# Boosting the discovery of $p\,p \to h\,h \to b\,b\,\tau\,\tau$ at the LHC

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(Yonsei University)

In collaboration with

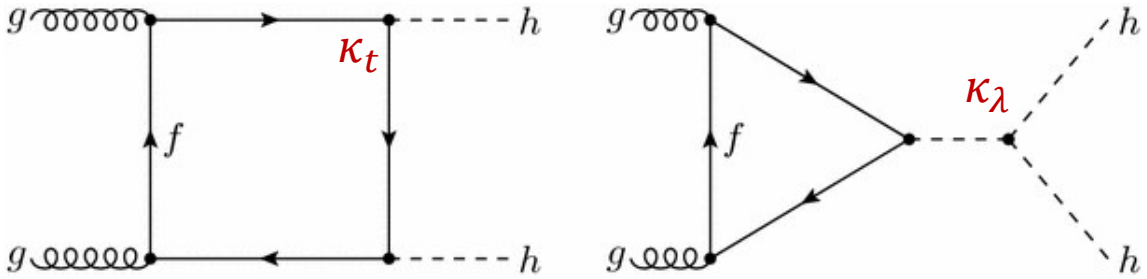
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# Introduction

- **Higgs pair production**




- **Higgs self-coupling**

$$\mathcal{L}_h = \frac{1}{2}\partial^\mu h \partial_\mu h - \frac{1}{2}m_h^2 h^2 - \kappa_\lambda \lambda_{SM} v h^3 - \frac{m_t}{v}(v + \kappa_t h)(\bar{t}_L t_R + h.c) + \cdots$$

✓ Di-Higgs search has a meaning to measure the Higgs self coupling and to understand the Higgs potential

✓ The topology is determine by each Higgs decay chain

Figure ref : arXiv:1512.08928

# Signal vs Background

@ 14TeV, 39.64 fb (HH), 953.6 fb (TT)

| Channel | Leptons | X section | Topology $* \ l = e \ or \ \mu$ |
|---|---|---|---|
| HH2Tau | 0 | ~1.2 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| TT2Tau | 0 | ~5097.2 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| HH2Tau | 1 | ~1.3 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2W*W | 1 | ~0.15 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2WW* | 1 | ~0.15 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ \tau_h + met$ |
| TT2Tau | 1 | ~5546.3 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ l + met$ |
| TT1Tau | 1 | ~29700.2 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2Tau | 2 | ~0.36 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ l\ l + met$ |
| HH2W*W1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW*1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW0Tau | 2 | ~0.47 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ l + met$ |
| TT2Tau | 2 | ~1508.7 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| TT1Tau | 2 | ~16158.3 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l + met$ |
| TT0Tau | 2 | ~43263.9 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ l\ l + met$ |

# Signal vs Background

@ 14TeV, 39.64 fb (HH), 953.6 fb (TT)

| Channel | Leptons | X section | Topology $* \ l = e \ or \ \mu$ |
|---|---|---|---|
| HH2Tau | 0 | ~1.2 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| TT2Tau | 0 | ~5097.2 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| HH2Tau | 1 | ~1.3 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2W*W | 1 | ~0.15 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2WW* | 1 | ~0.15 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ \tau_h + met$ |
| TT2Tau | 1 | 5546.2 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ l + met$ |
| TT1Tau | 1 | 11316.4 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2Tau | 2 | 0.30 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ l + met$ |
| HH2W*W1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW*1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW0Tau | 2 | ~0.47 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ l + met$ |
| TT2Tau | 2 | ~1508.7 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| TT1Tau | 2 | ~16158.3 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l + met$ |
| TT0Tau | 2 | ~43263.9 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ l\ l + met$ |

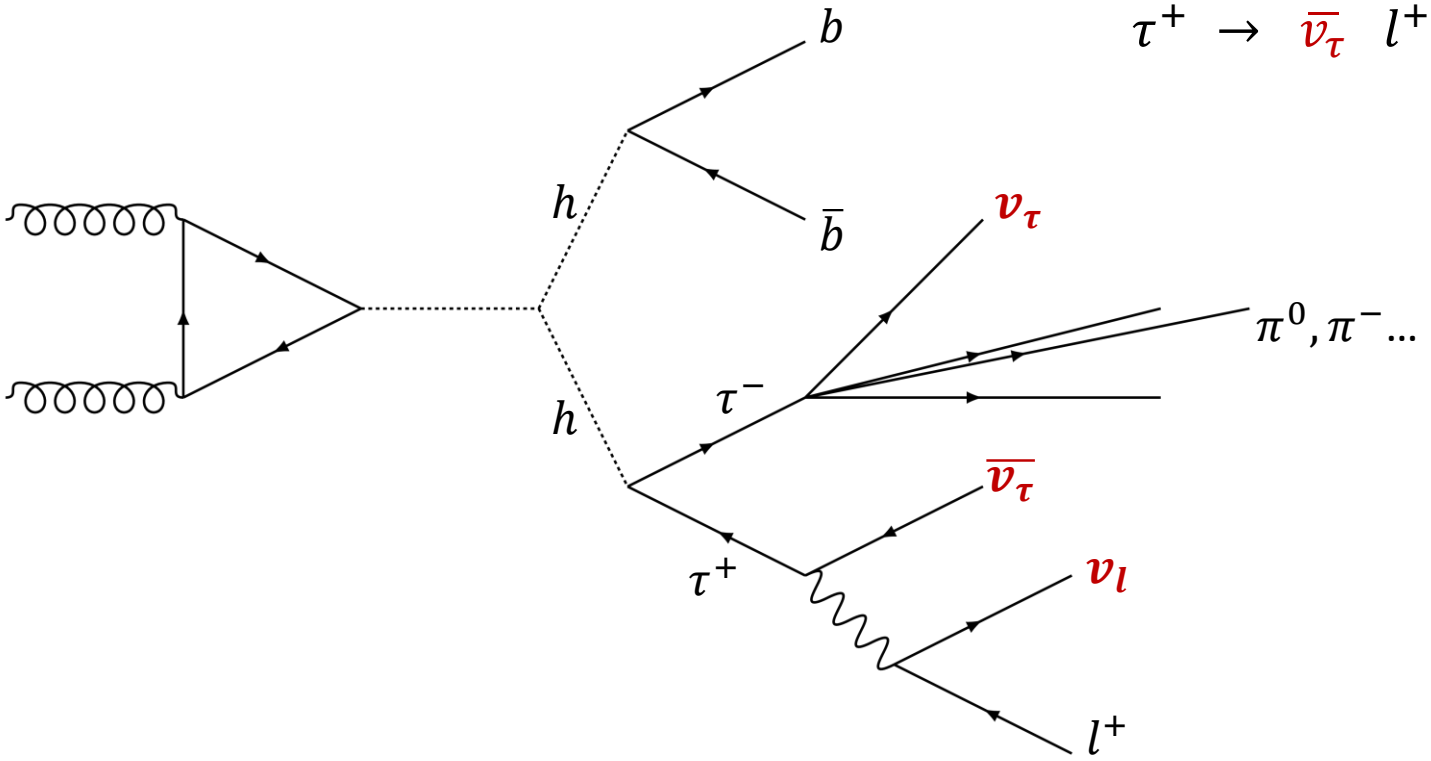
**Too Many $t\bar{t}$ Background**

# How to reconstruct the missing information?

**Ex) HH2tau : 1 lepton + 1 tau_h Channel** $hh \rightarrow b\,b\,\tau^-\tau^+$

$\tau^- \rightarrow \nu_\tau \;\; \tau_h$

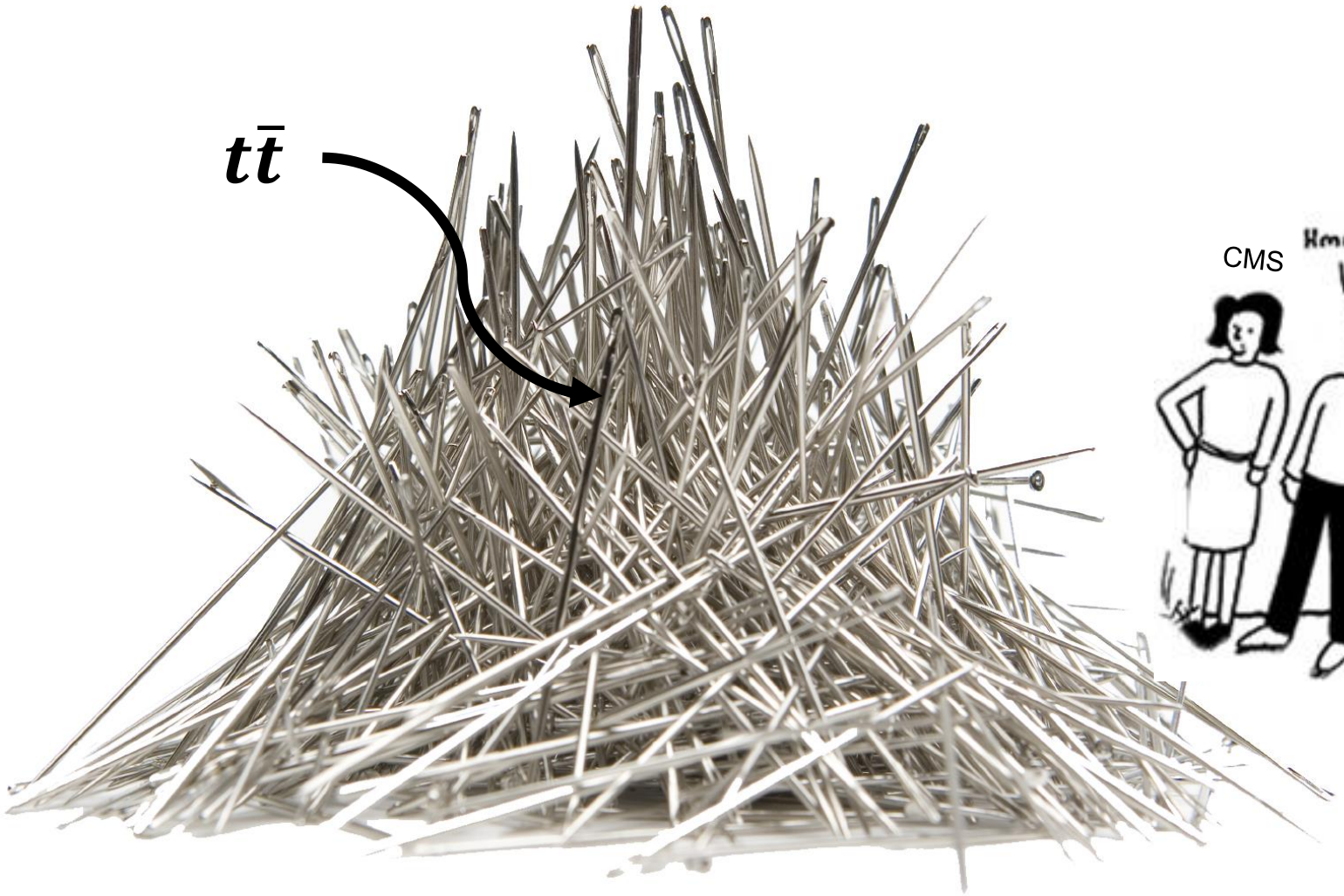
$\tau^+ \rightarrow \bar{\nu}_\tau \;\; l^+ \;\; \tau_l$




