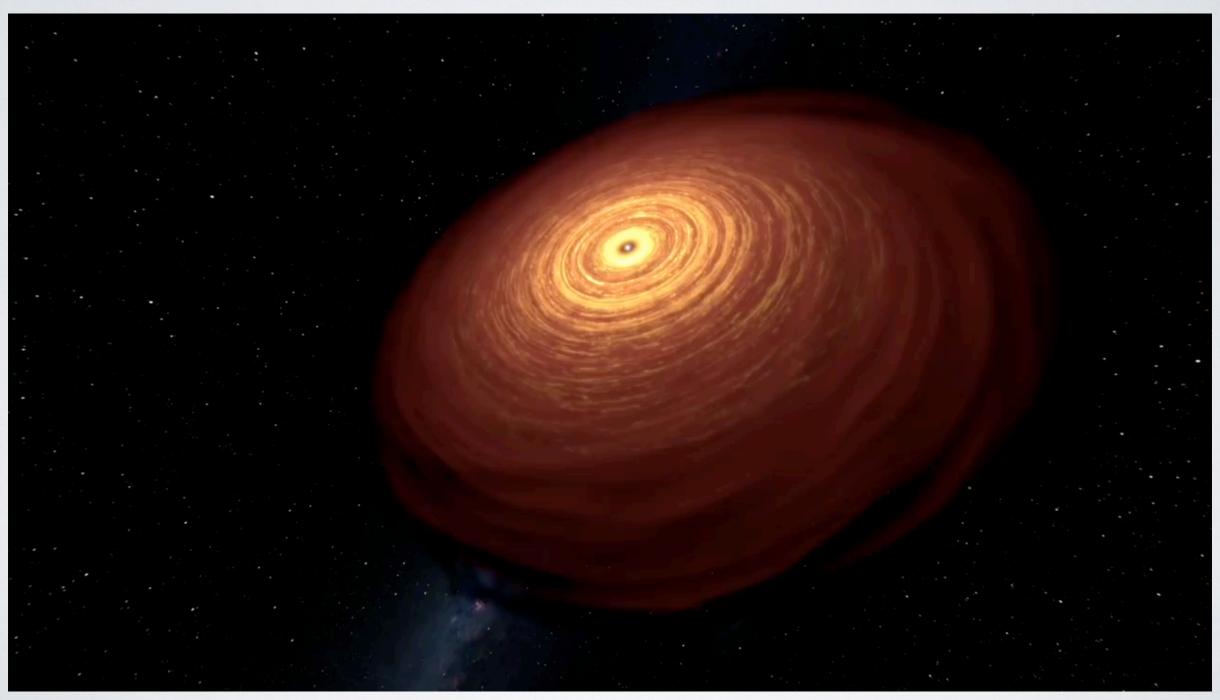
• In the bottom-up structure formation scenario in which CDM produces small-scale powers, massive stars form first ( $\sim 10^2 M_{\odot}$ ).





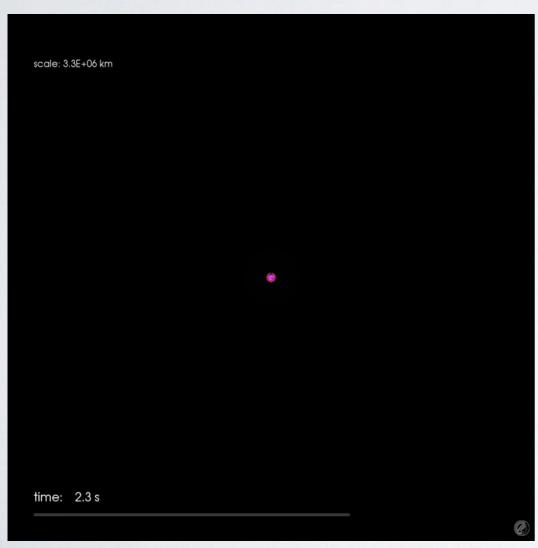
## Planet and Planetary System Formation

• A dense gas disk fragments to form a planetary system.



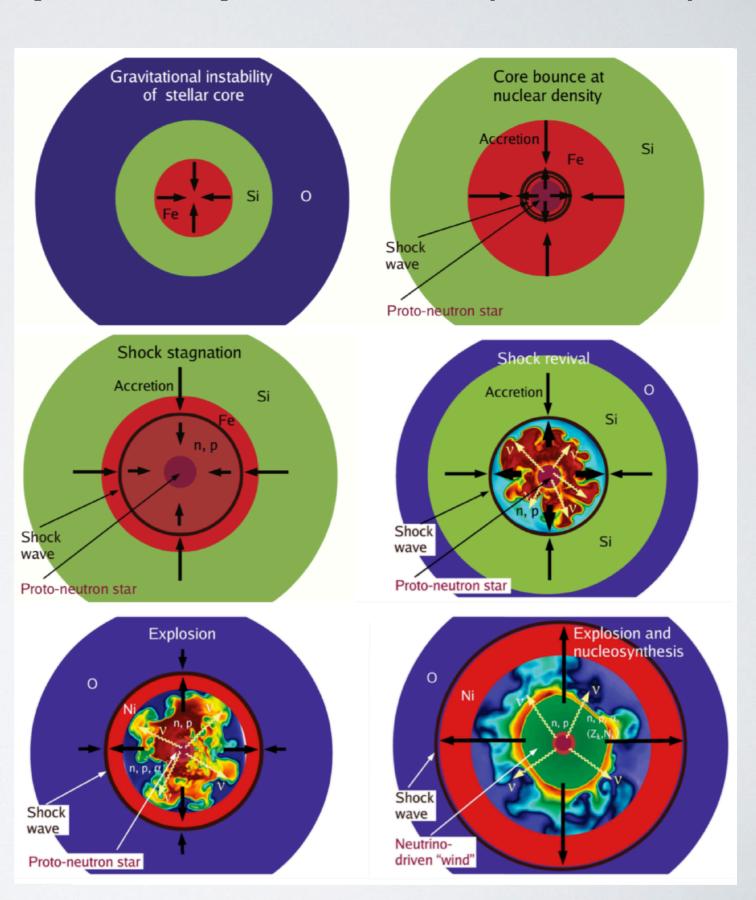
# Igniting Core-Collapse Supernova (CCSN)

 Neutrino plays an major role as it carries 99% of the total SN energy.



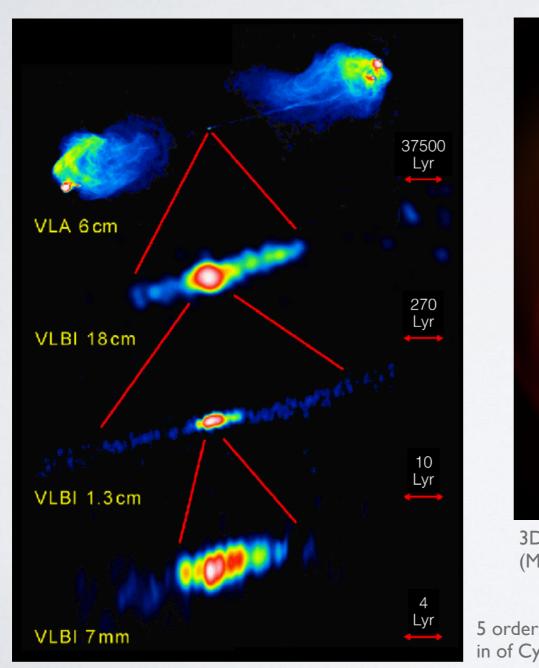
Hammer, Janka et al. (2010)

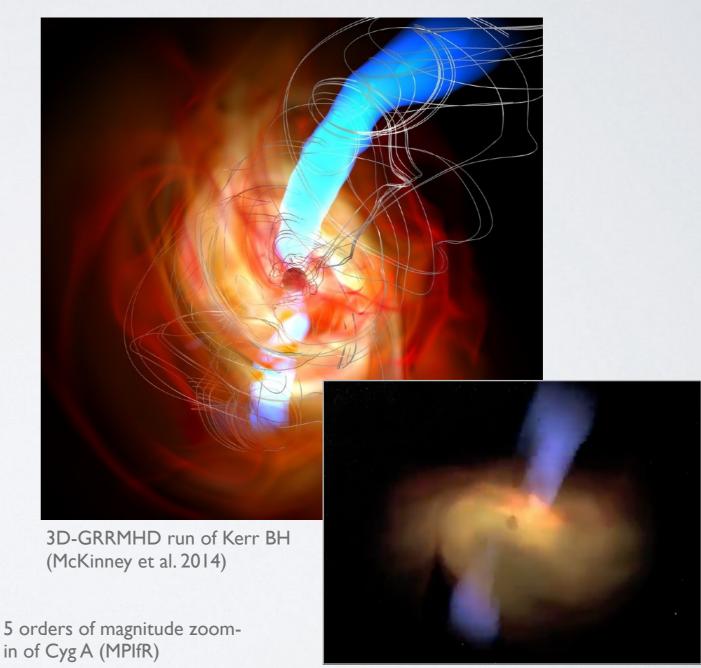
Janka et al. (2012)



#### Strong Jets From the Galactic Center

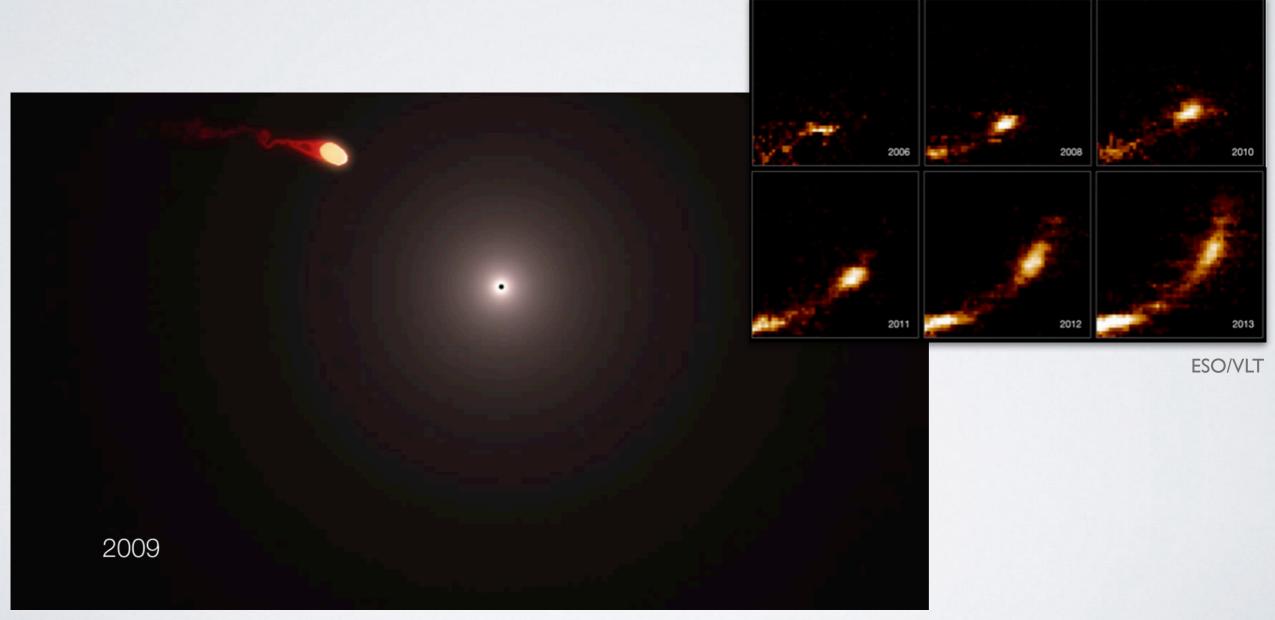
• Indicates a supermassive black hole or active galactic nucleus.





#### Tidal Disruption Event of A Gas Cloud

• A gas cloud ("G2 Cloud") approaching Milky Way's massive BH discovered in 2011. Pericentric approach in 2013.



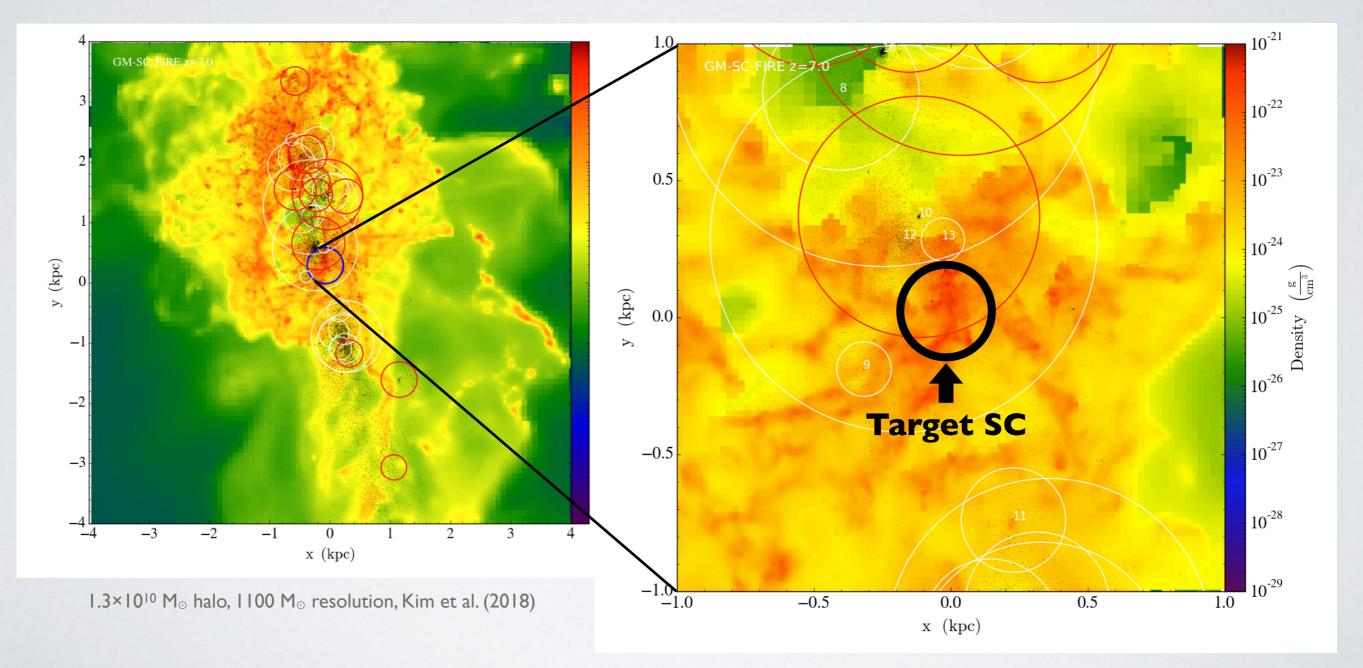
#### Star Cluster Formation

• In the bottom-up structure formation scenario in which CDM produces small-scale powers, small structures form first.



#### Merger-driven Globular Cluster Formation

• Realistic descriptions of interstellar medium (e.g., Hopkins et al.) are keys to describe SC formation in high-z merging proto-galaxies.



2 kpc width, density projection, centered on target SC

# Early Numerical Experiments: Holmberg

 Used 37 lightbulbs to represent a "nebula", and a photocell to measure simulated gravitational force (1941).

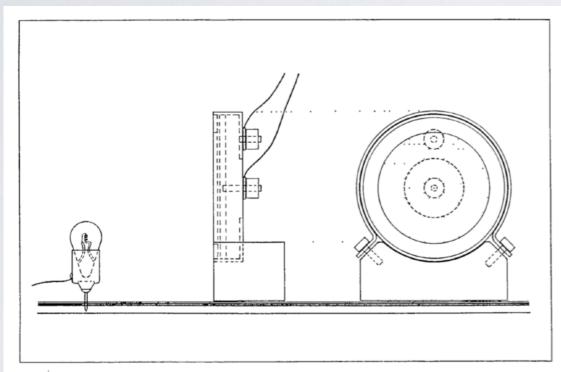


Fig. 1.—Cross-section of light-bulb and photocell (half-size)

Holmberg (1941)



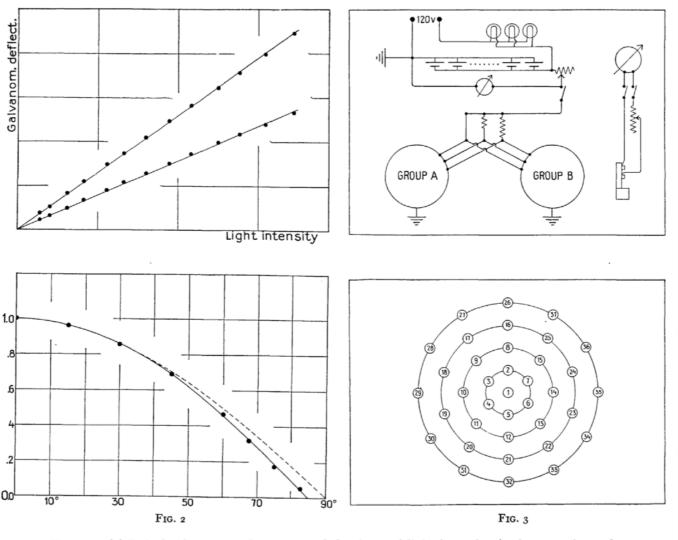


Fig. 2.—(a) Relation between galvanometer deflection and light-intensity (resistance of o and 10,000 ohms). (b) Relation between galvanometer deflection and angle of incidence of light (dotted line = theoretical cosine law).

Fig. 3.—(a) Coupling scheme. (b) Arrangement of the 37 light-bulbs in groups A and B

Holmberg (1908-2000)

# Early Numerical Experiments: Holmberg

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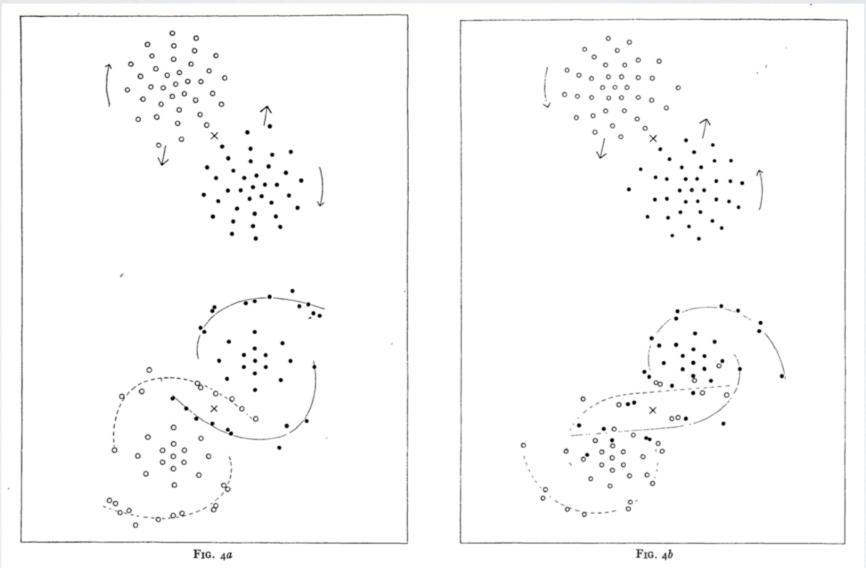


Fig. 4a.—Tidal deformations corresponding to parabolic motions, clockwise rotations, and a distance of closest approach equal to the diameters of the nebulae. The spiral arms point in the direction of the rotation.

Fig. 4b.—Same as above, with the exception of counterclockwise rotations. The spiral arms point in the direction opposite to the rotation.

#### Early Experiments: Toomre & Toomre

• Showed that bridges and tails in peculiar/multiple galaxies are tidal relics of close encounters.

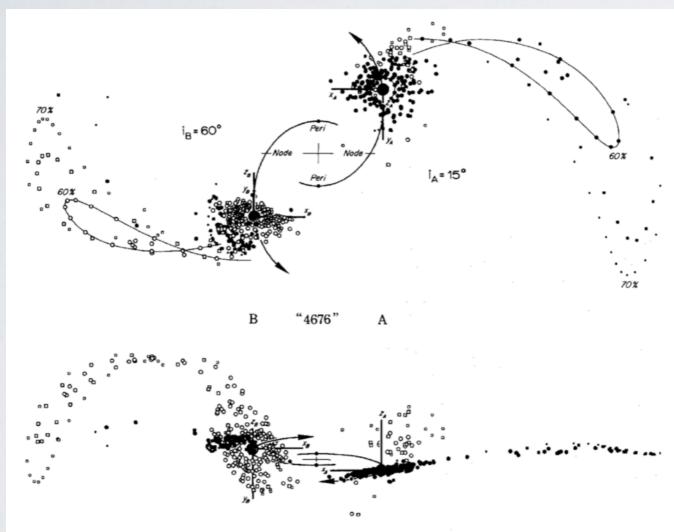


Fig. 22.—Model of NGC 4676. In this reconstruction, two equal disks of radius  $0.7R_{\rm min}$  experienced an e=0.6 elliptic encounter, having begun flat and circular at the time t=-16.4 of the last apocenter. As viewed from either disk, the adopted node-to-peri angles  $\omega_A=\omega_B=-90^\circ$  were identical, but the inclinations differed considerably:  $i_A=15^\circ$ ,  $i_B=60^\circ$ . The resulting composite object at t=6.086 (cf. fig. 18) is shown projected onto the orbit plane in the upper diagram. It is viewed nearly edge-on to the same—from  $\lambda_A=180^\circ$ ,  $\beta_A=85^\circ$  or  $\lambda_B=0^\circ$ ,  $\beta_B=160^\circ$ —in the lower diagram meant to simulate our actual view of that pair of galaxies. The filled and open symbols distinguish particles originally from disks A and B, respectively.



Toomre & Toomre (1972)

#### Early Experiments: Toomre & Toomre

• Showed that bridges and tails in peculiar/multiple galaxies are tidal relics of close encounters.

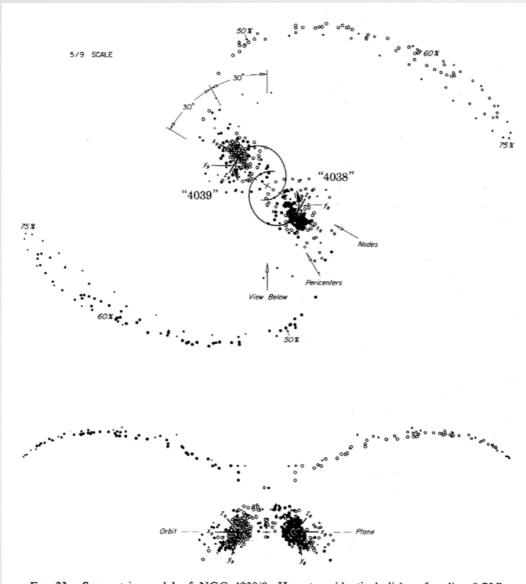
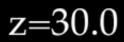
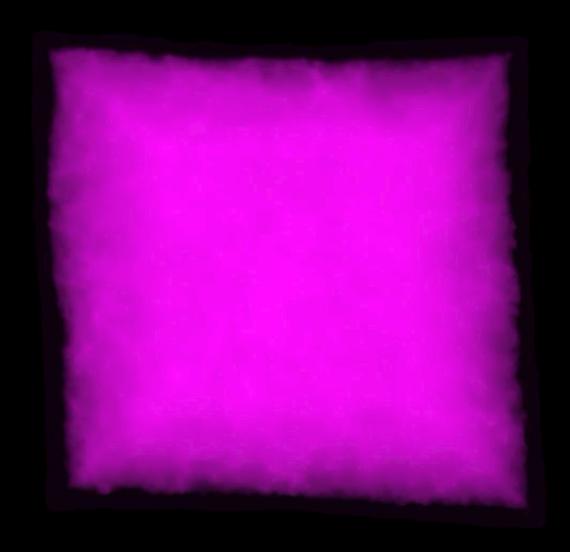


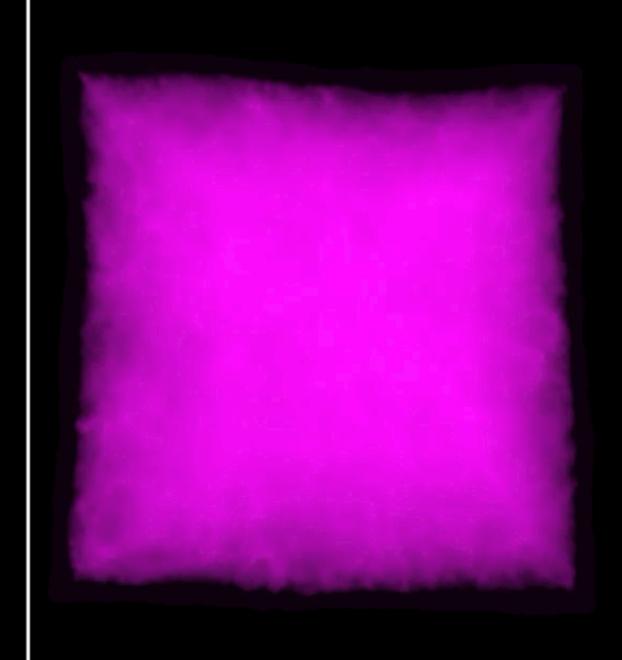
Fig. 23.—Symmetric model of NGC 4038/9. Here two identical disks of radius  $0.75R_{\rm min}$  suffered an  $e \approx 0.5$  encounter with orbit angles  $i_8 = i_9 = 60^\circ$  and  $\omega_8 = \omega_9 = -30^\circ$  that appeared the same to both. The above all-inclusive views of the debris and remnants of these disks have been drawn exactly normal and edge-on to the orbit plane; the latter viewing direction is itself 30° from the line connecting the two pericenters. The viewing time is t = 15, or slightly past apocenter. The filled and open symbols again disclose the original loyalties of the various test particles.



Toomre & Toomre (1972)

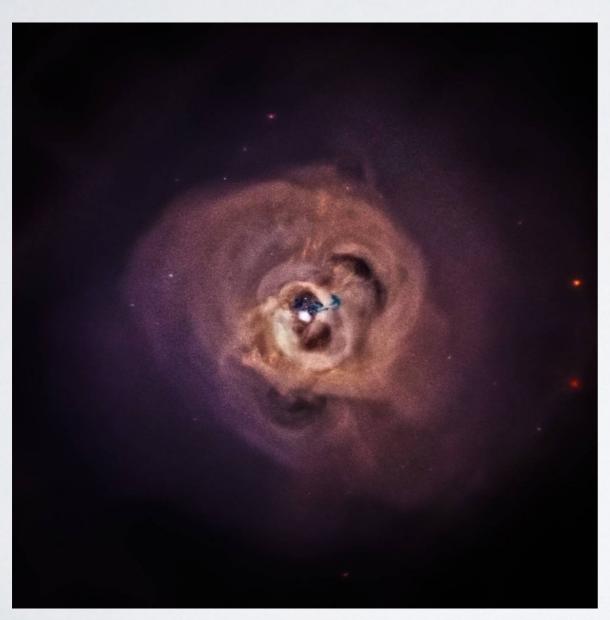




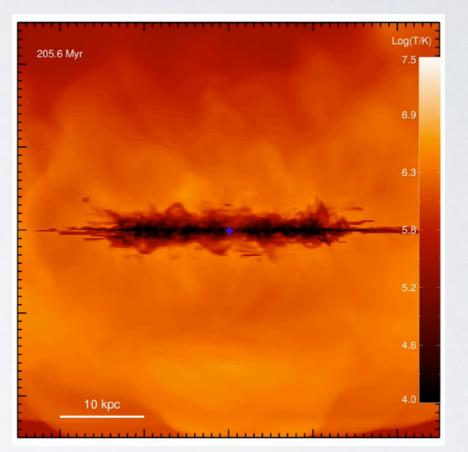


#### Strong Jets From the Galactic Center

• Mechanical feedback creates lobes and bubbles in X-ray images.

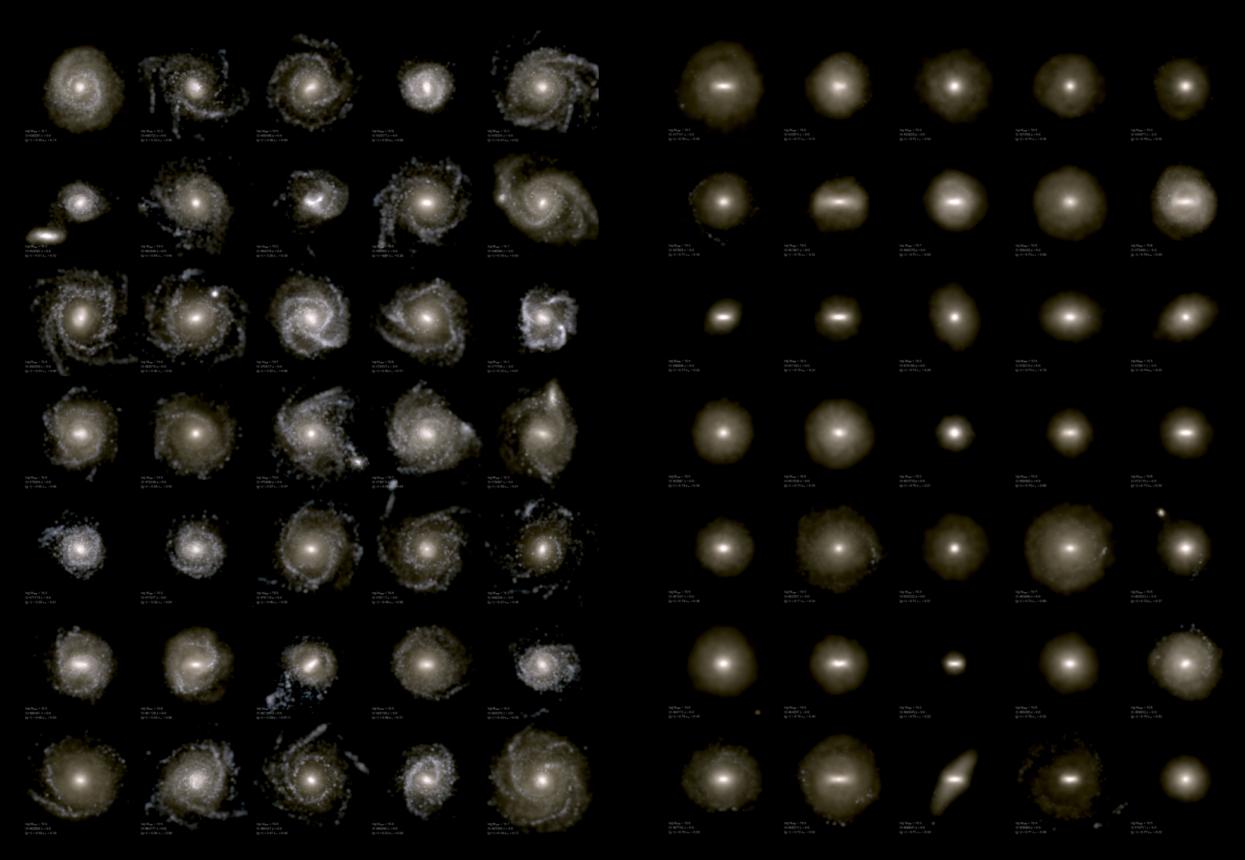


Per A Cluster, NASA/CXC/SAO



Gabor et al.