$\mathbf{H \rightarrow \tau\tau/WW}$

**# of Neutrinos >= 2**

# A Needle(HH) in a stack of Needles($t\bar{t}$)




**HH?**

# OptiMass introduction

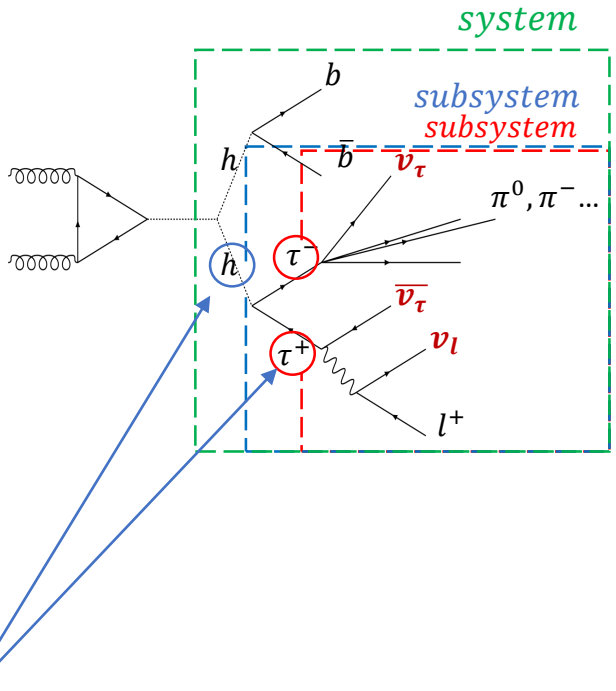
$M$ = *minimized mass variable function*
$\lambda_a$ = *augmented Lagrange parameter*
$\mu$ = *penalty parameter*
$\vec{x}$ = ***missing momentum***
$c_a$ = ***physical constraints***

- Augmented Lagrangian method

$$\mathcal{L}_k(\vec{x} \mid \lambda, \mu) = \boldsymbol{M(\vec{x})} - \sum_{a=1}^{m} \lambda_{ak}\, c_a(\vec{x}) + \frac{1}{2\mu_k} \sum_{a} c_a^2(\vec{x}).$$

$$\lambda_a^{k+1} = \lambda_a^k - \frac{c_a(\vec{x}_k)}{\mu_k}$$

$$\boldsymbol{CD} = ||c(\vec{x}_k)|| < \eta^* \quad with\ ||c(\vec{x}_k)|| = \sqrt{\sum_a |c_a(\vec{x}_k)|^2}$$




✓ **OM (OptiMass)** ~ TARGET MASS

✓ **CD (Compatibility Distance)** ~ **0** for TRUE SYSTEM

**OPTIMASS: A Package for the Minimization of Kinematic Mass Functions with Constraints**
- Cho, Won Sang *et al.* JHEP 1601 (2016) 026 arXiv:1508.00589

# Multi-Variable Classification

- All distinctive decay topology ⇒ Characterized by each constraints, $c_a$ / systems
- Using **OptiMass**, we can reconstruct the mass of systems/subsystems
  ⇒ the classes for MVA classification

| For 1 lepton Channel | |
|---|---|
| OM h2ta S | CD h2ta S |
| OM h2ta Mh1 | CD h2ta Mh1 |
| OM h2ta maxMta12 | CD h2ta maxMta12 |
| OM h1tawos S | CD h1tawos S |
| OM h1tawos Mh1 | CD h1tawos Mh1 |
| OM h1tawos maxMw12 | CD h1tawos maxMw12 |
| OM h1tawoff maxMw12 | CD h1tawoff maxMw12 |
| … | … |
| OM t2ta S | CD t2ta S |
| OM t2ta maxMt12 | CD t2ta maxMt12 |
| OM t2ta maxMta12 | CD t2ta maxMta12 |
| OM t2ta maxMw12 | CD t2ta maxMw12 |
| OM t1ta S | CD t1ta S |
| OM t1ta maxMt12 | CD t1ta maxMt12 |
| … | … |

| For 0 lepton Channel | |
|---|---|
| OM h2ta S | CD h2ta S |
| OM h2ta Mh1 | CD h2ta Mh1 |
| OM h2ta maxMta12 | CD h2ta maxMta12 |
| OM t2ta S | CD t2ta S |
| OM t2ta maxMt12 | CD t2ta maxMt12 |
| OM t2ta maxMta12 | CD t2ta maxMta12 |
| OM t2ta maxMw12 | CD t2ta maxMw12 |
| OM t2ta maxMt12_c2_etas05 | CD t2ta maxMt12_c2_etas05 |
| OM t2ta maxMt12_c1_etas005 | CD t2ta maxMt12_c1_etas005 |
| OM t2ta maxMt12 c2_etas01 | CD t2ta maxMt12 c2_etas01 |

- ✓ (0l) # ( Visible Features )
  **= 12 dim**
- ✓ (0l) # ( OM Features )
  **= 6(hh)+14(ttbar) = 20 dim**
- ✓ (1l) # ( Visible Features )
  **= 12 dim**
- ✓ (1l) # ( OM Features )
  **= 30(hh)+22(ttbar) = 52 dim**
- ✓ (2l) # ( Visible Features )
- (2l) # ( OM Features )
  **= (Talk on Thu.**
  **By Dr. Wonsang Cho )**

❖ **Visible : CMS/ATLAS common features ~ $p_T, \Delta R, \Delta\phi$ …**

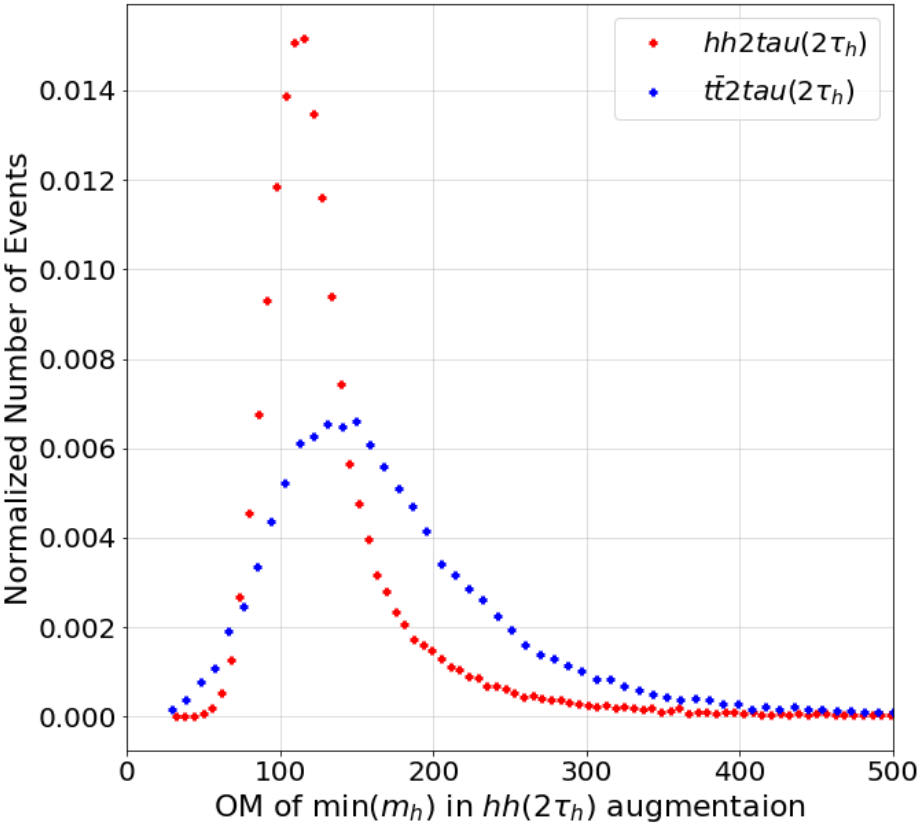
# Event Selection

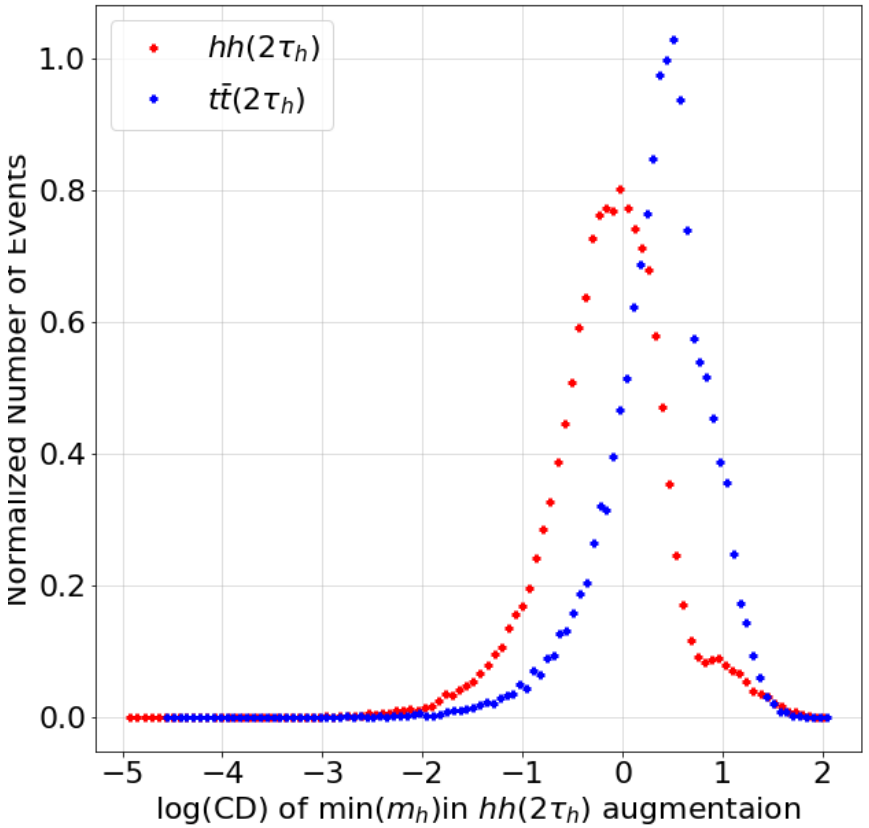
- **Using …**
  - MC : MG5_aMC v2.5.5 + MADSPIN (Decay)
  - Showering : PYTHIA8
  - Detector Simulation : Delphes
  - CT10nlo for all Channel

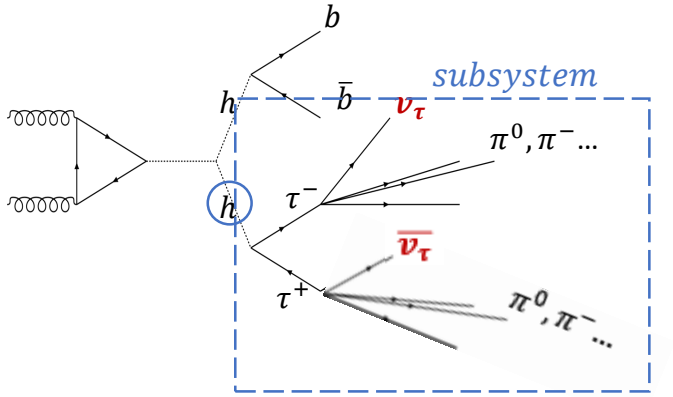
- **Cut …**
  - Delphes : Using delphes_card_ATLAS.dat
  - Tau Tagging : $\Delta R < 0.4$ , $\Delta R_{track} < 0.2$ , $P_T^{Track} > 1.0$ , $P_T^{\tau} > 2.0$ , $\eta_{\tau} < 2.5$
    1-prong Eff = 70% , N(>1)-prong eff = 60%
  - Others are same with delphes_card_ATLAS.dat default