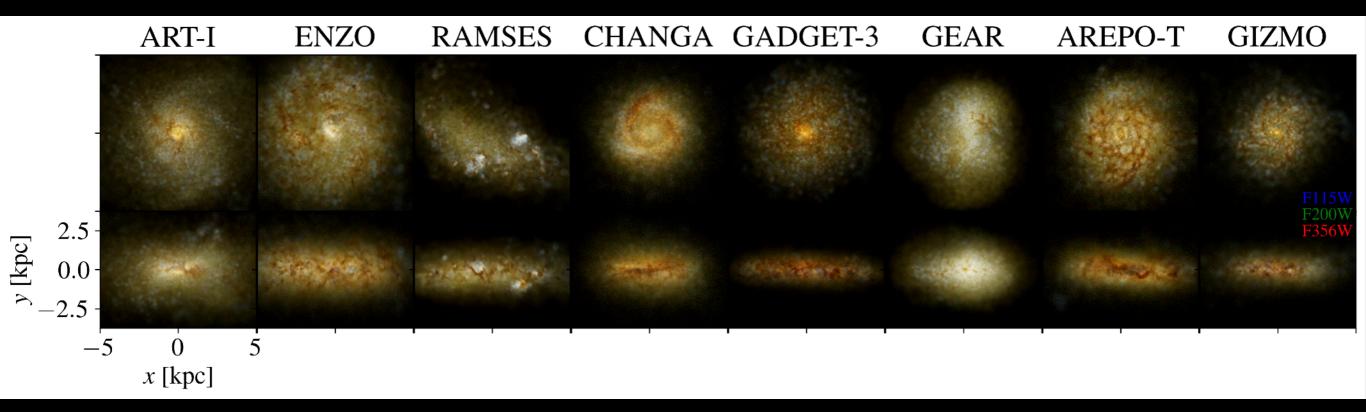
# Mock JWST Observations



Star-forming galaxies, Illustris-TNG Collaboration

Star formation quenched galaxies, Illustris-TNG Collaboration

# Mock JWST Observations

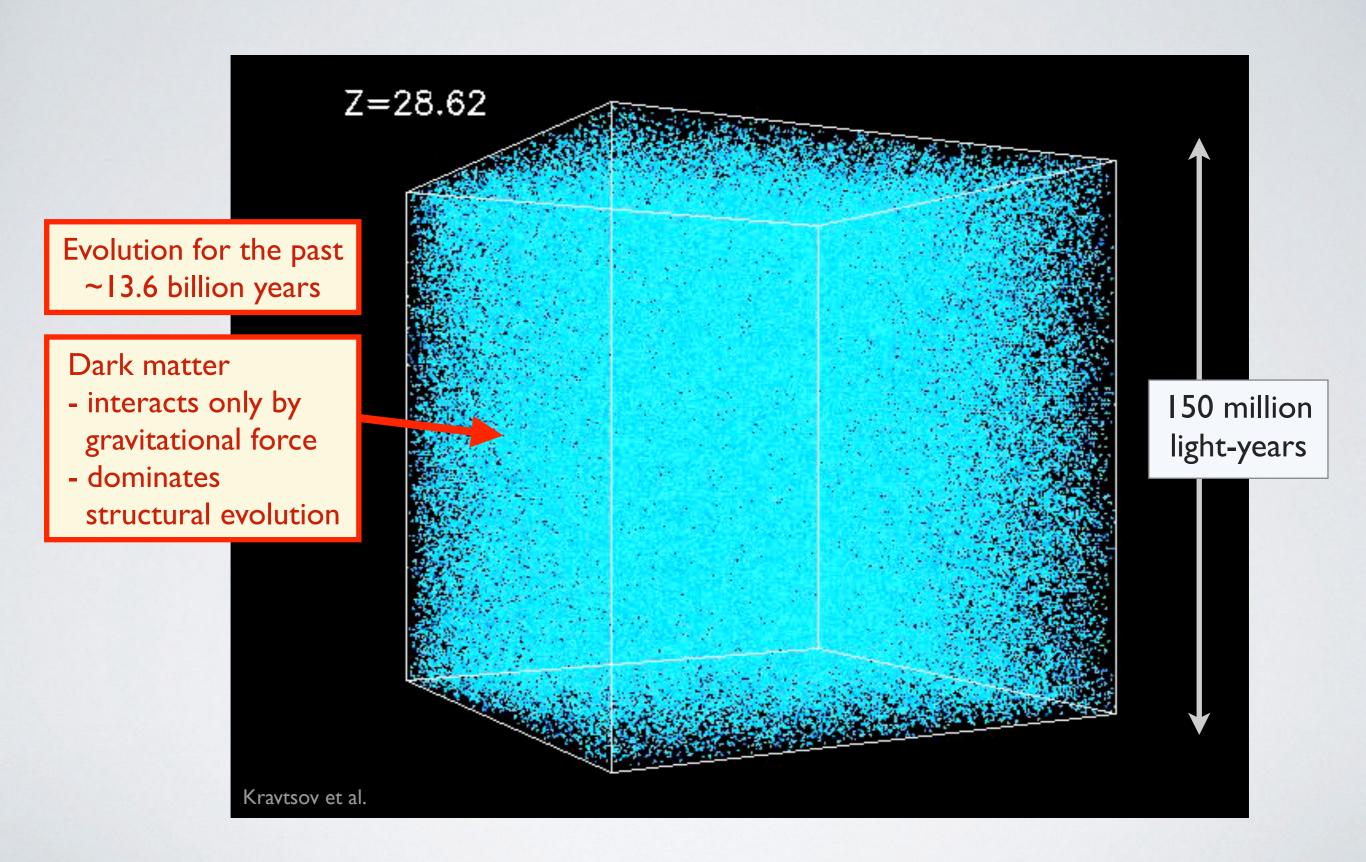


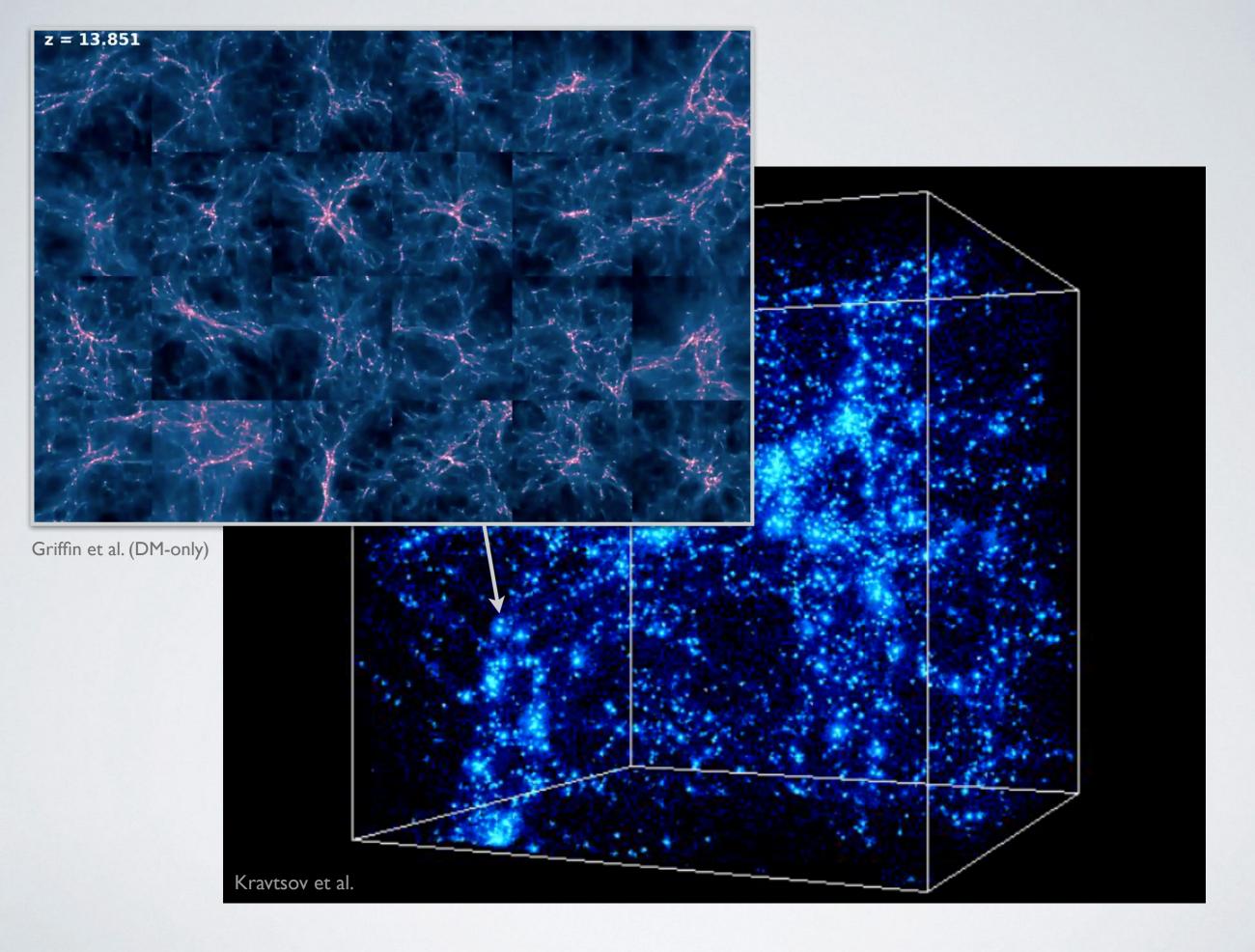
Jung et al. for the AGORA Collaboration (2025)

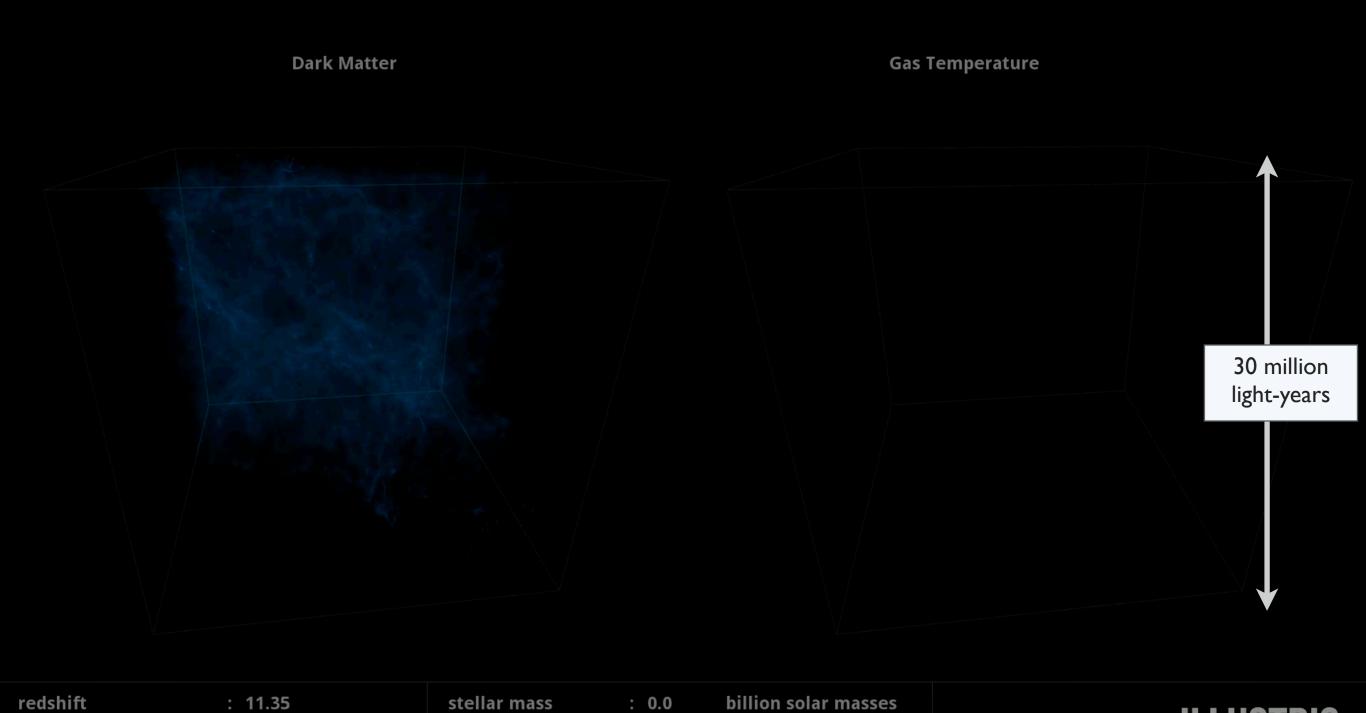
# Large-Scale Structure (LSS) of Universe