- Hadronic Tau decay using ALL N-prongs

# 0-lepton & 2-hadronic decay tau



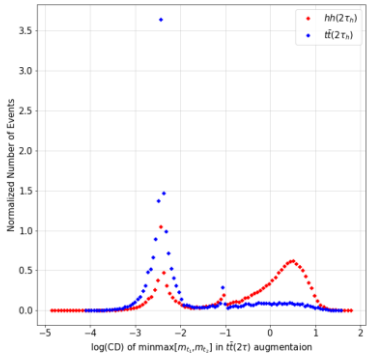



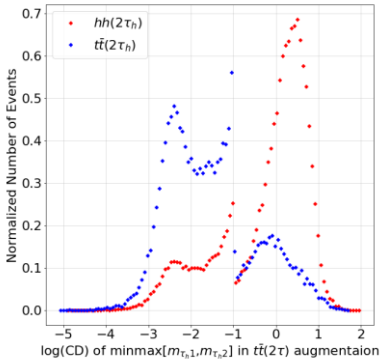



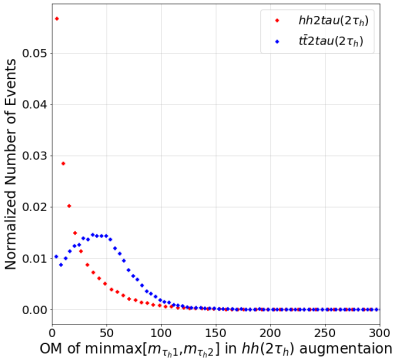

**Constraints of Mass**

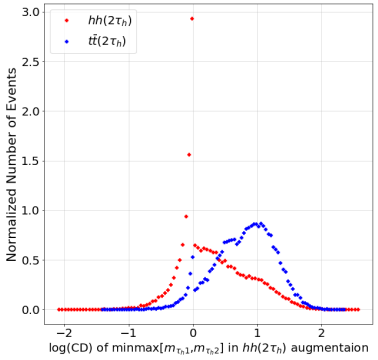
- Tau1 = 1.77
- Tau2 = 1.77
- Tau1 = Tau2