# Numerical Cosmology: Structure Formation





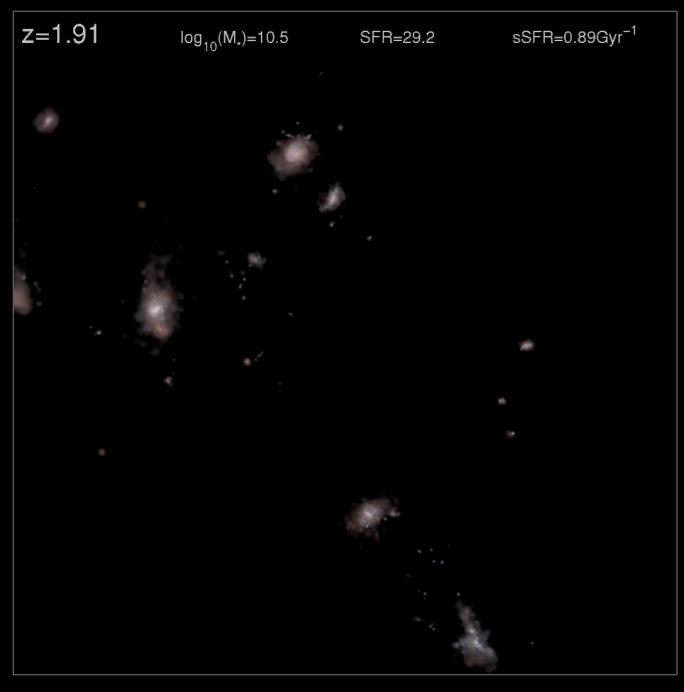


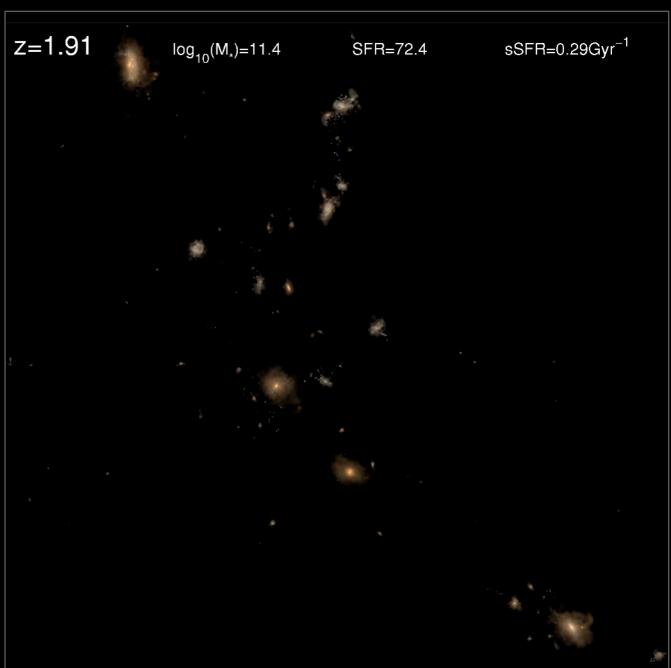
**ILLUSTRIS** 

DM density and gas temperature, 10 Mpc, Illustris Collaboration

Time since the Big Bang: 0.4 billion years

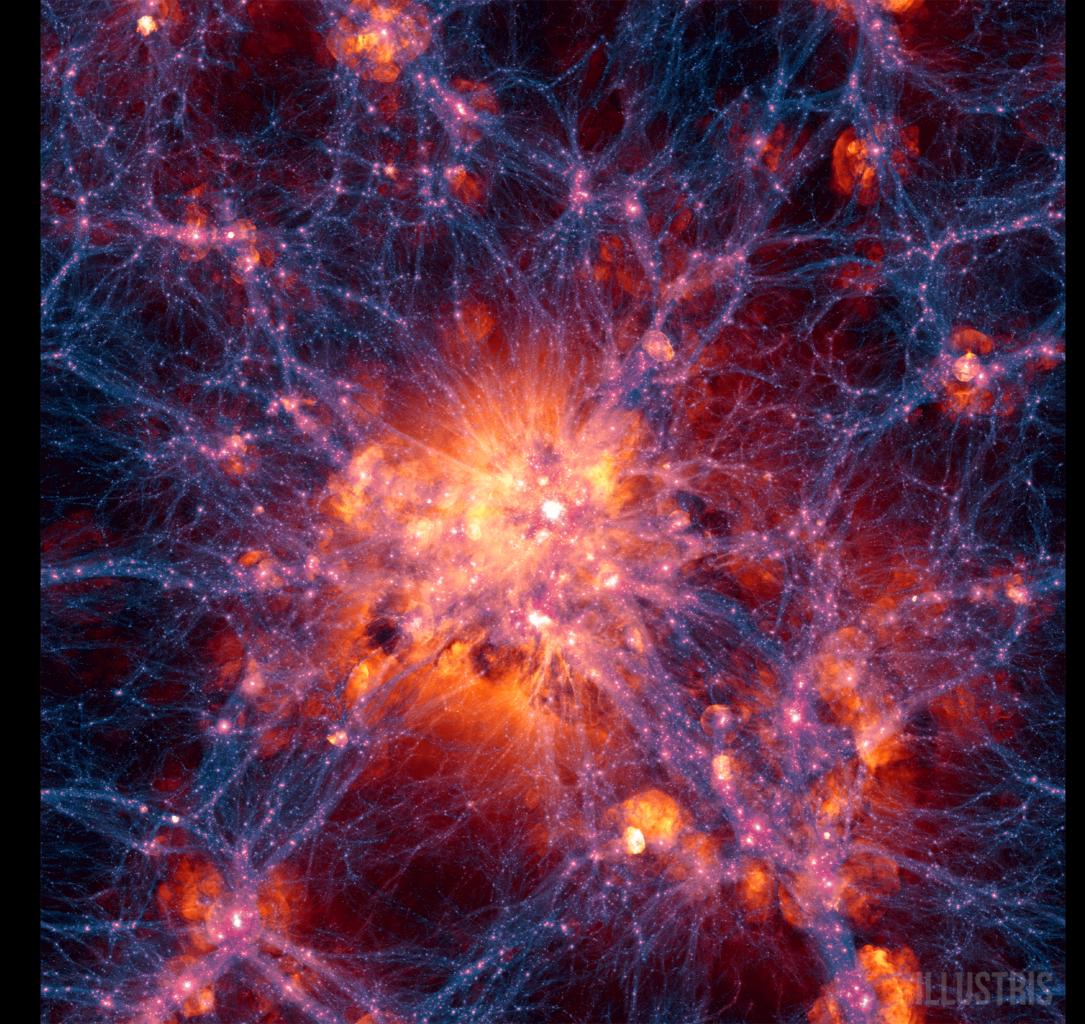
# Individual Galaxy Evolution History

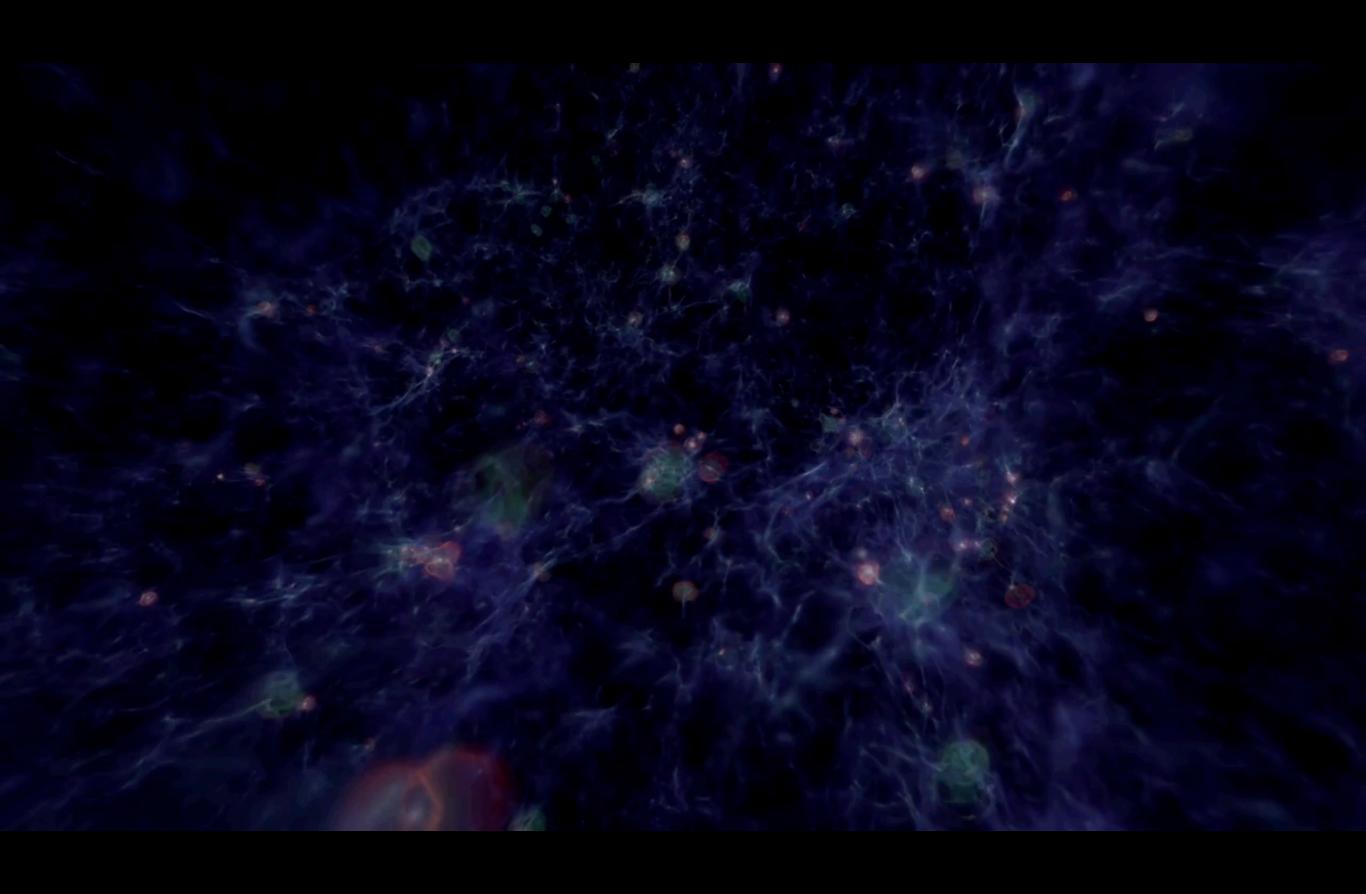




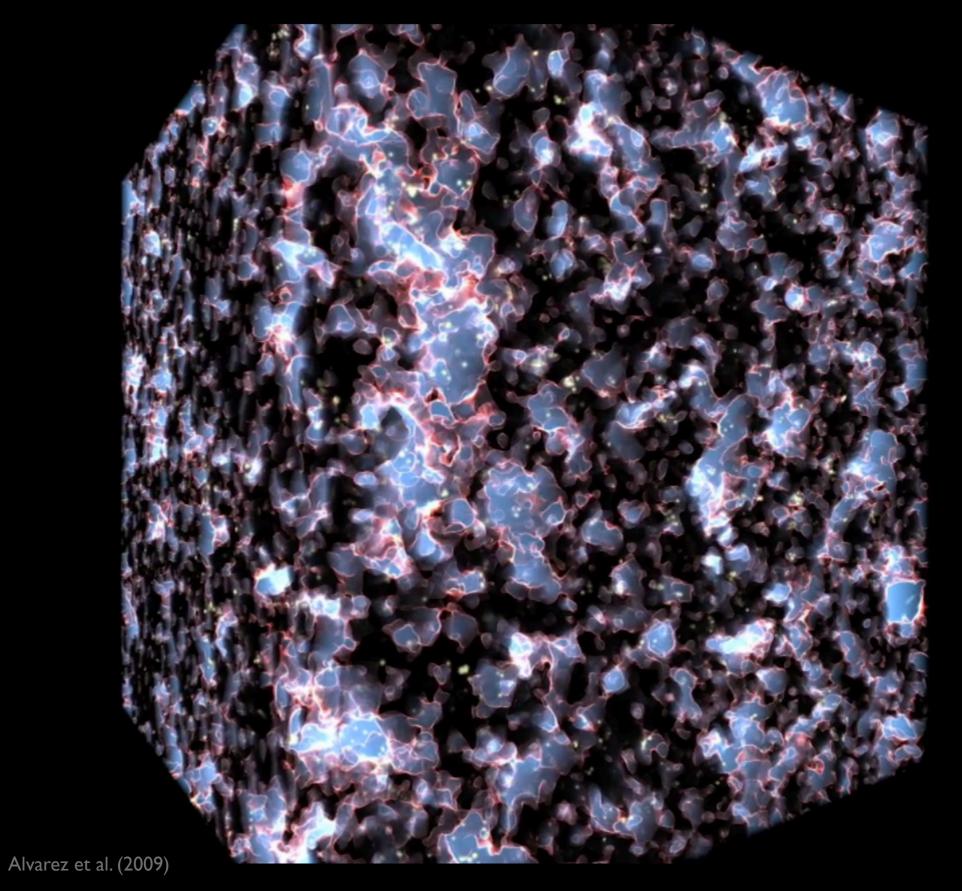
Star-forming late-type galaxy, Illustris-TNG Collaboration

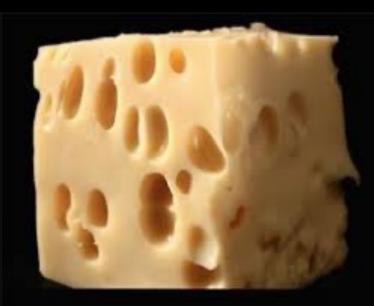
Star formation quenched, early-type galaxy, Illustris-TNG Collaboration