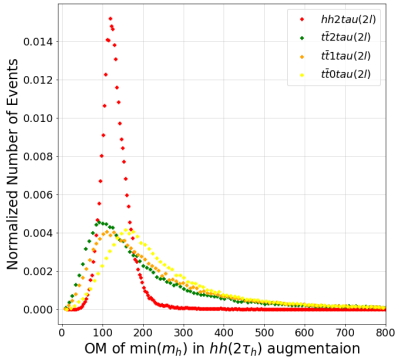
# OM/CD of (2l,1l,0l) Channels

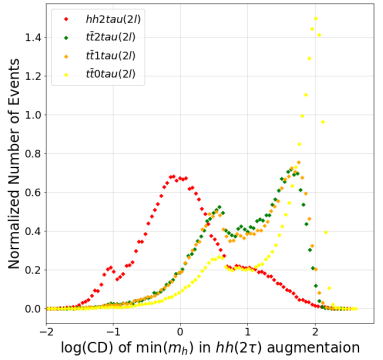


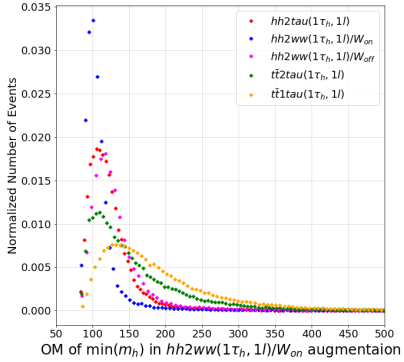



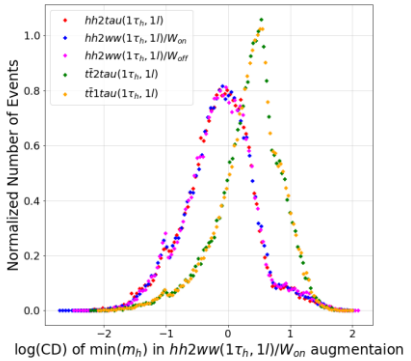



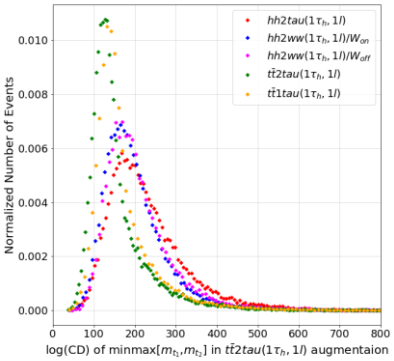



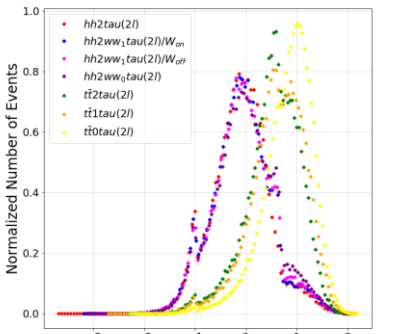



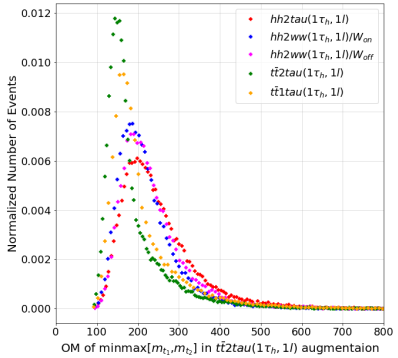



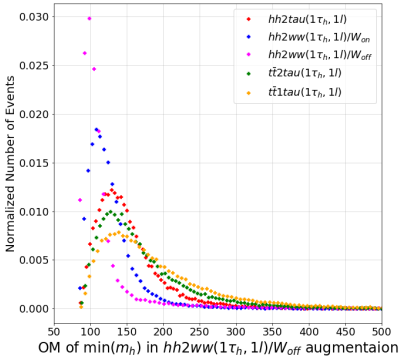



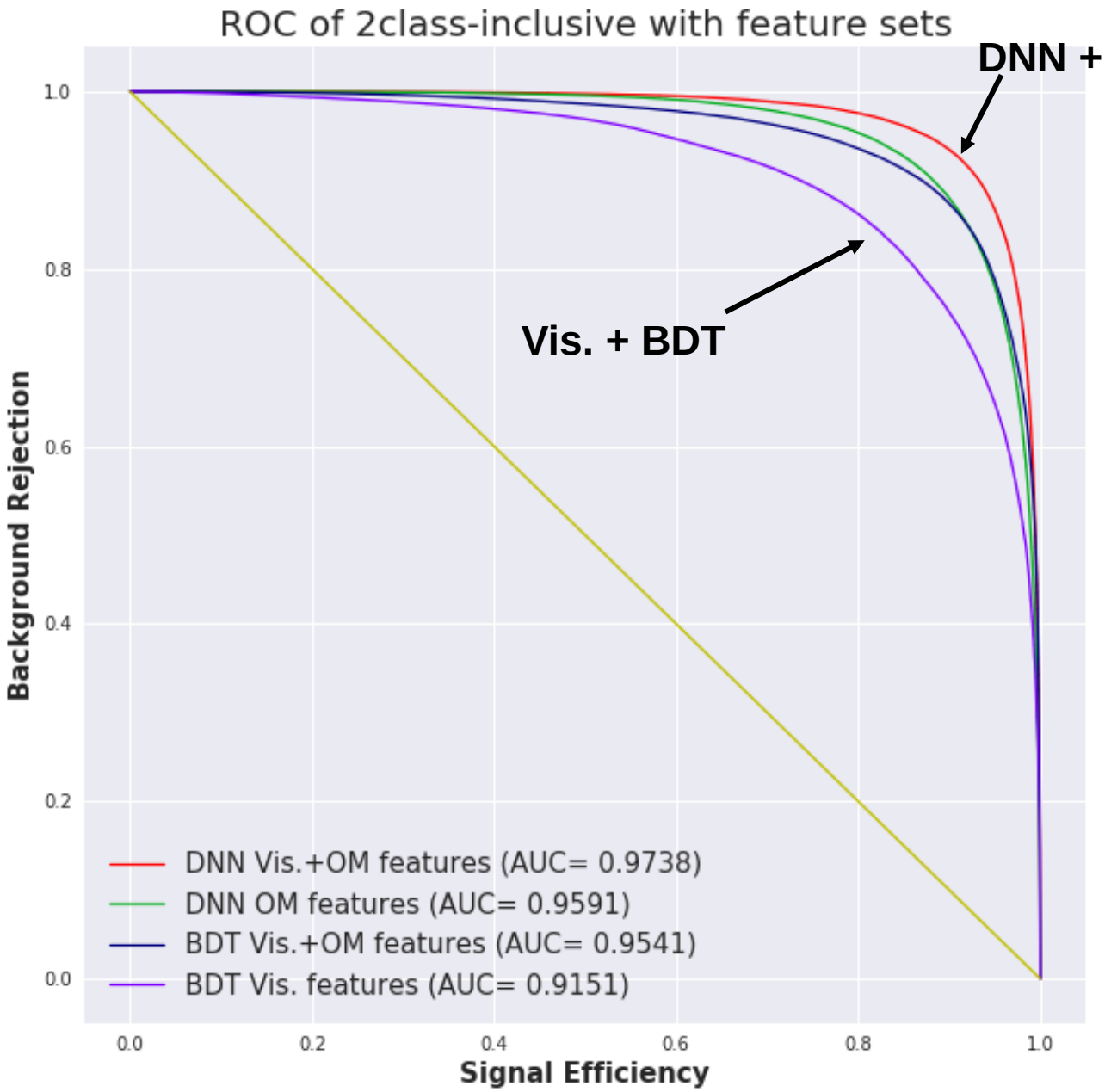



# DNN vs BDT

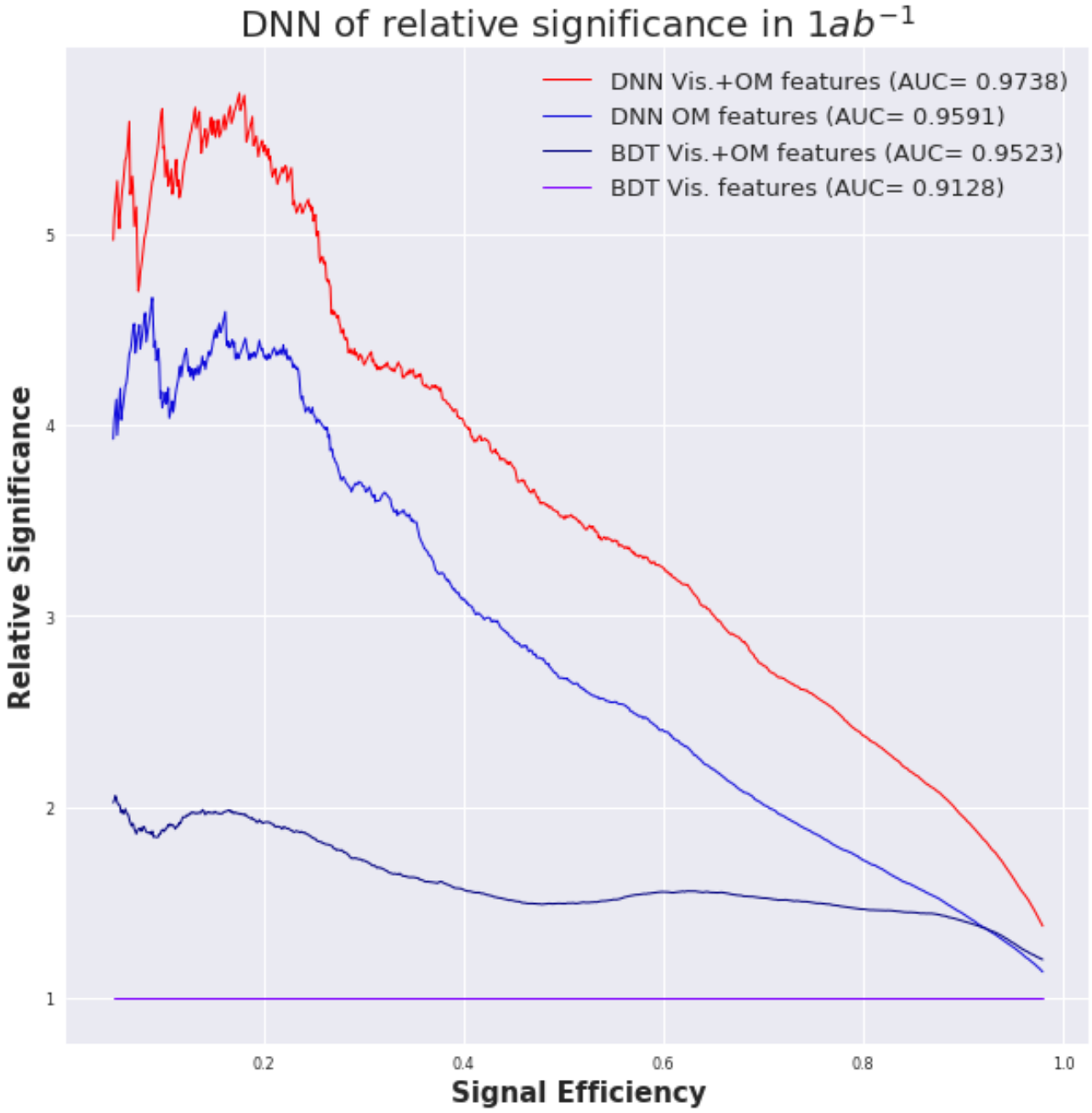
- **Deep Neural Network**
  - ✓ Keras + Tensorflow module
  - ✓ 7~8 hidden layers + 500 nodes per hidden layers
  - ✓ 2 / 5 / 7 nodes output ( for each class )
  - ✓ Using 'RELU' Activation function + 'SoftMax' output layer
  - ✓ Dropout = 0.2~3 + Batch Normalization

- **Boost Decision Tree**
  - ✓ Using 'AdaBoostClassification' in sklearn module
  - ✓ Max_depth = 2~3
  - ✓ # of Estimators = 500~1000, learning rate = 0.01
  - ✓ Algorithm = 'SAMME'

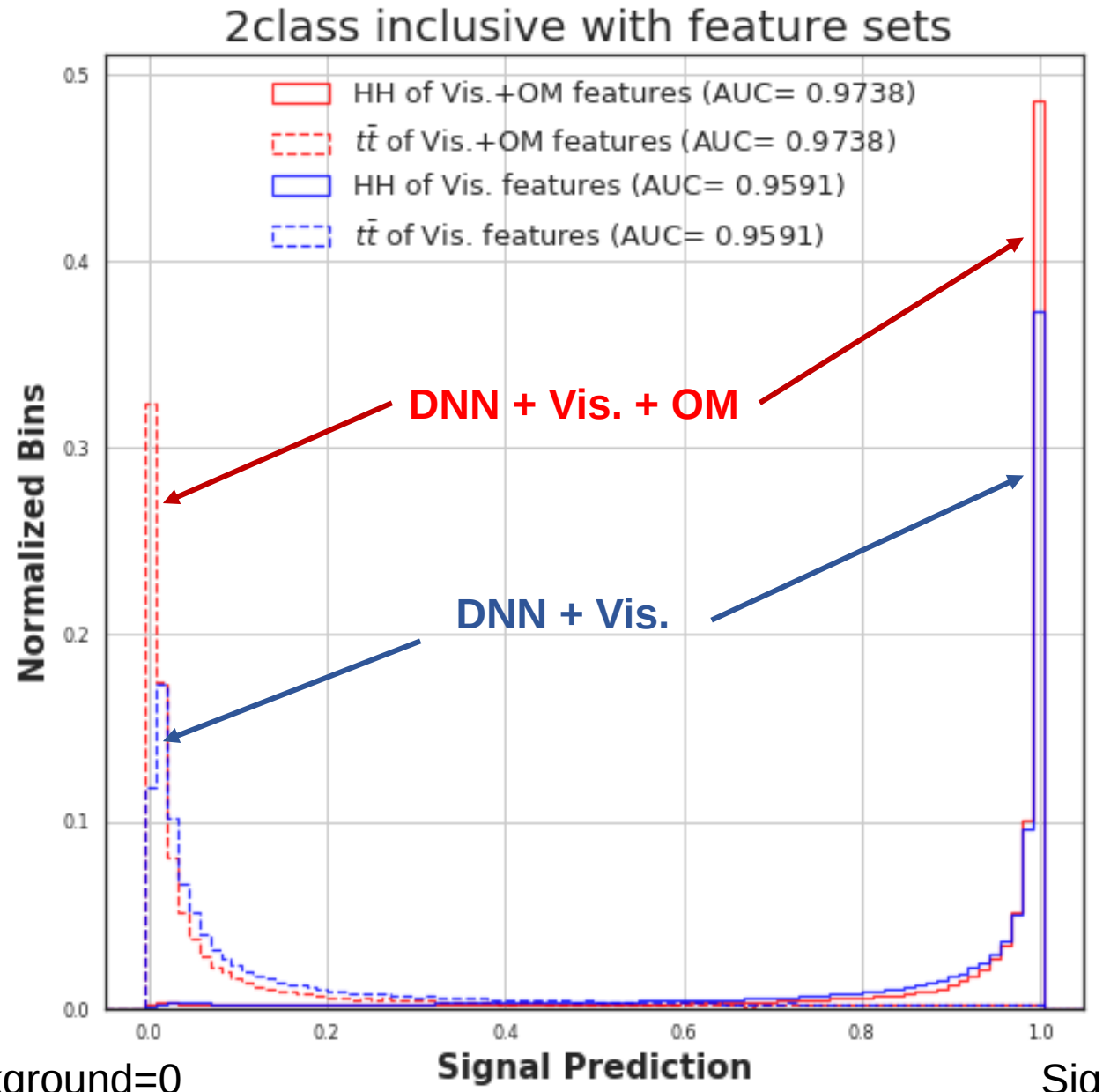
# ROC Result for 0 lep (2b+2tau_h)



# Significance Result for 0 lep (2b+2tau_h)



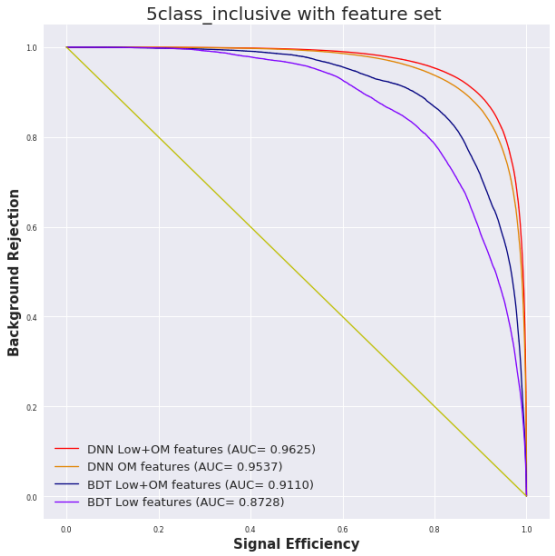
# Result for 0 lep (2b+2tau_h)

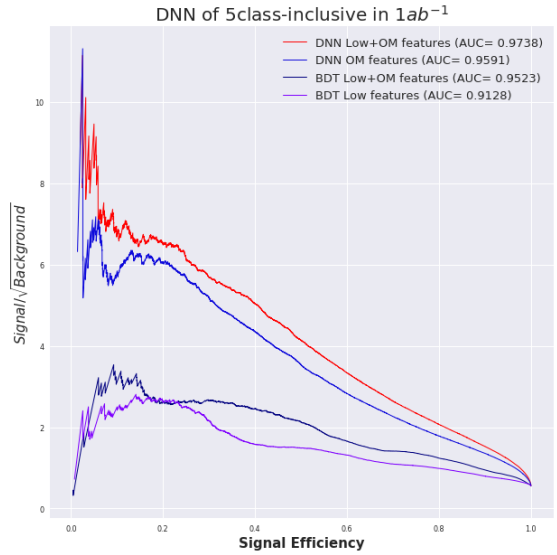


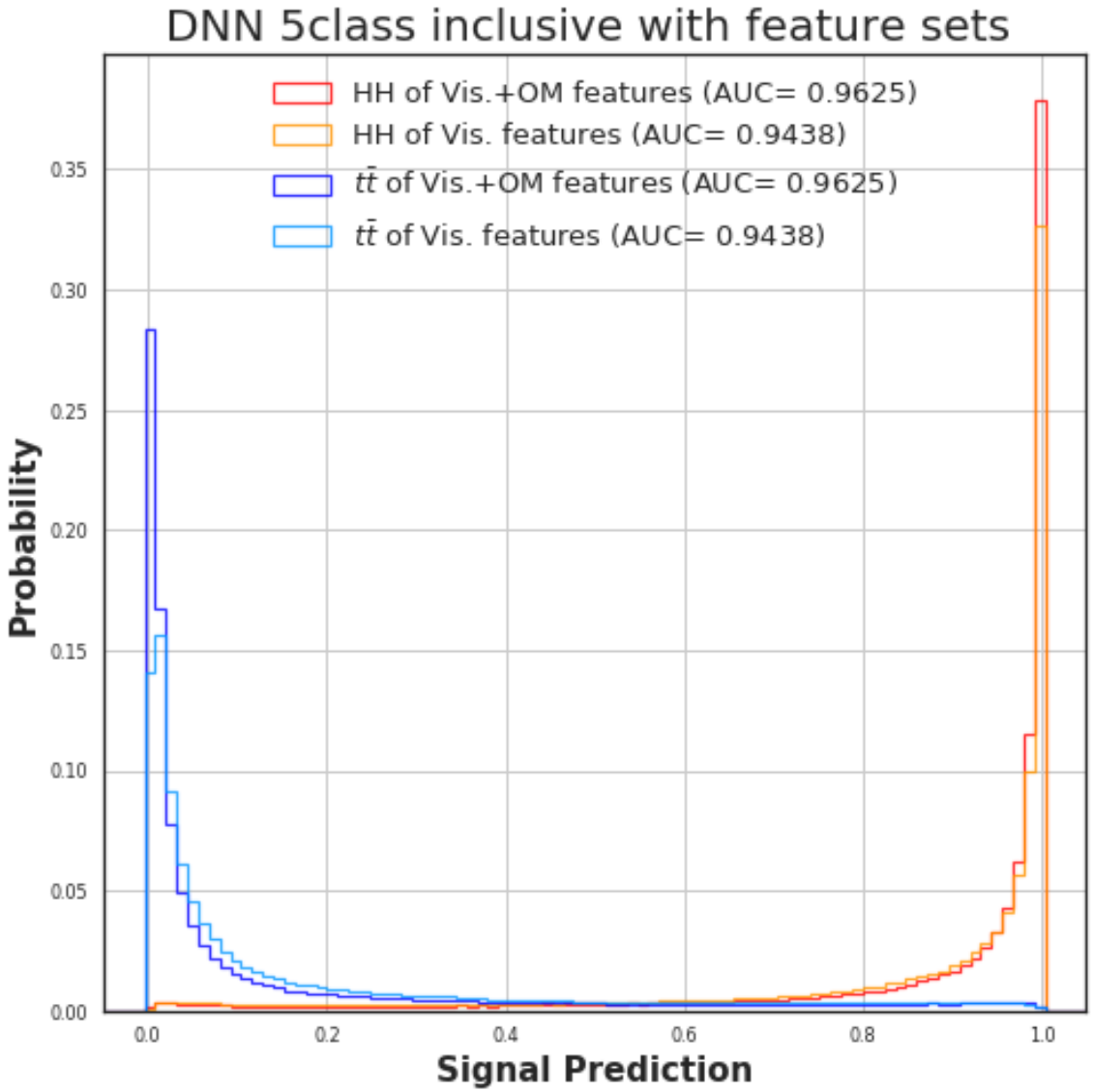

Background=0

Signal=1

# Classification Result for (1l) Channels



# Variable Importance Score Result for (0/1) lepton

| Rank | Feature Variables | Importance |
|---|---|---|
| 1 | **OM h2ta maxMta12** | **11%** |
| 2 | dR_bb | 10% |
| 3 | mt2_bbtata | 9% |
| 4 | **CD t2ta maxMta12** | **9%** |
| 5 | **CD h2ta maxMta12** | **9%** |
| 6 | **CD h2ta S** | **8%** |
| 7 | pT_tata | 8% |
| 8 | **CD h2ta Mh1** | **7%** |
| 9 | **CD t2ta maxMt12 c2_etas01** | **7%** |
| 10 | dR_tata | 5% |
| 11 | pT_bb | 3% |
| 12 | **OM t2ta maxMt12 c1_etas1** | **3%** |
| 13 | **OM t2ta maxMt12 c2_etas01** | **2%** |
| 14 | dphi_bbmet | 2% |
| 15 | **OM h2ta Mh1** | **2%** |
| 16 | **OM t2ta maxMt12** | **2%** |

| Rank | Feature Variables | Importance |
|---|---|---|
| 1 | **OM h2ta maxMta12** | **21%** |
| 2 | **OM h1tawos Mw1** | **15%** |
| 3 | dr_lta | 10% |
| 4 | pt_lta | 10% |
| 5 | **OM h2ta Mh1** | **9%** |
| 6 | dr_bb | 5% |
| 7 | **CD h2ta S** | **5%** |
| 8 | **CD h2ta Mh1** | **5%** |
| 9 | mt_ta1 | 3% |
| 10 | **OM h1tawoff Mw2** | **2%** |
| 11 | **OM h1tawos maxMw12** | **2%** |
| 12 | **OM h1tawos Mh1** | **2%** |
| 13 | **OM h1tawoff Mh1 c2_etas100** | **1%** |
| 14 | **OM h1tawoff maxMw12** | **1%** |
| 15 | **CD h1tawos Mh1** | **1%** |
| 16 | **CD t1ta S** | **1%** |
| 17 | **CD h1tawos Mh1 c2_etas10** | **1%** |

# Result of 0/1-lepton

@ 14TeV, 39.64 fb (HH), 953.6 fb (TT)
1000 fb luminosity (1 $ab^{-1}$)

| | HH2Tau | TT2Tau | HH2Tau | TT2Tau |
|---|---|---|---|---|
| Cross Section | ~1.2 | ~5097.2 | ~1.6 | ~35246.5 |
| Number of Detected | ~1,200 | ~5,097,200 | ~1,600 | ~35,246,500 |
| | ↓ # of remained ↓ | | | |
| BDT + Visible | ~240 | ~65,659 | ~328 | ~19,803 |
| BDT + Visible + OM | ~240 | ~17,630 | ~328 | ~18,615 |
| **DNN + OM** | **~240** | **~3,205** | **~328** | **~3,329** |
| **DNN + Visible + OM** | **~240** | **~1,995** | **~328** | **~2,831** |

Assume the same amount of signal

# Conclusion

- ✓ Discovering **HH** is important
- ✓ But we have to distinguish the signal from the **HUGE background (ttbar)**
- ✓ We introduce
  - **New Handles : "OPTIMASS Variables" (~40)**
  - **Improved Classification Method : "DNN"**

**AUC(CMS, BDT) = 0.91 -> AUC(Ours) = 0.97**

**!!! Use DNN + OPTIMASS Variables !!!**

# Q&A

# BACK UP

❖ **Visible : CMS/ATLAS common features**

- **CMS-HIG 17-002**

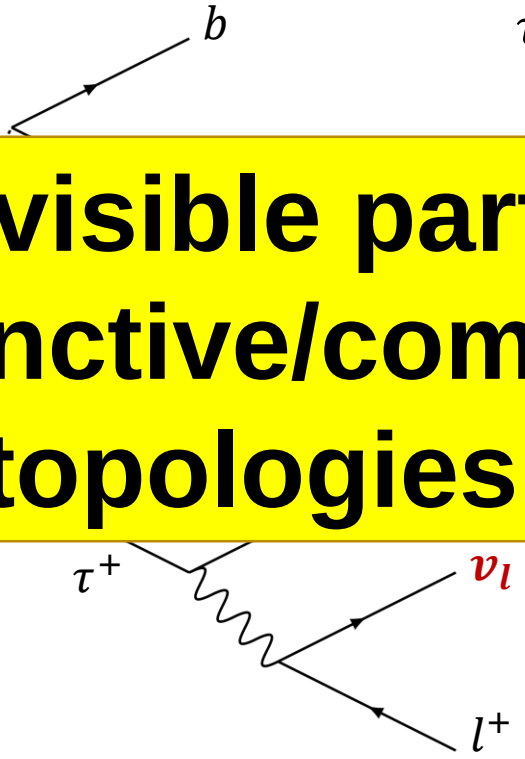
- 'dr_tata', 'dr_bb’
- 'dphi_bbtata’, 'dphi_tatamet'', 'dphi_bbmet', 'dphi_ta1met', 'dphi_ta2met'
- 'pt_tata', 'pt_bb’
- 'mt2_bbtata,'mt_ta1', 'mt_ta2'

# How to reconstruct the missing information?

**Ex) HH2tau : 1 lepton + 1 tau_h Channel** $hh \rightarrow b\,b\,\tau^-\tau^+$

$\tau^- \rightarrow \nu_\tau \;\; \tau_h$

$\tau^+ \rightarrow \bar{\nu}_\tau \;\; l^+ \;\; \tau_l$




**Too Many invisible particles from each distinctive/complicated decay topologies**

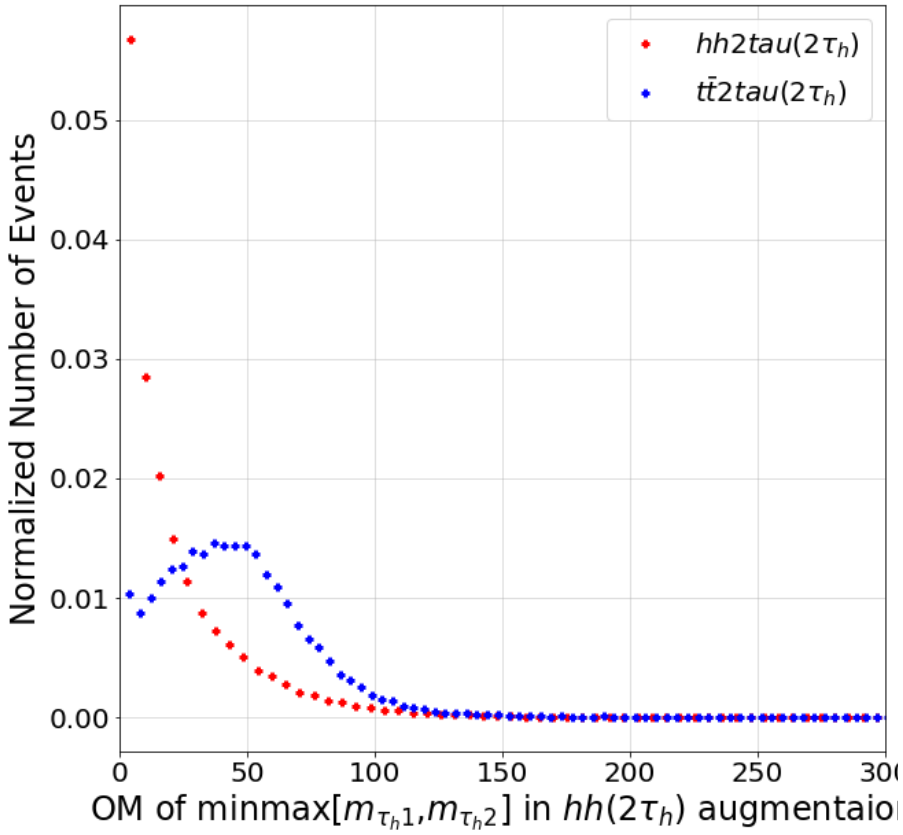
**# of Neutrinos >= 2**

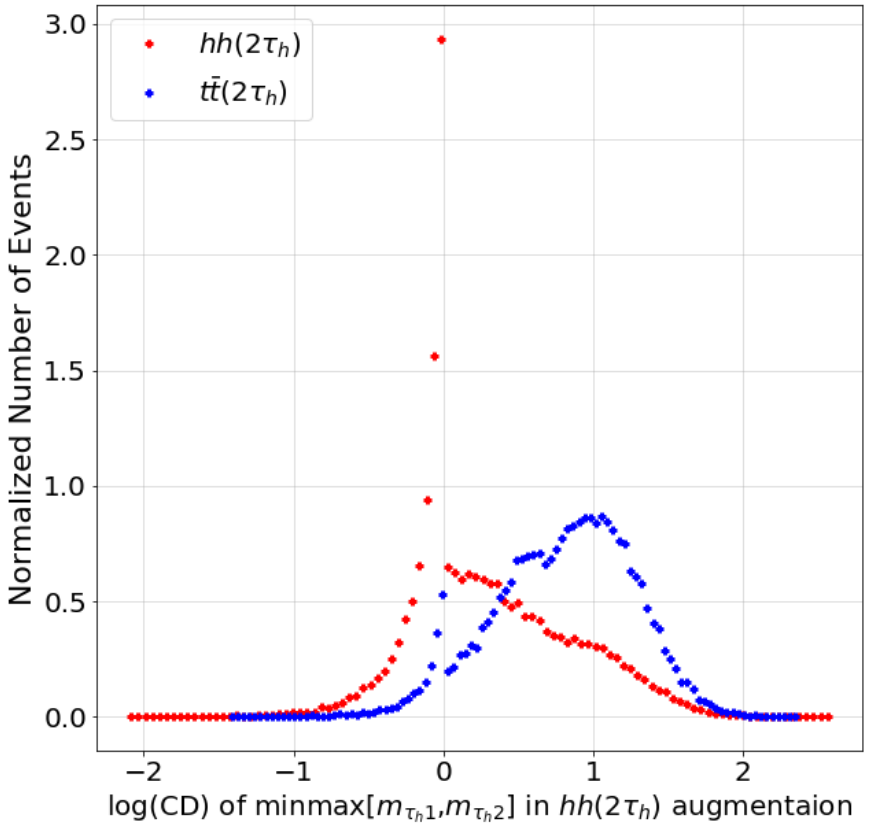
# Event Selection

$* \; l = e \; or \; \mu$

- **0-l**eptons + **2-h**adronic decay tau **(2 class)**
  - $(SG) \quad hh \rightarrow b\ b\ \tau\ \tau \qquad\qquad\qquad\qquad \rightarrow b\ b\ \tau_h\ \tau_h + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ \tau_h + met$
- **1-l**eptons + **1-h**adronic decay tau **(5 class)**
  - $(SG) \quad hh \rightarrow b\ b\ \tau\ \tau \qquad\qquad\qquad\qquad \rightarrow b\ b\ \tau_h\ l\ + met$
  - $(SG) \quad hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l\ + met$
  - $(SG) \quad hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ \tau_h\ + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ l\ + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ \tau_h\ l\ + met$
- **2-l**eptons + **0-h**adronic decay tau **(7 class)**
  - $(SG) \quad hh \rightarrow b\ b\ \tau\ \tau \qquad\qquad\qquad\qquad \rightarrow b\ b\ l\ l\ + met$
  - $(SG) \quad hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l\ + met$
  - $(SG) \quad hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ l\ + met$
  - $(SG) \quad hh \rightarrow b\ b\ w\ w^* \qquad\qquad\qquad\qquad \rightarrow b\ b\ l\ l\ + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ l\ l\ + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l\ + met$
  - $(BG) \quad \bar{t}t \rightarrow b\ w\ b\ w \qquad\qquad\qquad\qquad \rightarrow b\ b\ l\ l\ + met$