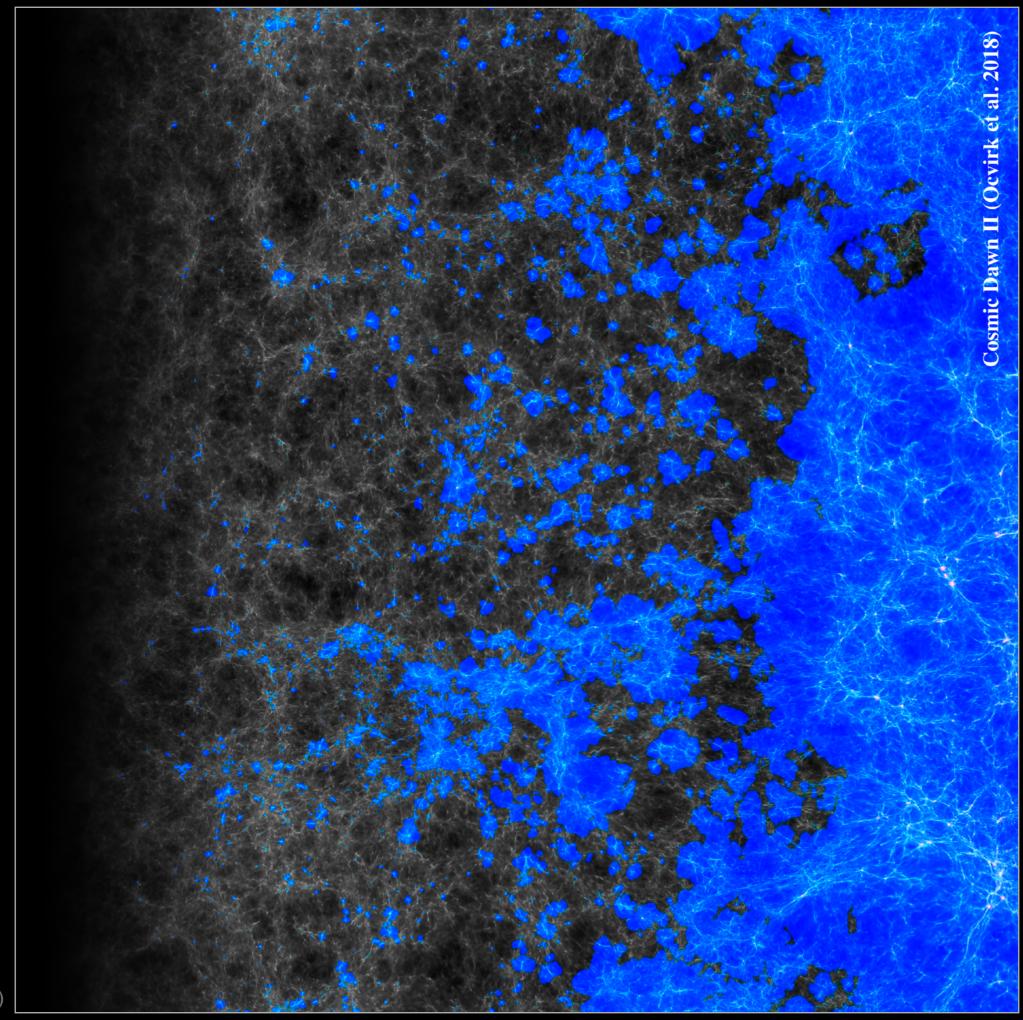


# "Swiss Cheese" Reionization



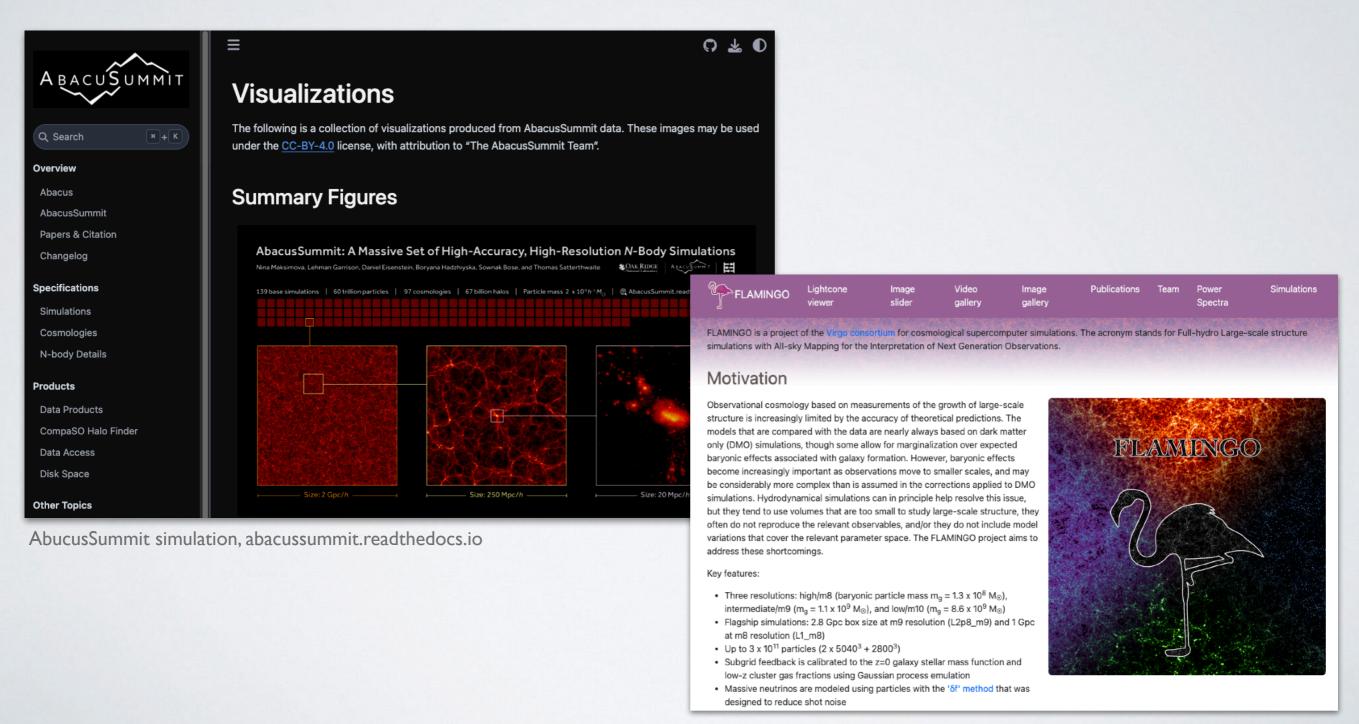


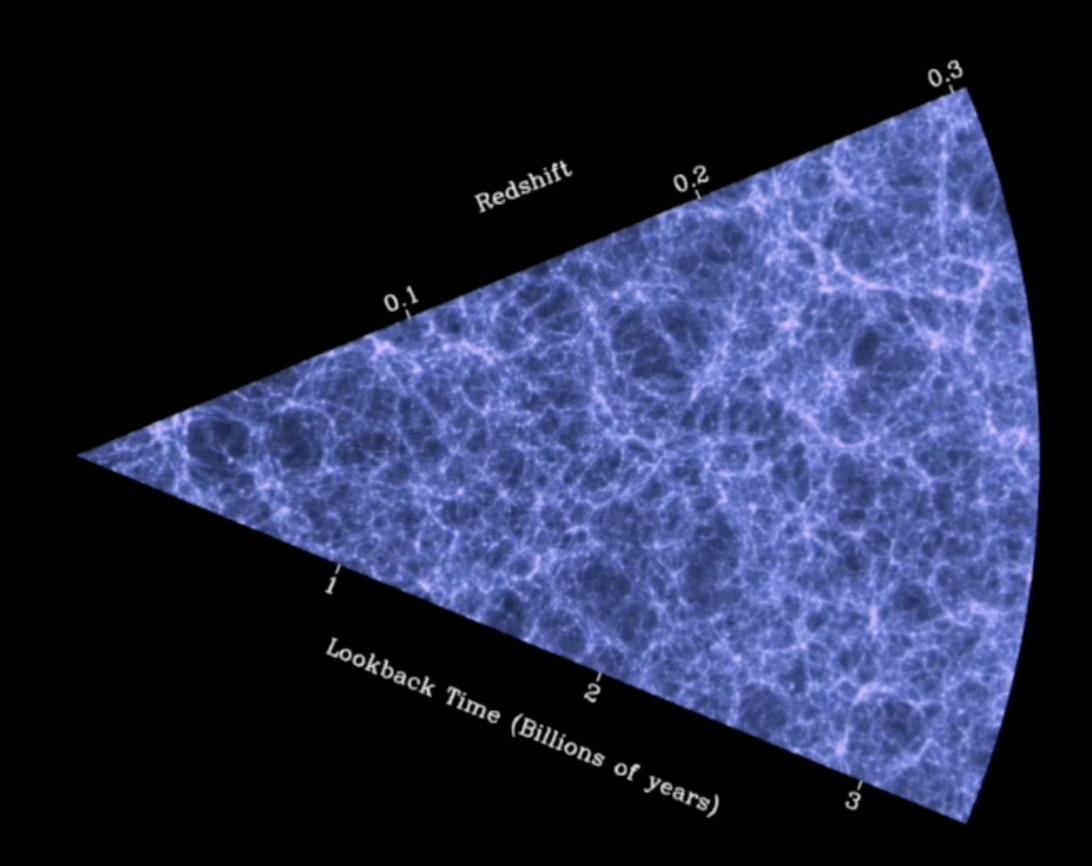




# Generating "Large" Universes

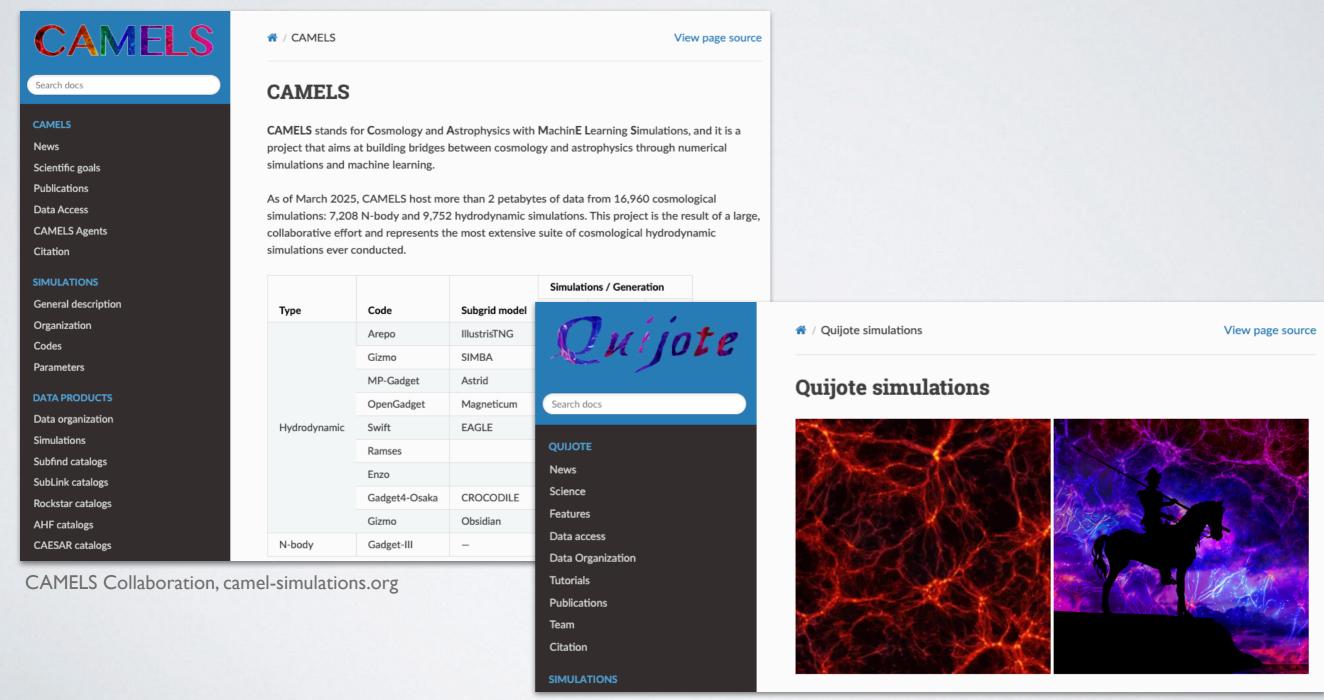
• Large-box simulations try to cover the volumes comparable to the "observable" universe.



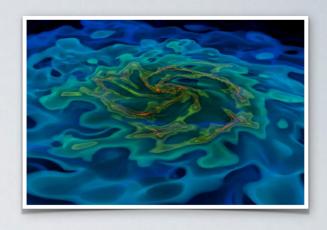


# Generating "Many" Different Universes

 Can be used to train a machine that infers physics parameters or cosmological parameters of our universe.

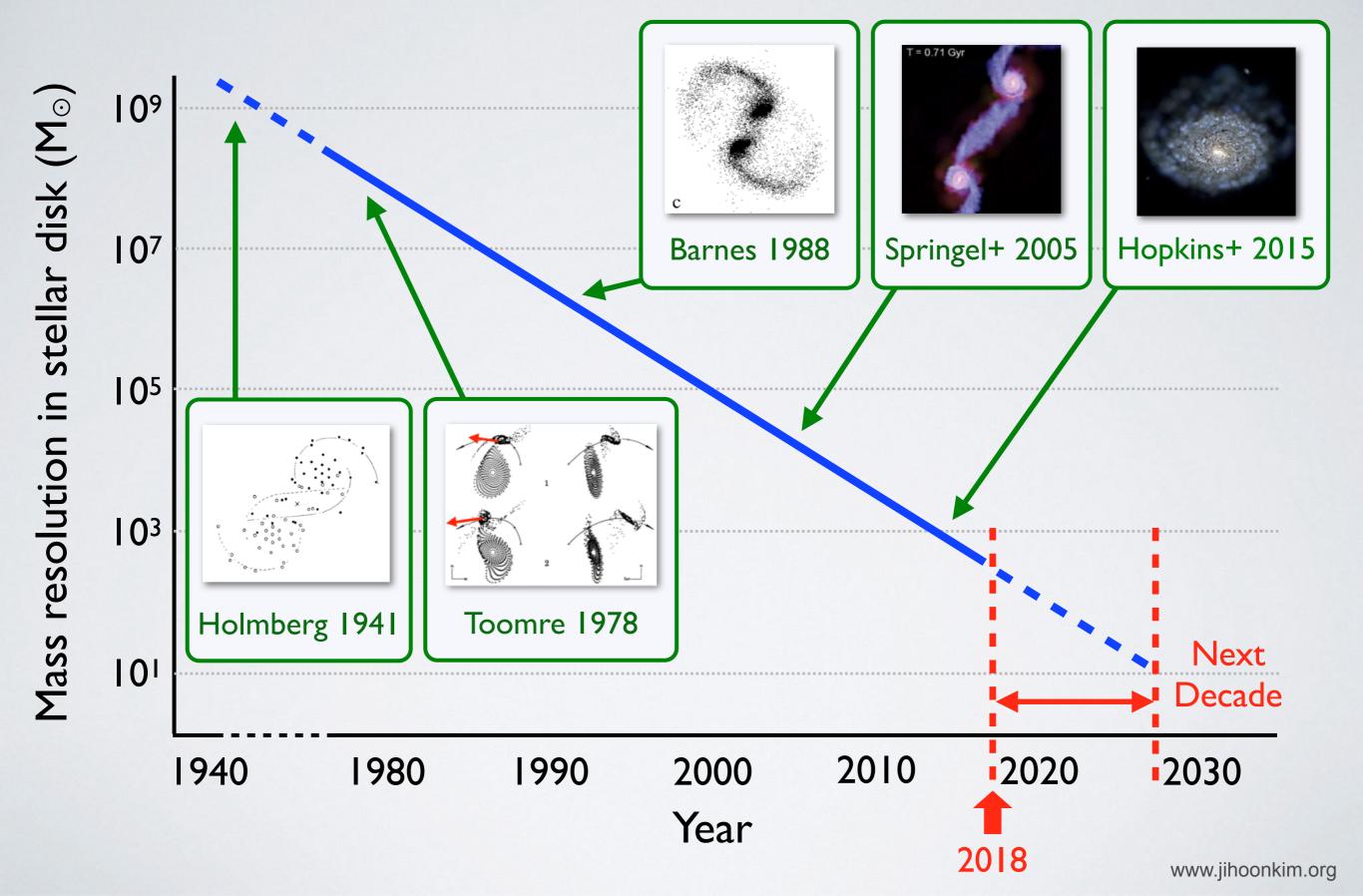


Quijote Collaboration, quijote-simulations.readthedocs.io



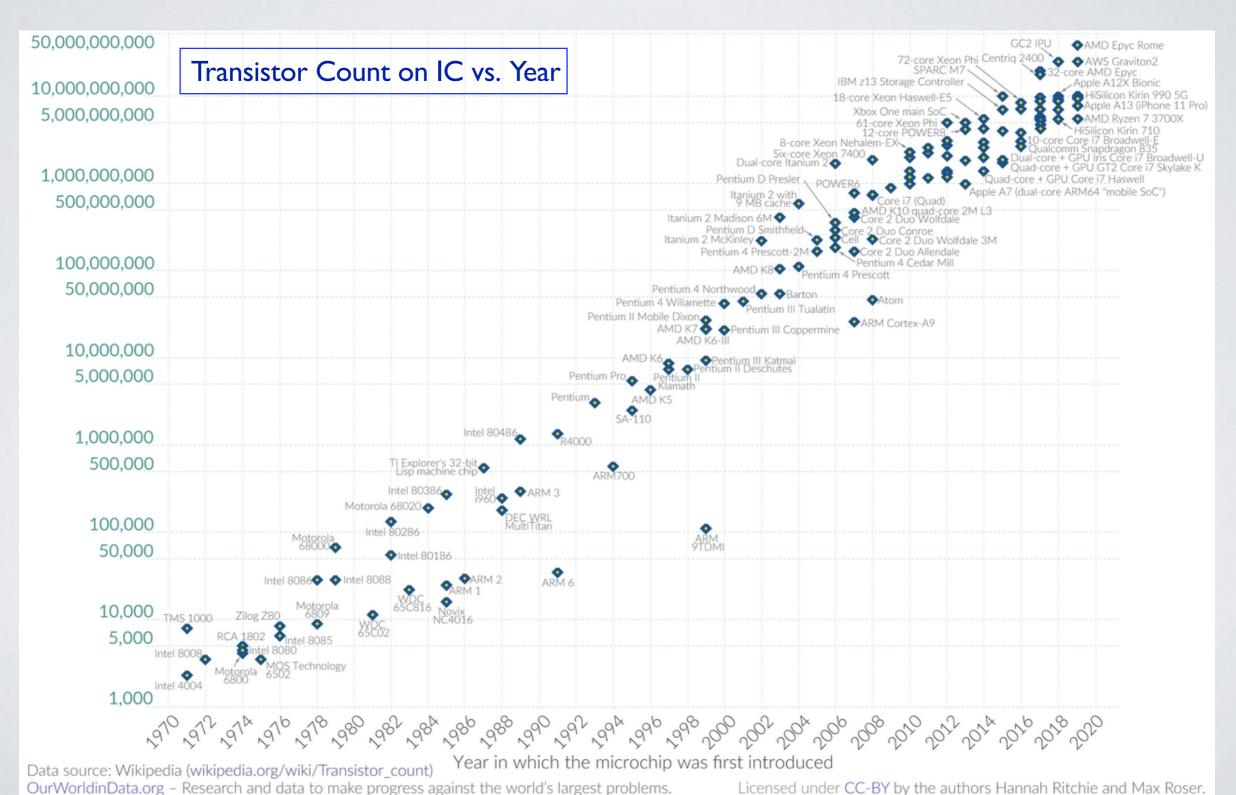
# Computational Astrophysics: Methodology

# Computational Cosmology: Resolution



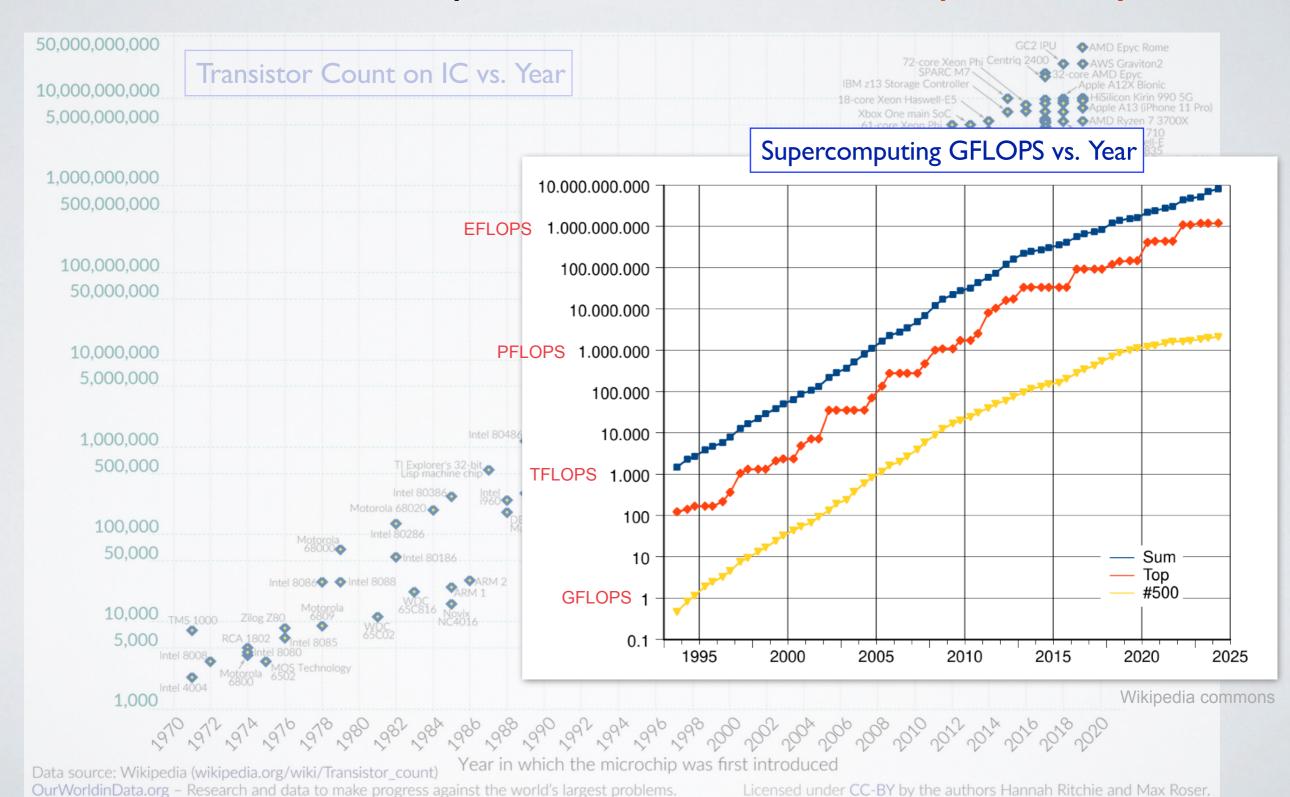
# Computational Cosmology: Tools

Tools of numerical experiments have evolved exponentially.