# 0-lepton & 2-hadronic decay tau



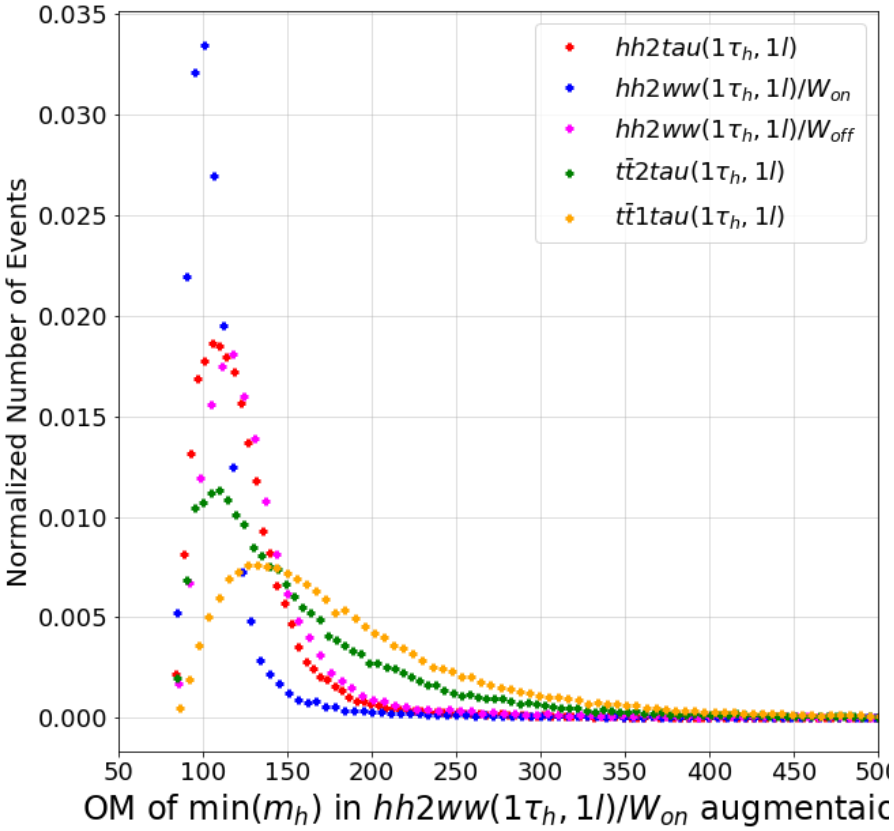
# Event Selection

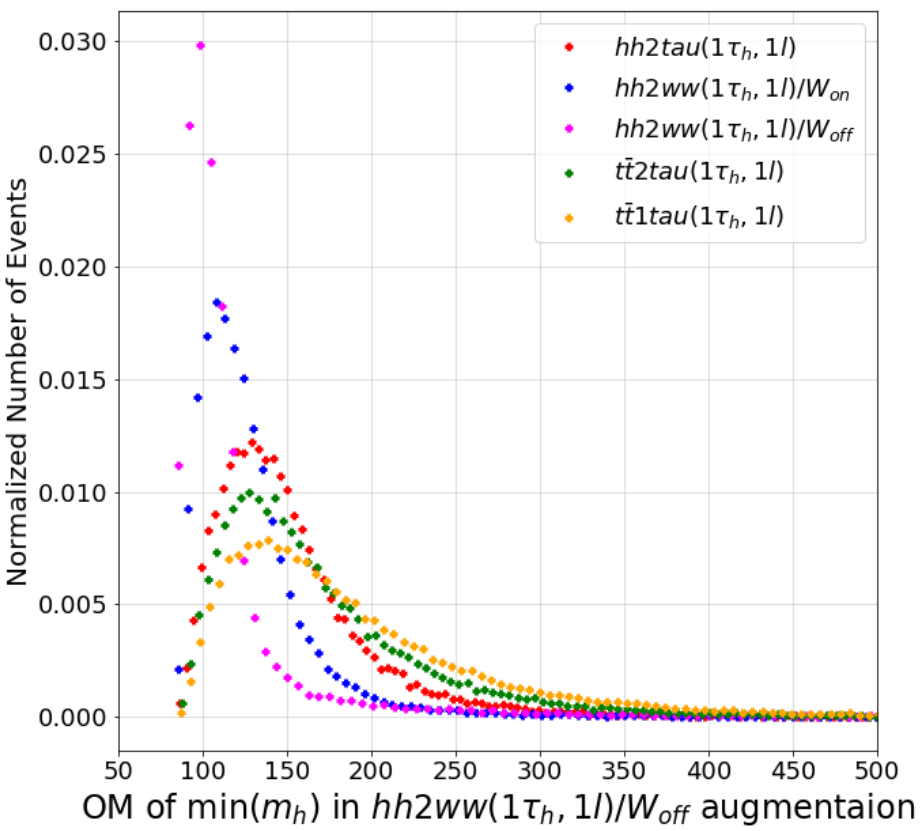
- Using …
  - MG5_aMC v2.5.5 + MADSPIN / Delphes / PYTHIA8
  - CT10nlo

- Cut …
  - Delphes : Using delphes_card_ATLAS.dat
  - Tau Tagging : $\Delta R < 0.4$ , $\Delta R_{track} < 0.2$ , $P_T^{Track} > 1.0$ , $P_T^{\tau} > 2.0$ , $\eta_{\tau} < 2.5$
    1-prong Eff = 70% , N(>1)-prong eff = 60%

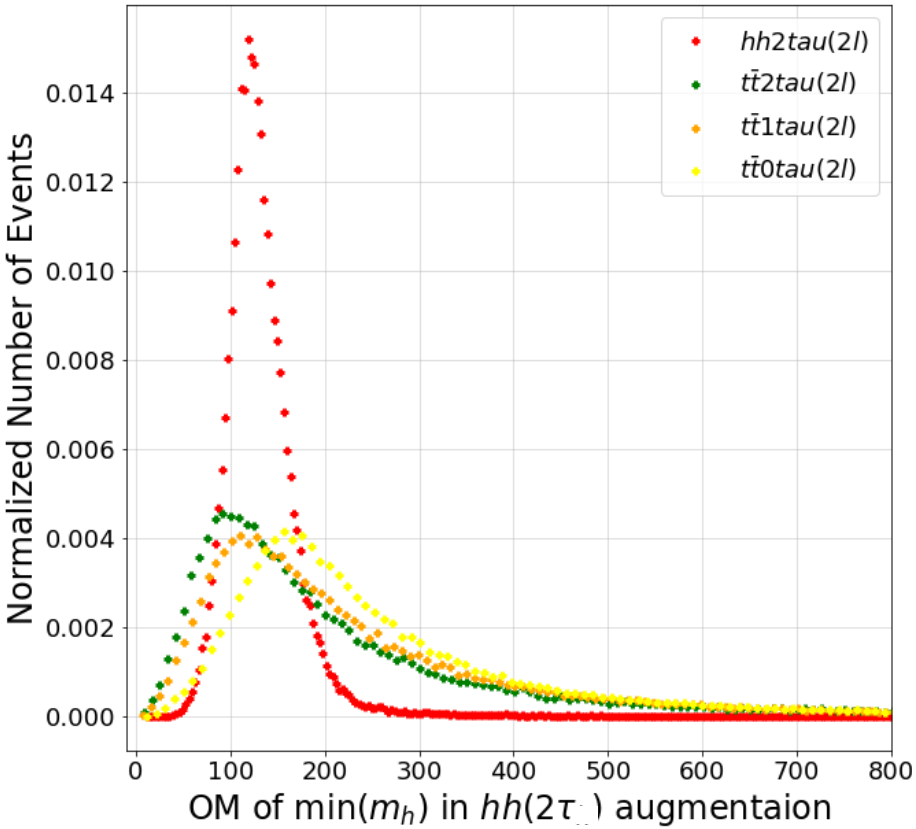
- Hadronical Tau decay using ALL N-prongs