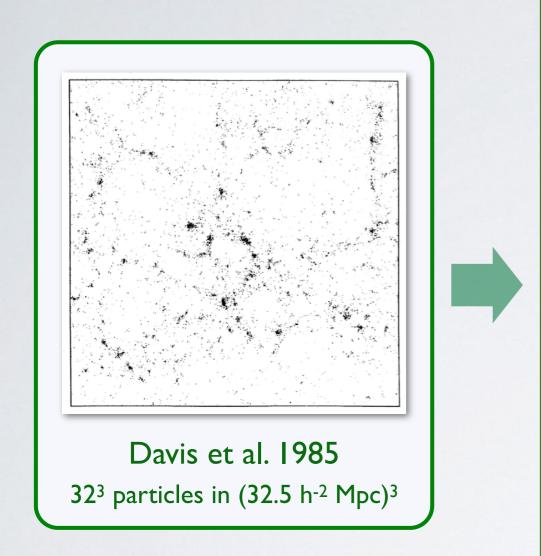


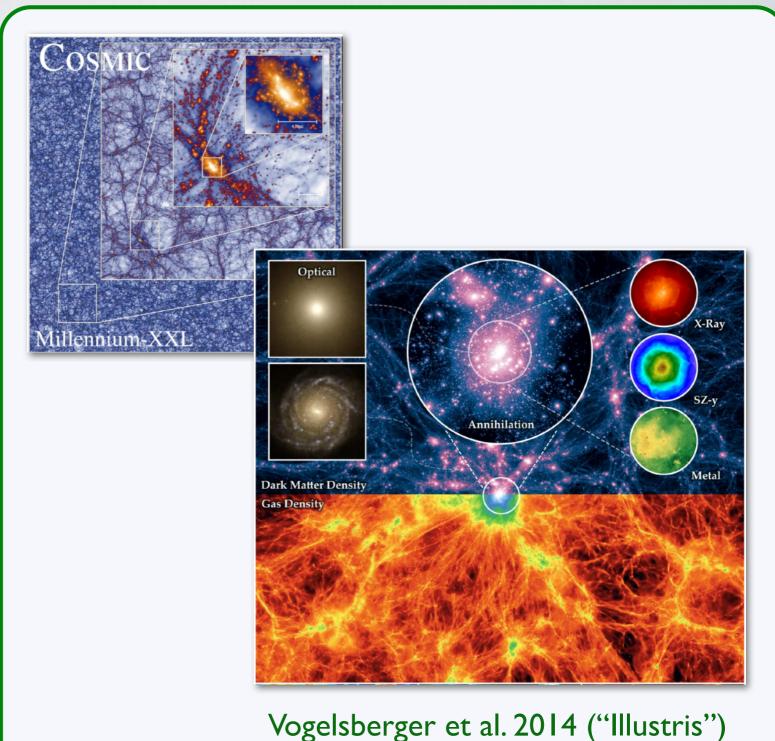
# Computational Cosmology: Tools

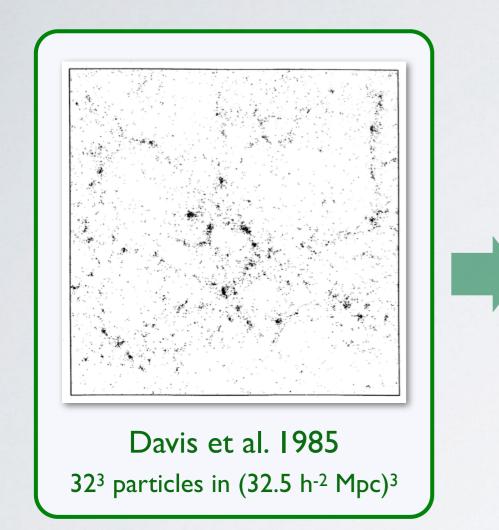
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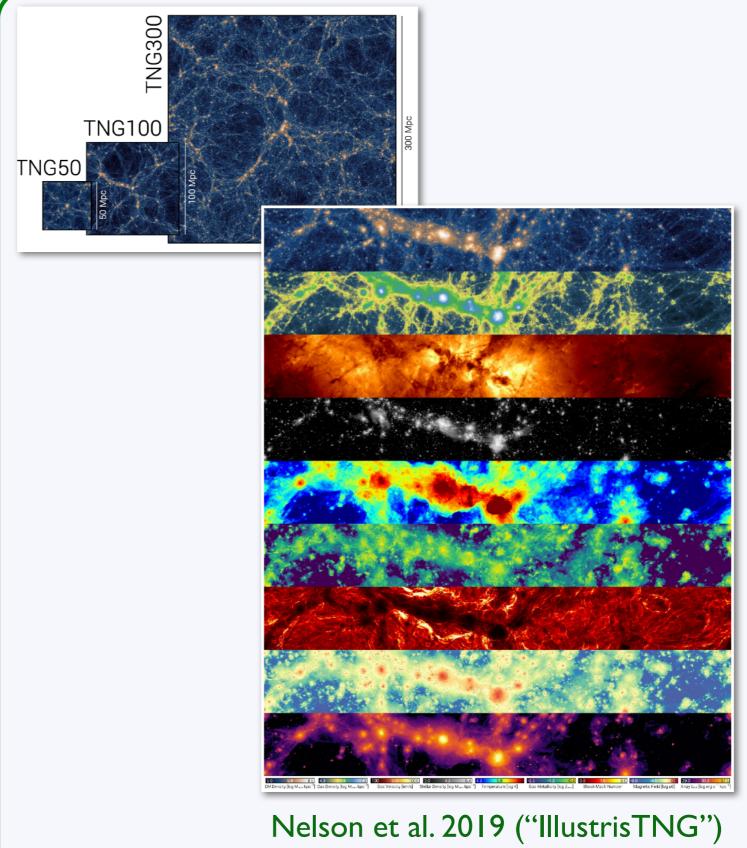


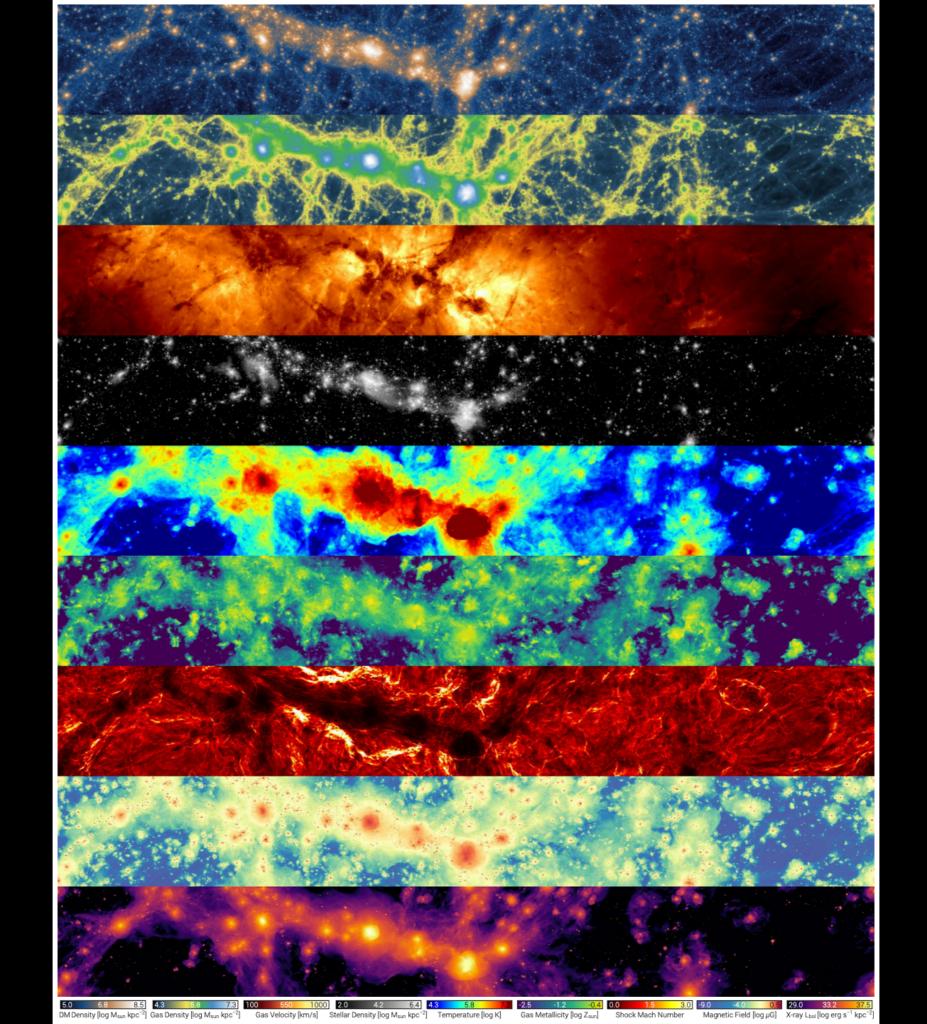
# Computational Cosmology: Resolution





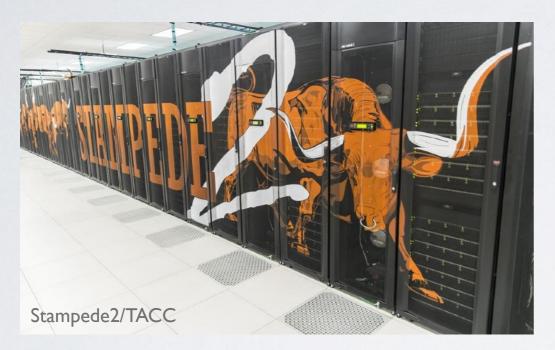






# Supercomputing Facilities

• Supercomputing resources provided by e.g., national labs.







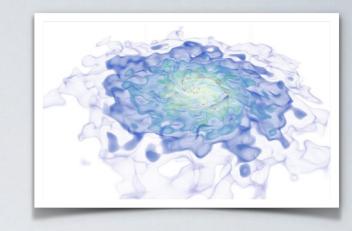


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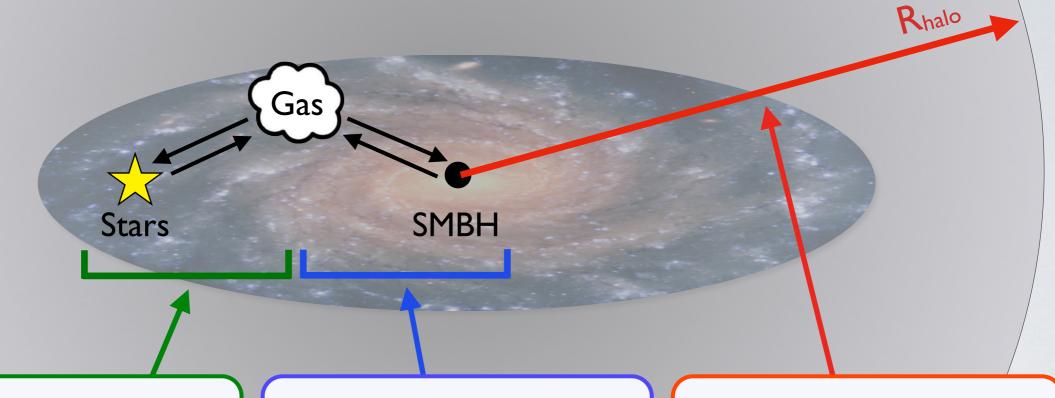


Nurion(5th gen)/KISTI



# Components of Simulations

## Multi-scale, Nonlinear Interactions



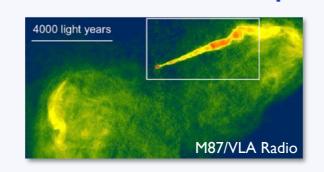
Stars or Molecular Clouds Formation & Feedback

 $R_{GMC} \sim 10 pc$ 



Massive Black Hole Accretion & Feedback

 $R_{Bondi} \sim pc$  $R_{Schw.} \sim 10^{-5} pc$ 



(Inter-)Galactic

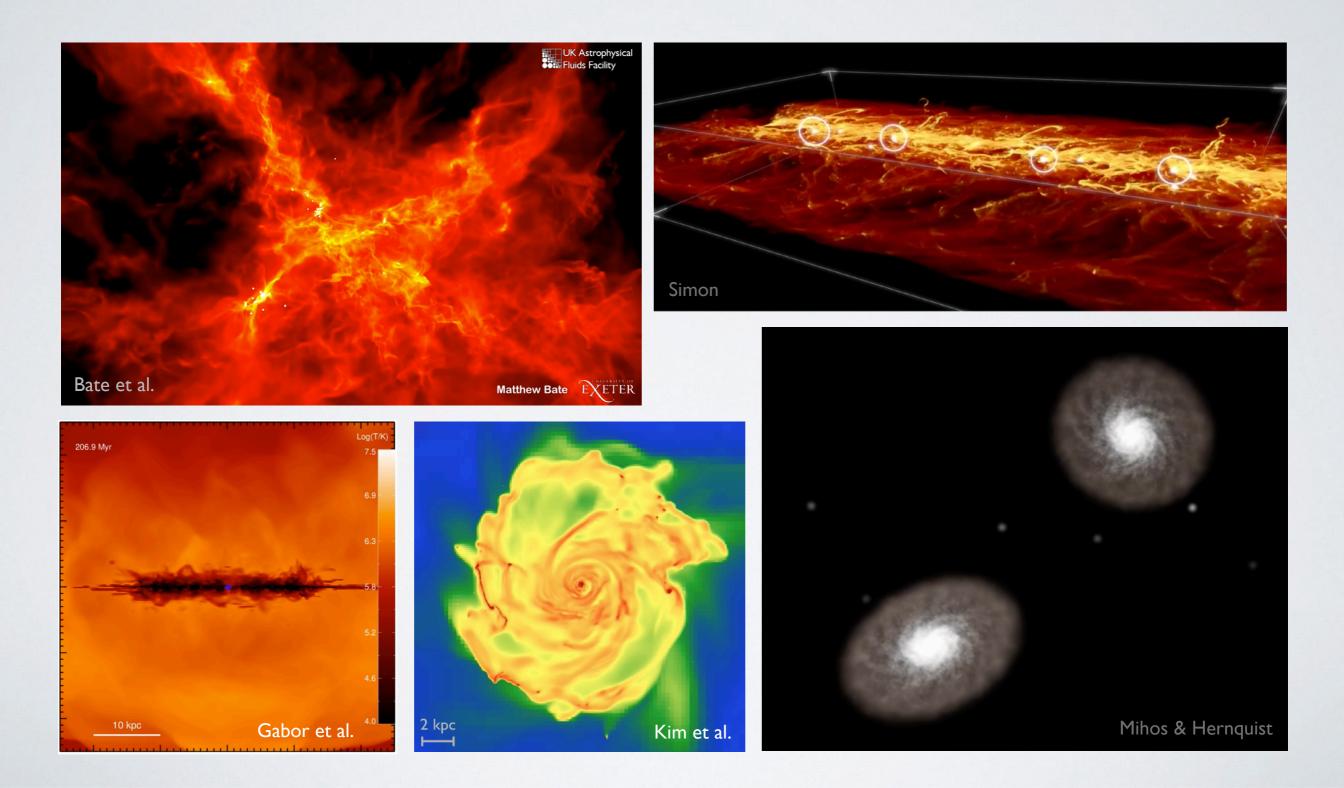
Dynamics & Interaction

 $R_{halo} \sim 100 \text{ kpc}$ 



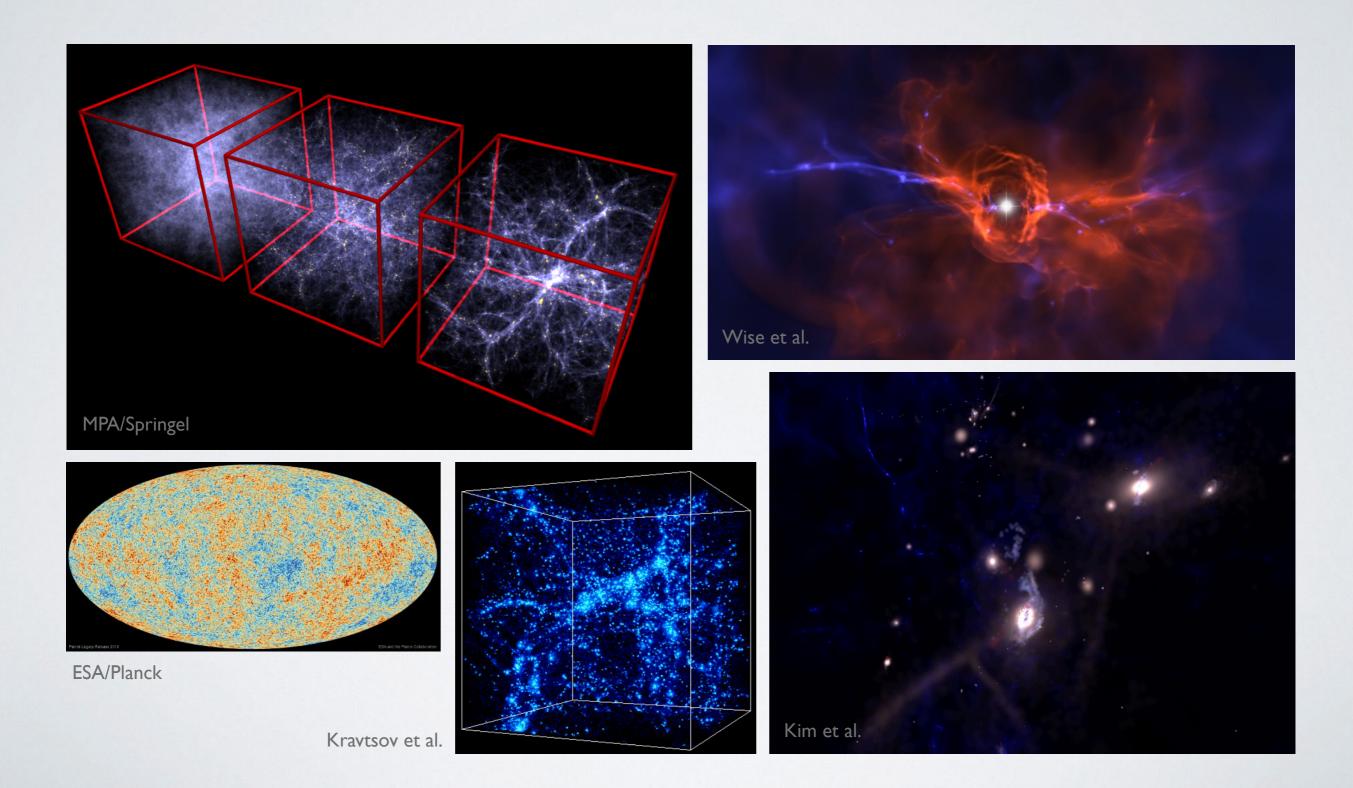
### "Idealized" Initial Conditions

• Start from physically-motivated, yet idealized, often isolated ICs.



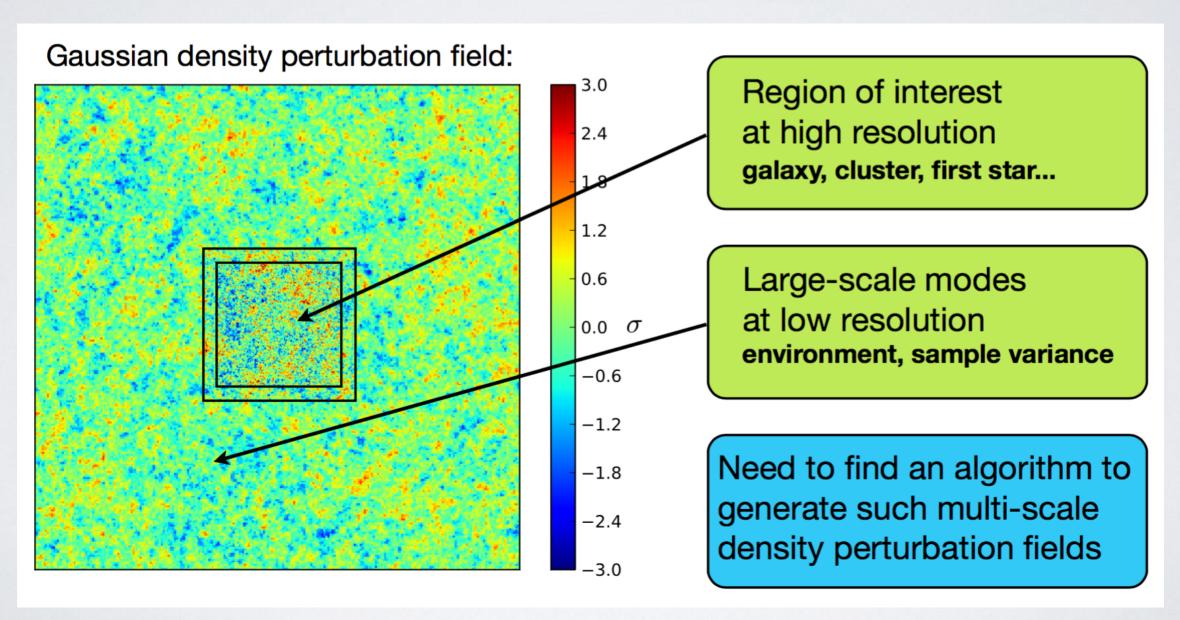
# "Cosmological" Initial Conditions

• Start from perturbed density distribution motivated by CMB.



# "Zoom-in" Cosmological ICs

- Strategy to best utilize your resources on regions of interest.
- Nested zoom-in IC to capture both large- and small-scale power.

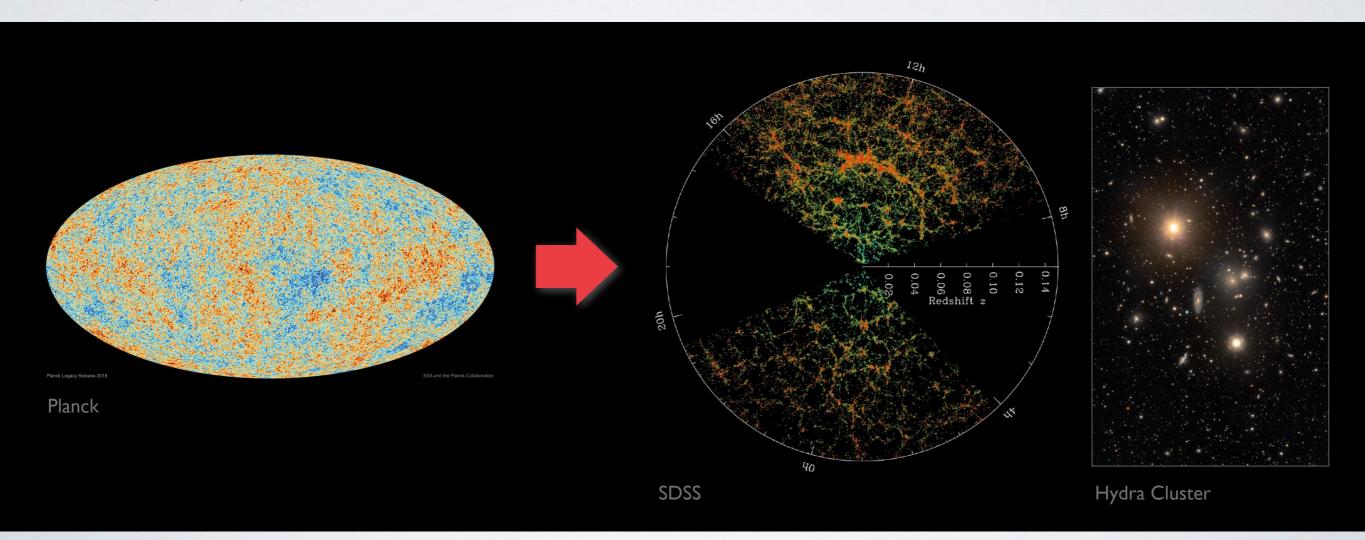


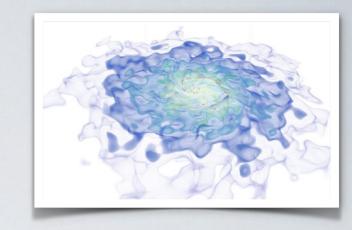
## Linear and Nonlinear Growth

- If  $|\delta \rho/\bar{\rho}| = |\delta(x)| \ll 1$ ,  $\delta(x)$ 's evolves linearly (right after CMB).
- The Universe at ~Mpc scale has entered the nonlinear regime.

 $\langle (\delta \rho/\bar{\rho})^2 \rangle^{0.5} \sim 10^{-5}$ 

 $\langle (\delta \rho/\bar{\rho})^2 \rangle^{0.5} \gg 1$ 





# Physics Processes in Simulations

superinteractive stellar radiation star massive magnetic gas stellar galactic cooling formation feedback fields fields black medium nuclei holes kinetic/ kinetic/ initial stellar numerical ideal MHD/ effective thermal/ atomic/ thermal/ seeding/ mass ray tracing/ radiative/ cleaning molecular/ equation variety of function/ growth by Monte Carlo/ schemes/ metals/ of state/ quasar sources probabilistic accretion moment-

from stars.

supernovae

#### most important astrophysical processes

prescription/

merging

#### numerical discretization of matter components

#### **Collisionless Gravitational Dynamics**

multi-

phase

- N-body methods based on integral Poisson's equation (e.g. tree, fast multipole)
- N-body methods based on differential Poisson's equation (e.g. particle-mesh, multigrid)

sampling/

enrichment

- N-body hybrid methods (e.g. TreePM)
- Beyond N-body methods (e.g. Lagrangian tesselation)





#### **Hydrodynamics**

mode/

radio

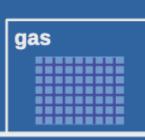
mode

Lagrangian methods (e.g. smoothed particle hydrodynamics)

constrained

transport

- **Eulerian methods** (e.g. adaptive-mesh-refinement)
- **Arbitrary Lagrangian-Eulerian methods** (e.g. moving mesh)
- Mesh-free / mesh-based



cosmic

rays

production/

heating/

anisotropic

diffusion/

streaming

**Volume** 

tabulated/

network

sample of galaxies

#### generating initial conditions

linear perturbation theory

**Zoom** 



based

individual galaxy

#### **Gravity**

- Newtonian gravity in an expanding background
- modified gravity as dark matter alternative
- modified gravity as dark energy alternative

#### **Dark Matter**

- cold dark matter
- warm dark matter
- self-interacting dark matter
- fuzzy dark matter

#### **Dark Energy**

- cosmological constant
- dynamical dark energy
- inhomogeneous dark energy
- coupled dark energy

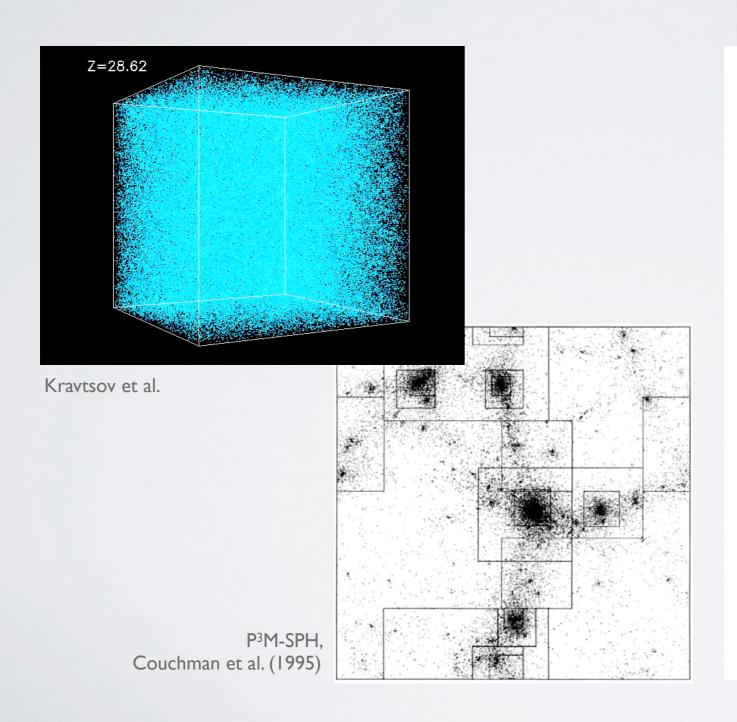
#### **Initial Conditions**

- inflation generated initial perturbations on top of homogeneous Friedmann model

#### cosmological framework

# Gravity: Poisson's Equation

• Gravity is the main driver for structure formation in Universe.



Poisson's equation for gravity:

$$\nabla^2 \Phi = 4\pi G \rho$$

Its solution has the form:

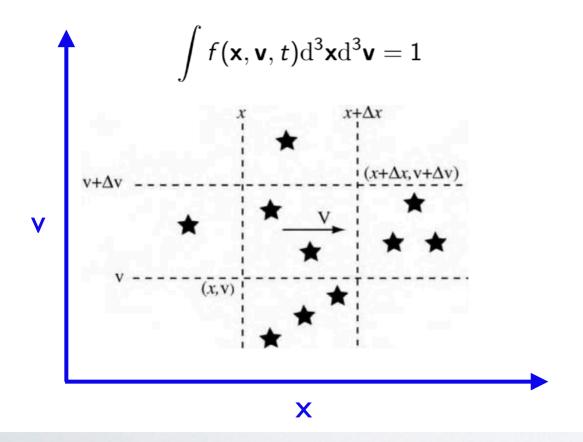
$$egin{aligned} arPhi(\mathbf{x}) &= \int g(\mathbf{x}-\mathbf{x}')\, oldsymbol{
ho}(\mathbf{x}')\, \mathrm{d}\mathbf{x}', \ & ext{with} \ \ g(\mathbf{x}) &= -rac{G}{|\mathbf{x}|} \end{aligned}$$

The convolution in x-space is simply a multiplication in k-space:

$$\hat{\boldsymbol{\Phi}}(\mathbf{k}) = \hat{g}(\mathbf{k}) \cdot \hat{\boldsymbol{\rho}}(\mathbf{k})$$

# Collisionless Boltzmann Equation

- Let us consider a stellar/galactic system of a large number of identical bodies moving in a smooth potential  $\Phi(\mathbf{x}, t)$ .
- Galactic dynamics is all about deriving the probability  $f(\mathbf{x}, \mathbf{v}, \mathbf{t})$  of finding a star in a 6-dimensional phase space volume  $d^3\mathbf{x}d^3\mathbf{v}$ .



Then, 6-dim continuity equation: 
$$\frac{\partial f}{\partial t} + \sum_{i=1}^{6} \dot{w}_i \frac{\partial f}{\partial w_i} = 0$$

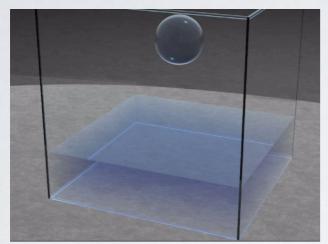
$$\frac{\partial f}{\partial t} + \mathbf{v} \cdot \nabla f - \nabla \Phi \cdot \frac{\partial f}{\partial \mathbf{v}} = 0$$



Euler equation in fluid dynamics:  $\frac{\partial \rho}{\partial t} + \boldsymbol{\nabla} \cdot (\rho \mathbf{v}) = 0$ 

# Fluid Dynamics: Euler Equations

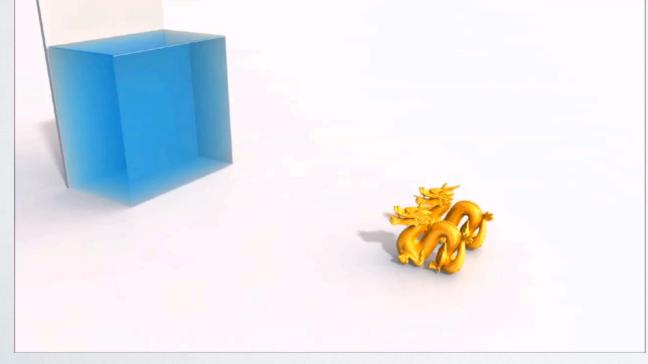
 At small scales, hydrodynamics of the baryonic components turns out to be important (e.g., star formation, supernovae).





Fedkiw et al.

Fedkiw et al.