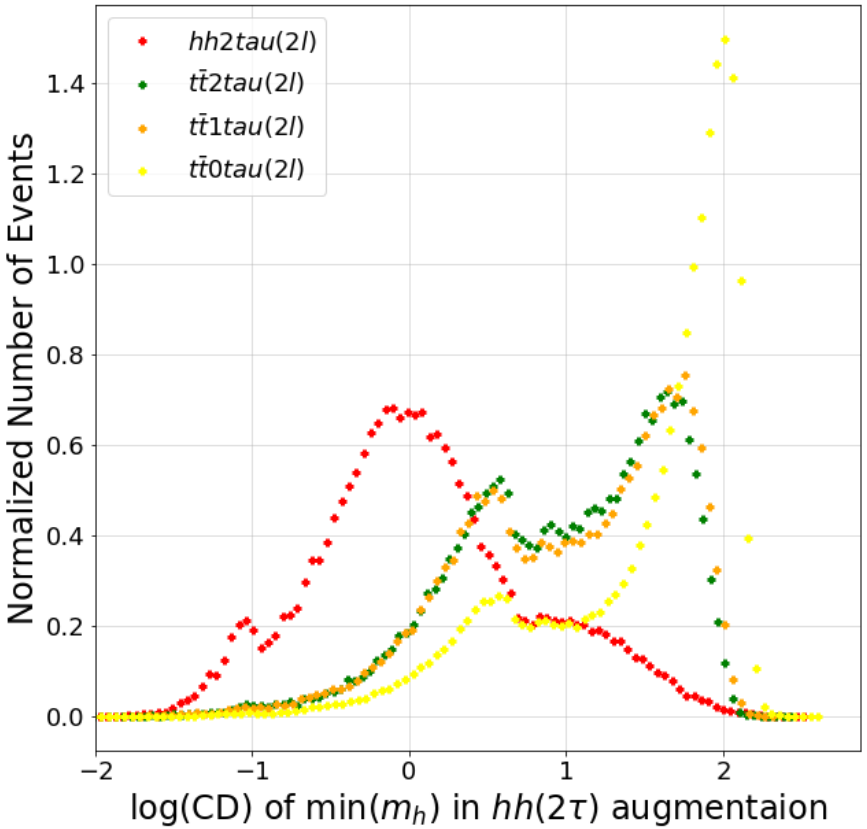
# 1-lepton & 1-hadronic decay tau



# 2-lepton & 0-hadronic decay tau

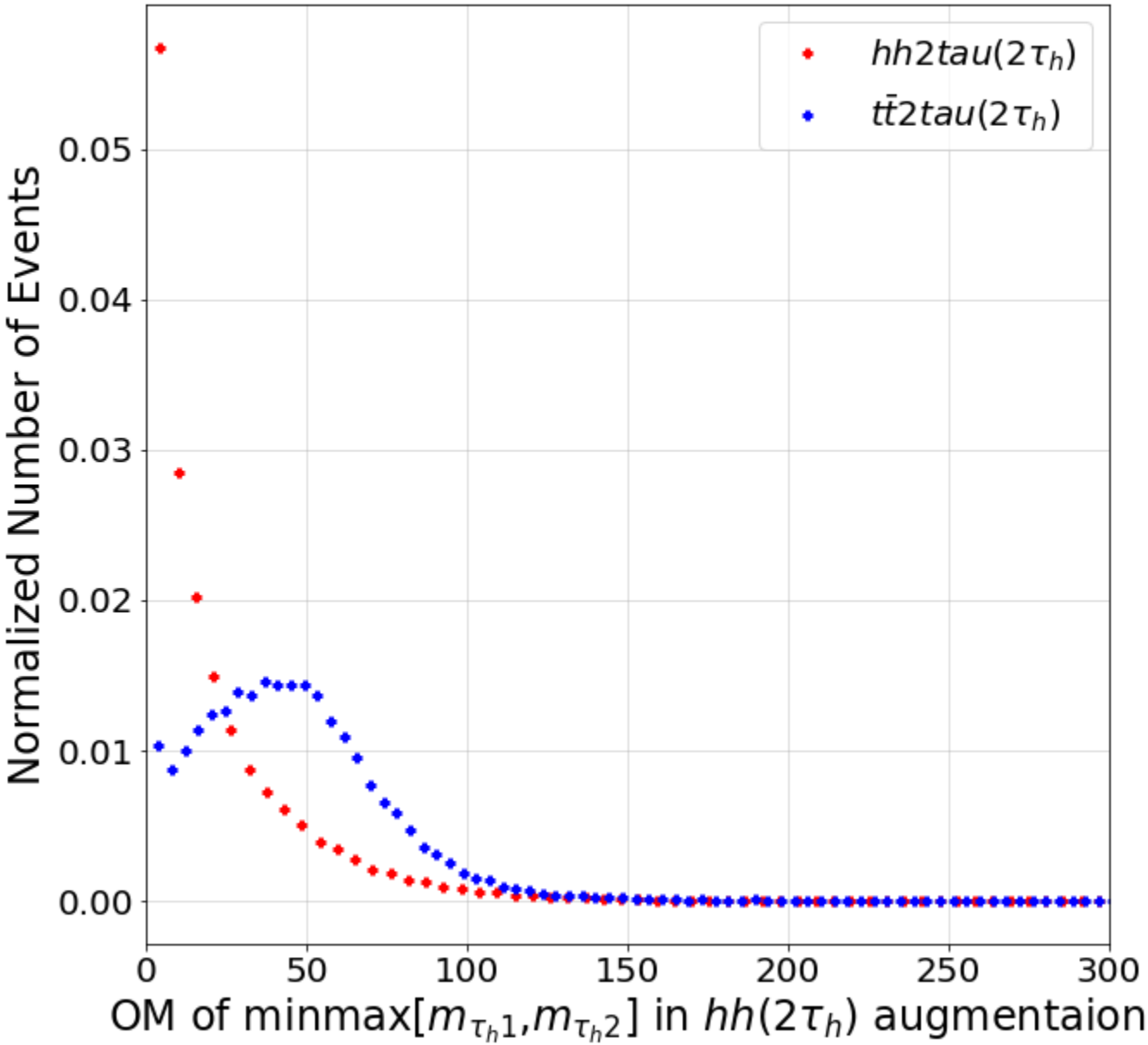



Constraints of Mass

- H1 (tata) = 125.
- H2 (bb) = 125.
- Tau1 = Tau2

# 0-lepton & 2-hadronic decay tau



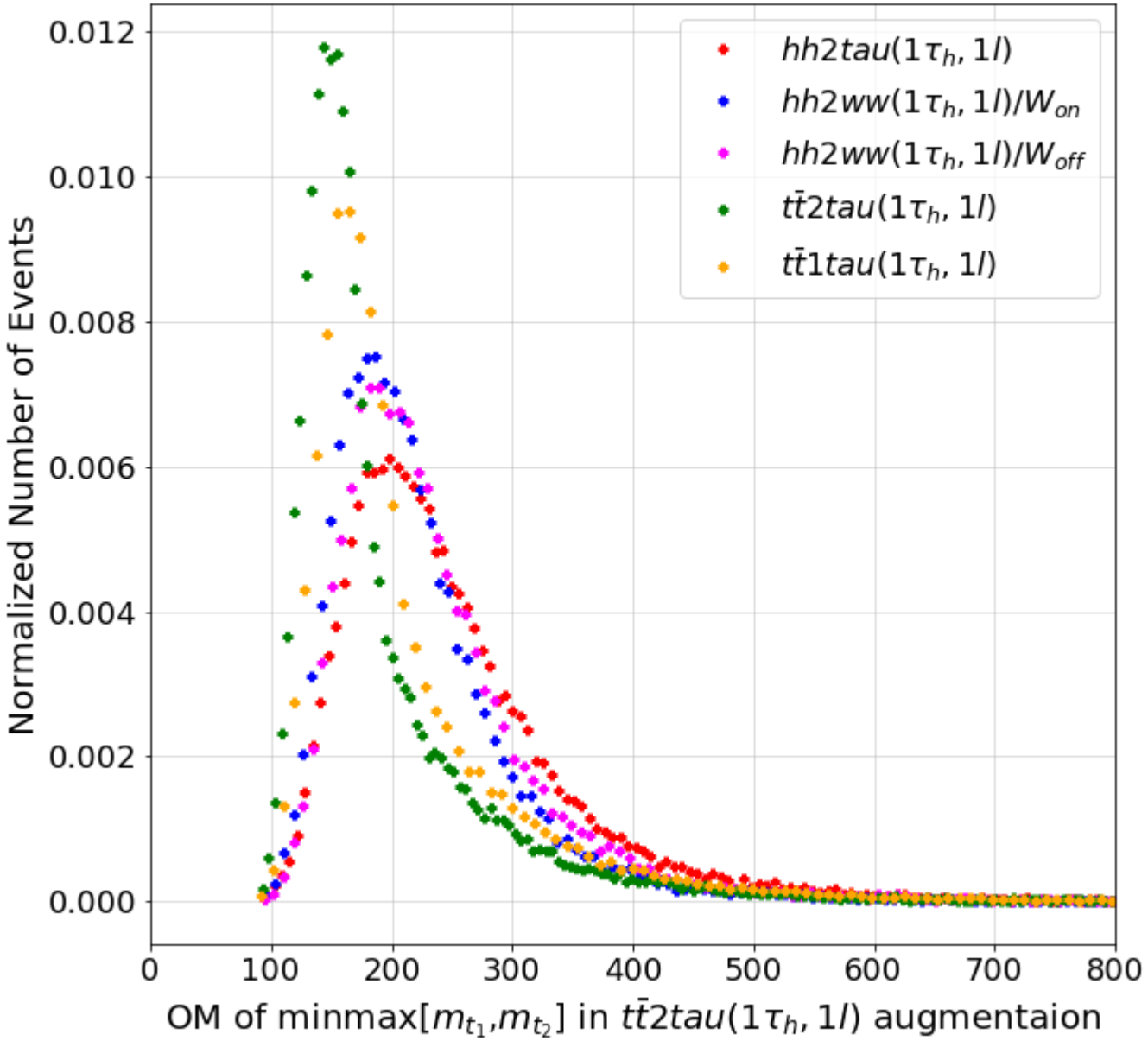

**Constraints of Mass**

- H1(tautau)= 125
- H2(bb)= 125
- Tau1 = Tau2

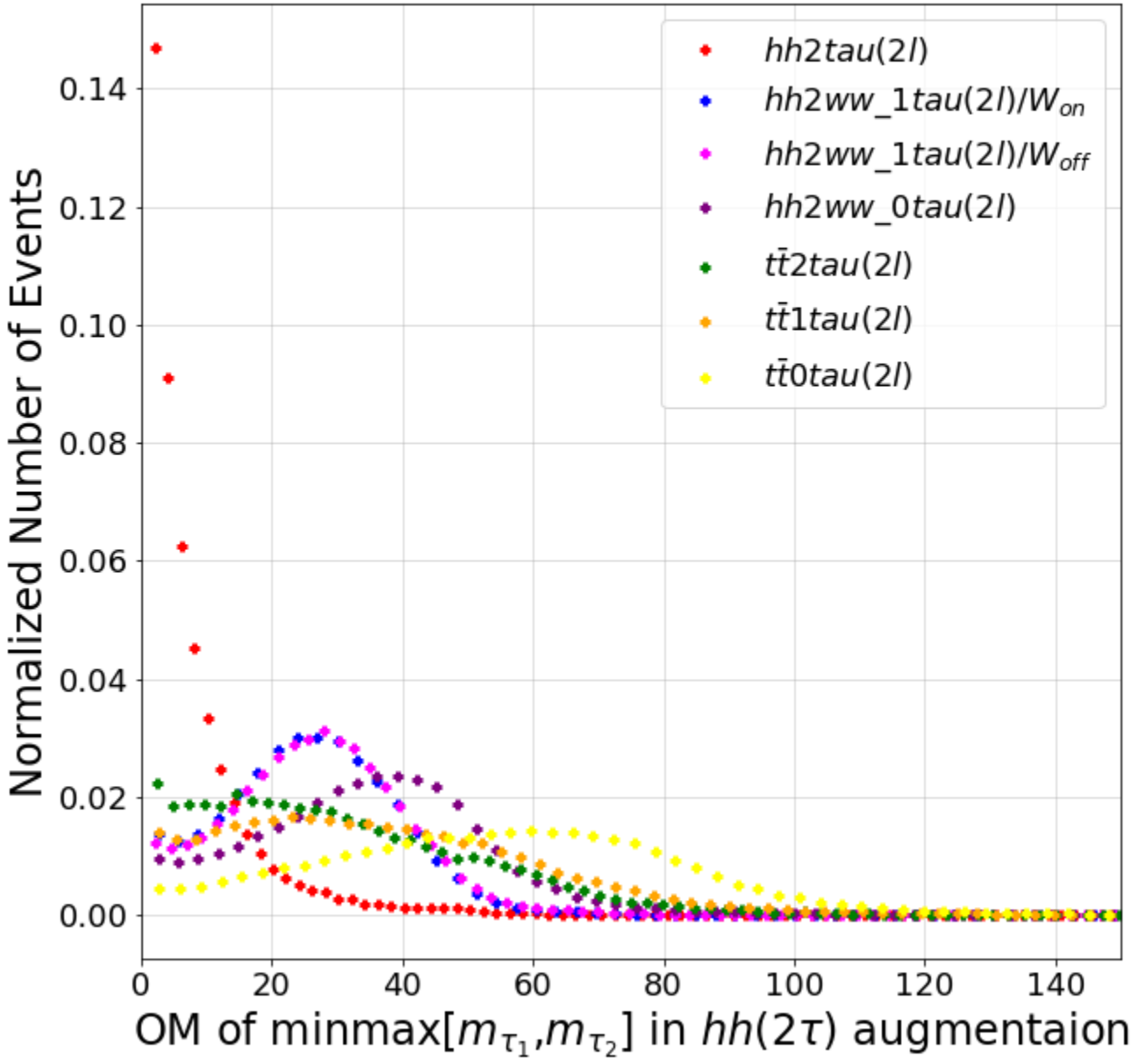
# 1-lepton & 1-hadronic decay tau

**Constraints of Mass**

- t1 = t2
- W1 = 80.4
- W2 = 80.4
- tau1 = 1.77
- tau2 = 1.77



# 2-lepton & 0-hadronic decay tau




**Constraints of Mass**

- H1 (tautau) = 125.
- H2 (bb) = 125.
- Tau1 = Tau2

# Back up slides - OptiMass introduction

- Lagrange multipliers

$$M(\vec{x}^*) \equiv \min_{x \in \mathbb{R}^n} M(\vec{x}) \; s.t \; c_{a=1,\dots,m}(\vec{x}^*) = 0.$$

Minimum value of the function

constraints

$$\mathcal{L}(\vec{x}, \lambda) = M(\vec{x}) - \sum_{a=1}^{m} \lambda_a \, c_a(\vec{x}).$$

-> It does NOT tell us which is the correct minimizer among the N-stationary points!

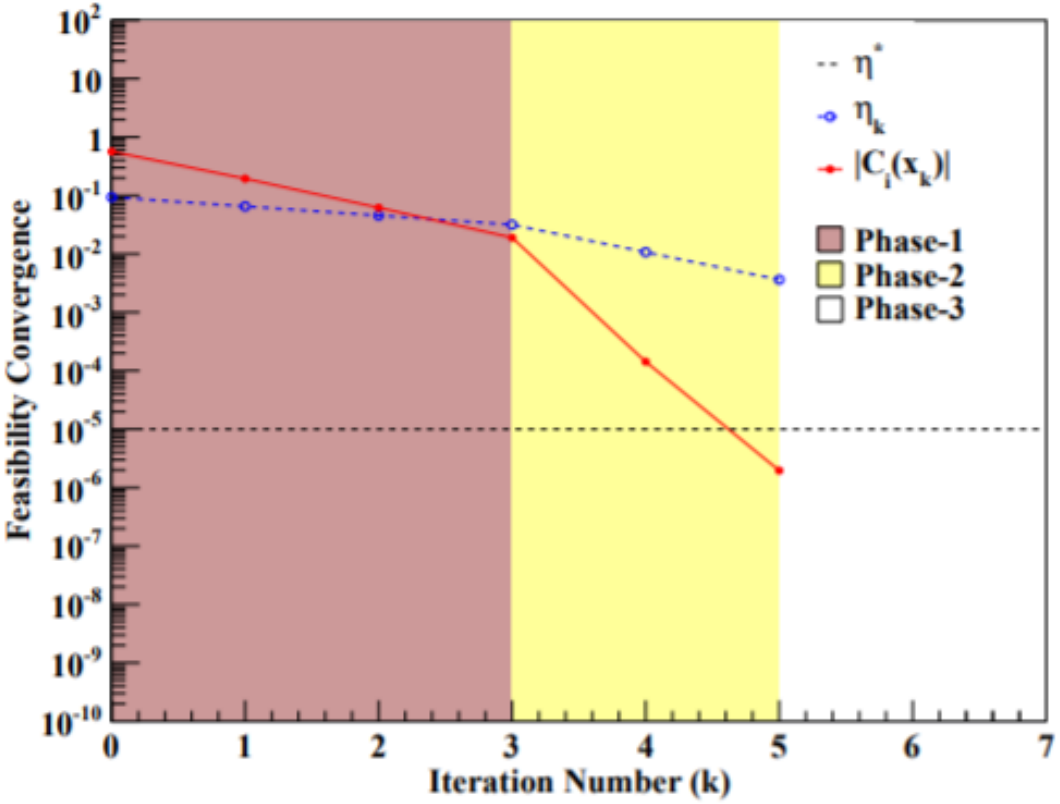
$M = minimized\ mass\ variable\ function$
$\lambda_a = augmented\ Lagrange\ parameter$
$\mu = penalty\ parameter$

- Penalty methods

$$P(\vec{x}, \mu) \equiv M(\vec{x}) + \frac{1}{2\mu} \sum_{a=1} c_a^2(\vec{x}).$$

**OPTIMASS: A Package for the Minimization of Kinematic Mass Functions with Constraints**
- Cho, Won Sang *et al.* JHEP 1601 (2016) 026 arXiv:1508.00589

# Back up slides - OptiMass introduction




- ✓ The evolution of the intermediate feasibility tolerance $\eta^k$
- ✓ The real feasibility $||c_i(x_k)||$
- ✓ The scale set by the ultimate feasibility tolerance $\eta^*$

# Back up slides – OPTIMASS Algorithm Example

**OPTIMASS: A Package for the Minimization of Kinematic Mass Functions with Constraints** - Cho, Won Sang *et al.* JHEP 1601 (2016) 026 arXiv:1508.00589 (pg 17-18)

### 3.2.1 Example one

Our first example involves minimizing the objective function

$$f(x, y) = x + y, \tag{3.30}$$

over the usual plane, $\vec{x} \equiv (x, y)$, subject to the constraint

$$x^2 + y^2 - 1 = 0. \tag{3.31}$$

This constraint implies that our solution must lie on a unit circle centered at the origin. Clearly, the function (3.30) is minimized along the circle at the point

$$(x^*, y^*) = \left( -\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2} \right), \tag{3.32}$$

which is the global minimizer in this example.

The objective function, (3.30), is plotted in the left panel of figure 2. The locus of feasible points (i.e., the unit circle about the origin,) is shown in black. With the Lagrange multiplier method, one adds a Lagrange multiplier term to the objective function as in (2.4)

$$\mathcal{L}(x, y, \lambda) = x + y - \lambda (x^2 + y^2 - 1). \tag{3.33}$$

There are two *stationary points* given by

$$(x^*, y^*, \lambda^*) = \pm\left(\frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}, \frac{\sqrt{2}}{2}\right). \tag{3.34}$$

The Hessian corresponding to the function (3.33) is

$$H_{\mathcal{L}} = \begin{pmatrix} -2\lambda & 0 \\ 0 & -2\lambda \end{pmatrix}, \tag{3.35}$$

and the condition for a minimum (i.e., that $H_{\mathcal{L}}$ should be positive definite) requires us to choose $\lambda < 0$, which selects the correct minimizer among the two stationary points (3.34):

$$(x^*, y^*, \lambda^*) = (-\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}, -\frac{\sqrt{2}}{2}), \tag{3.36}$$

confirming the earlier result (3.32).

We now wish to verify that the OPTIMASS algorithm reproduces this solution. After running the code, we obtain

$$(x^*, y^*; \lambda^*) = (-0.707106, -0.707106; -0.707180), \tag{3.37}$$

which is consistent with (3.36) ($\sqrt{2}/2 = 0.707107...$). We note that this convergence only required five steps, suggesting that the minimum was found relatively easily. The right panel of figure 2 shows a contour plot of the augmented Lagrangian,

$$\tilde{\mathcal{L}}(x, y; \mu_5, \lambda_5) = (x + y) - \lambda_5 (x^2 + y^2 - 1) + \frac{1}{2\mu_5}(x^2 + y^2 - 1)^2 \quad \text{with} \tag{3.38}$$

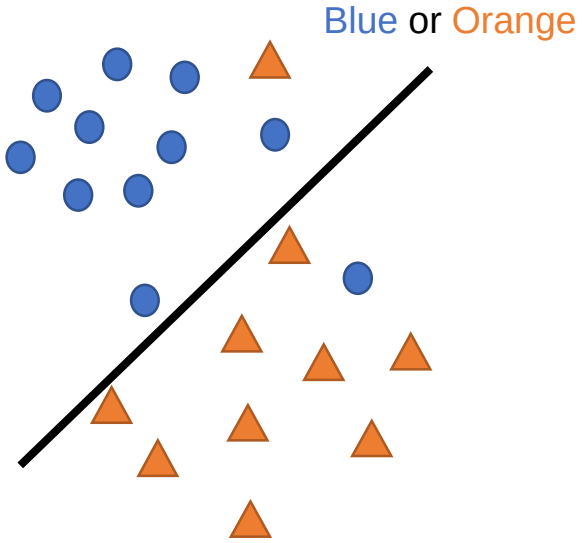
# Summary(Backup)

- **Di-Higgs search in …**
  - 2b + 2-lep
  - 2b + 1-lep + 1-tau_h
  - 2b + 2-tau_h
- **High Level Feature variables for each decay channel**
  - Existing (low level) variables (P_T/deltaR/MT2 …)
  - OPTIMASS variables (om/cd)
  - Around 40~70 variables
- **Using Deep Neural Network**
  - Multi-class Classification
  - Better performance than only using low level features

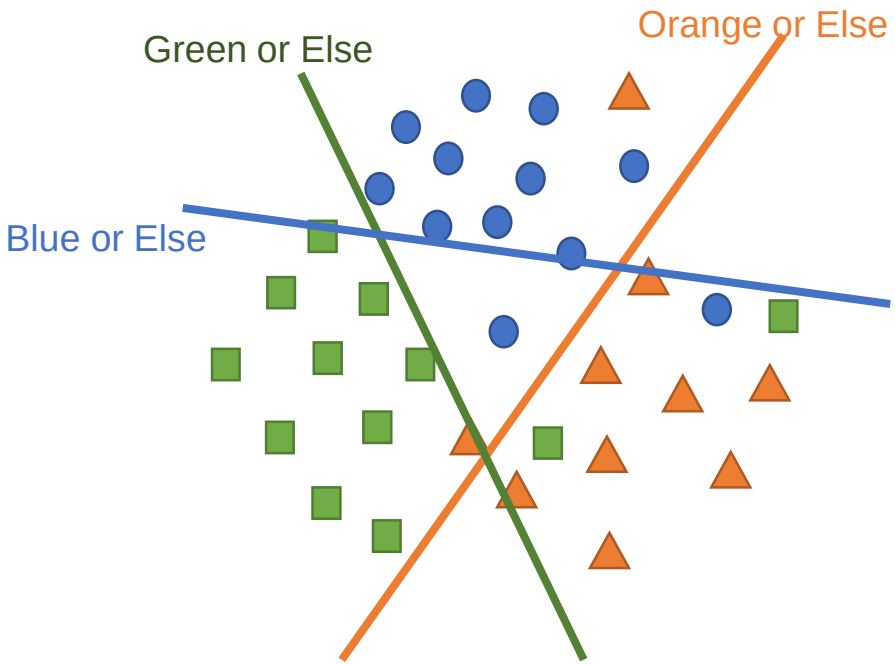
**Use DNN + OPTIMASS Variables!!!**

# Multi-Class Classification

**Binary classification**




**Multi-Class classification**




❖ **Visible : CMS/ATLAS common features**



# Signal vs Background

@ 14TeV, 39.64 fb (HH), 953.6 fb (TT)

| Channel | Leptons | X section | Topology $* \ l = e \ or \ \mu$ |
|---|---|---|---|
| HH2Tau | 0 | ~1.2 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| TT2Tau | 0 | ~5097.2 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ \tau_h\ \tau_h + met$ |
| HH2Tau | 1 | ~1.3 | $hh \rightarrow b\ b\ \tau\ \tau \rightarrow b\ b\ \tau_h\ l + met$ |
| HH2WW*W1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w \rightarrow b\ b\ l\ l + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW*1Tau | 2 | ~0.08 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| HH2WW0Tau | 2 | ~0.47 | $hh \rightarrow b\ b\ w\ w^* \rightarrow b\ b\ l\ l + met$ |
| TT2Tau | 2 | ~1508.7 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ \tau + met \rightarrow b\ b\ l\ l + met$ |
| TT1Tau | 2 | ~16158.3 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ \tau\ l + met \rightarrow b\ b\ l\ l + met$ |
| TT0Tau | 2 | ~43263.9 | $\bar{t}t \rightarrow b\ w\ b\ w \rightarrow b\ b\ l\ l + met$ |

**Too Many invisible particles from each distinctive/complicated decay topologies**