Bender & Koschier

Three conservation equations:

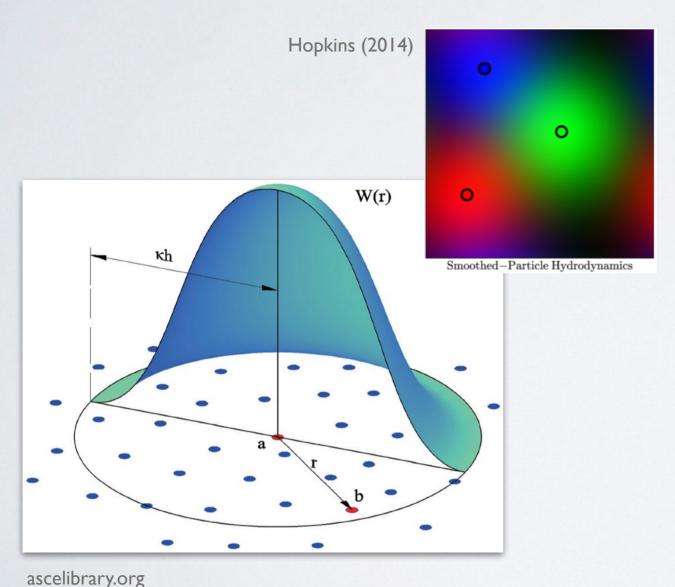
$$\frac{\partial \boldsymbol{\rho}}{\partial t} + \nabla(\boldsymbol{\rho} \mathbf{v}) = 0,$$

$$\frac{\partial}{\partial t}(\rho \mathbf{v}) + \nabla(\rho \mathbf{v} \mathbf{v}^T + P) = 0,$$
$$\frac{\partial}{\partial t}(\rho e) + \nabla[(\rho e + P)\mathbf{v}] = 0$$

$$\frac{\partial}{\partial t}(\rho e) + \nabla[(\rho e + P)\mathbf{v}] = 0$$

# Smoothed Particle Hydrodynamics (SPH)

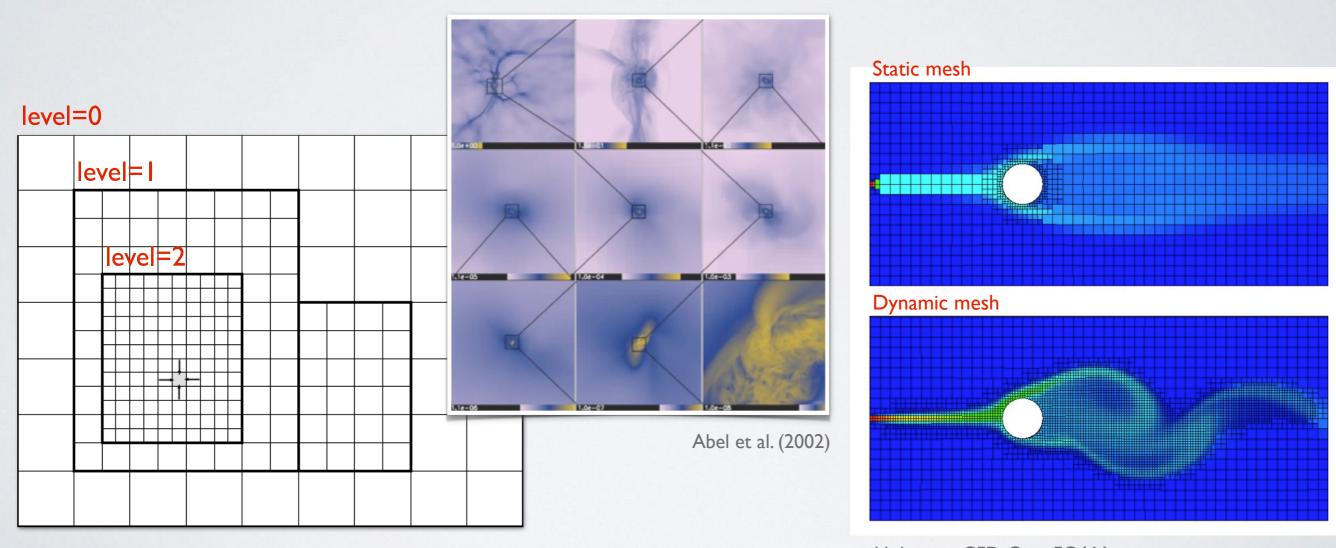
- Describe the continuum media with discrete particles.
  - originally for astrophysics (1970s), but now for many other fields with fluids



Bender & Koschier

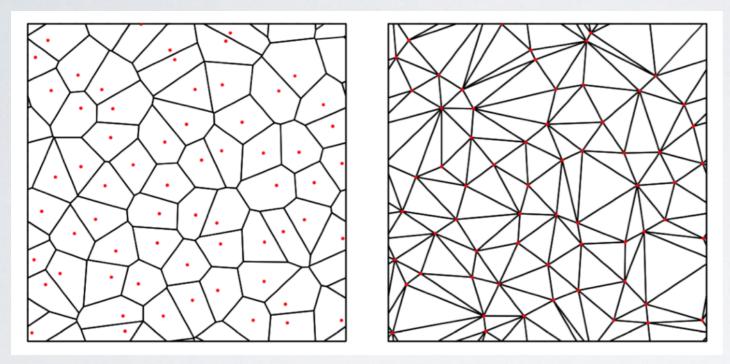
# Adaptive Mesh Refinement (AMR)

- Eulerian mesh adaptively focused on regions of high interests.
  - refines cells if found interesting; e.g., dense, collapsing, unstable, shocked

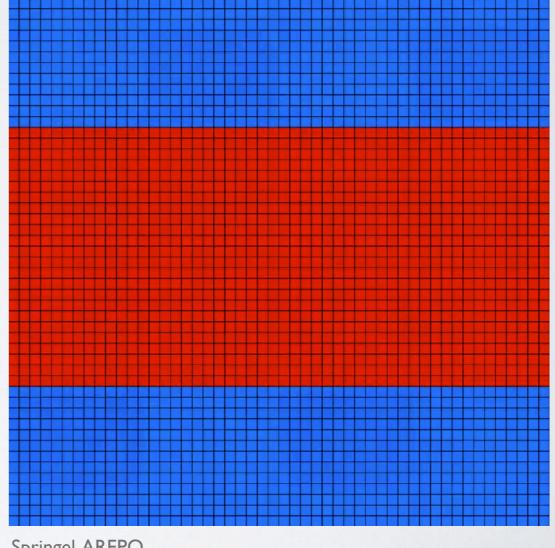


# Moving Mesh

 Based on a moving, unstructured mesh defined by the Voronoi tessellation of space using a set of discrete points.



Springel (2009), Voronoi & Delaunay tesselation



Springel, AREPO

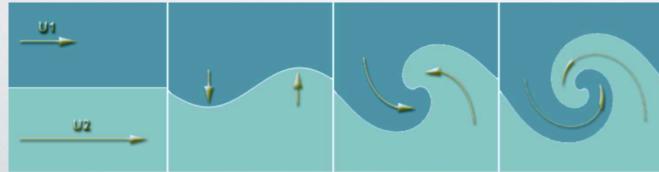
# Fluid Instability (I): Kelvin-Helmholtz

• If there is a velocity difference across the interface between two fluids (e.g., Jupiter's great red spot).



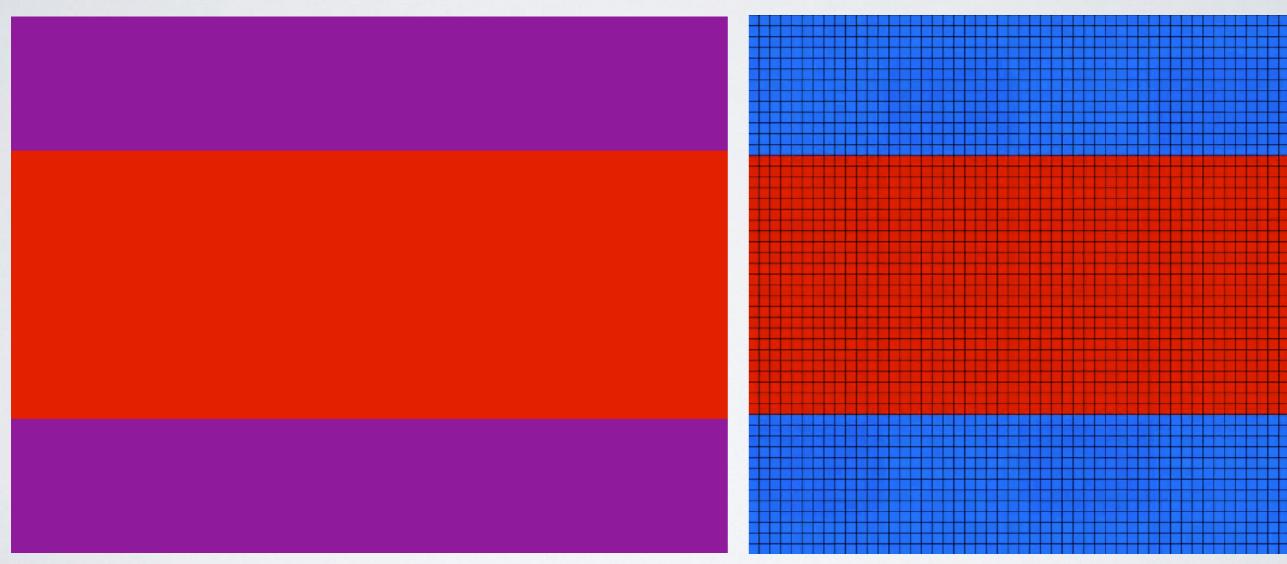


karlgaff.wordpress.com/kelvin-helmholtz-instability



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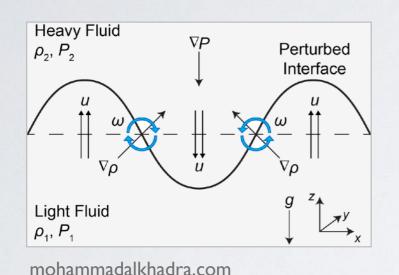


Springel, AREPO (moving mesh, seeded by random noise)

Springel, AREPO (one excited mode)

# Fluid Instability (II): Rayleigh-Taylor

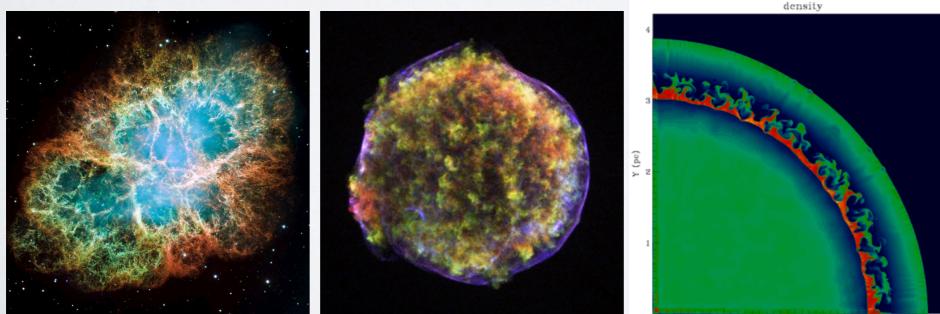
• If there is a density difference across the interface between two fluids (e.g., dense shell pushed by SN into lighter ISM).



Li & Li



Riordon, AIP



SN1054 (Crab), NASA/ESA/HST

SNI572 (Tycho's), NASA/CXC

Fraschetti et al. (2010)

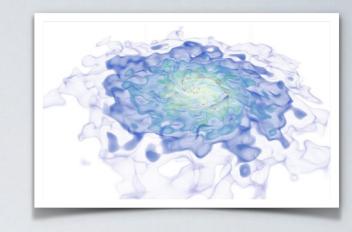
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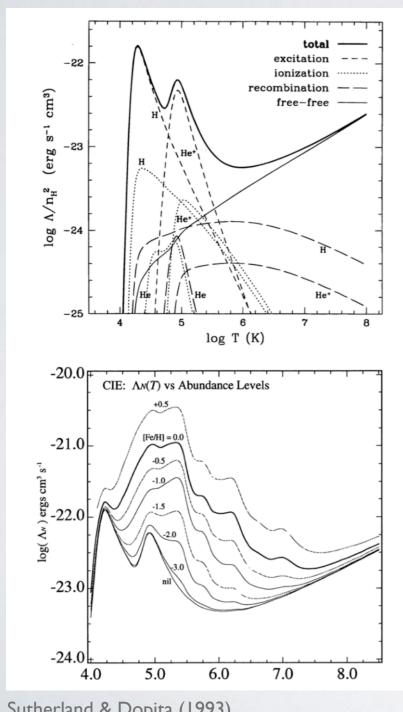
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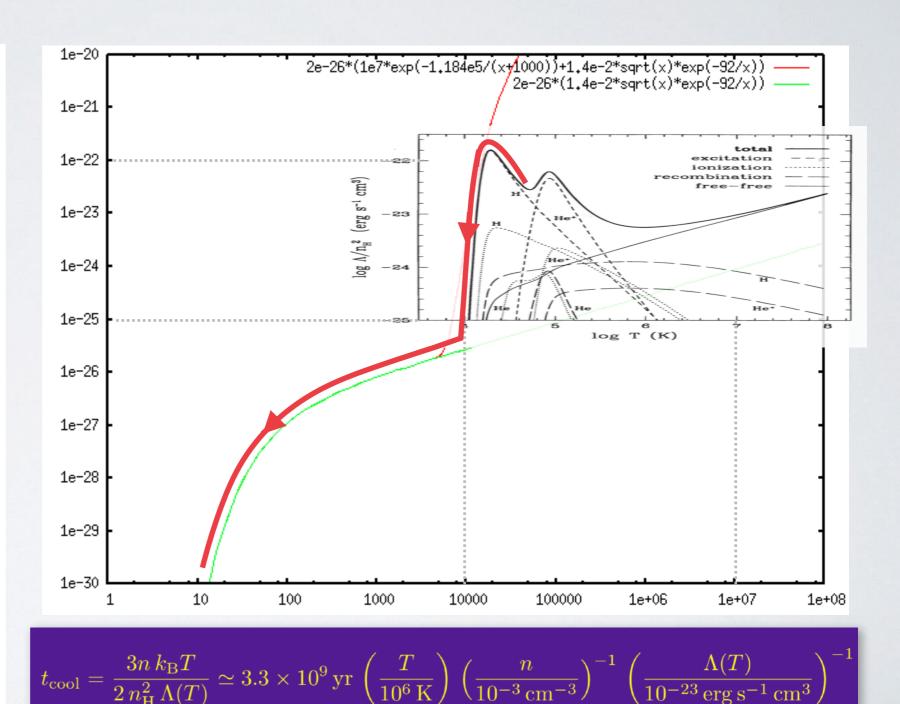


# Physics Processes in Simulations Continues

# "Radiative Cooling"

Baryons cool by radiating photons (atomic processes).

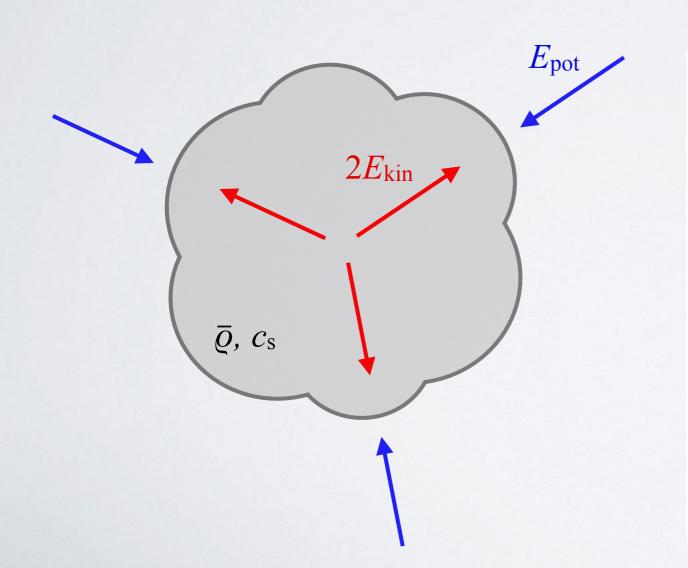




Sutherland & Dopita (1993)

# "Jeans Instability"

• If the gas pressure of a cloud can no longer balance the self-gravity, the cloud becomes gravitationally unstable and collapses.



Jeans unstable if virial equilibrium breaks down with the gas pressure that is not strong enough:

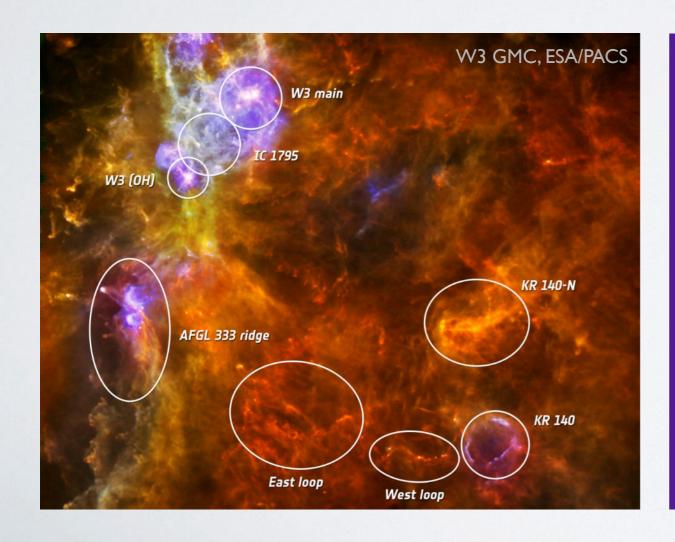
$$2\langle E_{\rm kin} \rangle < -\langle E_{\rm pot} \rangle$$

$$\rightarrow M\langle v^2 \rangle < GM^2/R$$

$$\rightarrow M > M_{\rm Jeans} \simeq \frac{c_{\rm s}^3}{G^{3/2}\bar{\rho}^{1/2}}$$

# Jeans Mass and Fragmentation

- Jeans mass (M<sub>Jeans</sub>) is the minimum mass of a gravitationally unstable cloud. Once M<sub>Jeans</sub> is exceeded, runaway collapse occurs.
- Increase in  $\bar{\rho}$  (or decrease in  $c_s$ ) reduces  $M_{Jeans}$ . This means that as the cloud collapses, it will fragment into even smaller clouds.



When the gas is gravitationally compressed, it takes  $t_{\text{sc}}$  for pressure waves to cross the region and restore the pressure–gravity balance.

But, if the cloud collapses quicker than the pressure waves can respond, then the balance breaks down.

$$t_{\rm ff} = \left(\frac{3\pi}{32G\bar{\rho}}\right)^{1/2} < t_{\rm sc} = \frac{R}{c_{\rm s}}$$

$$\rightarrow M > M_{\rm Jeans} \simeq \frac{c_{\rm s}^3}{G^{3/2}\bar{\rho}^{1/2}}$$