DM models with dark gauge interactions

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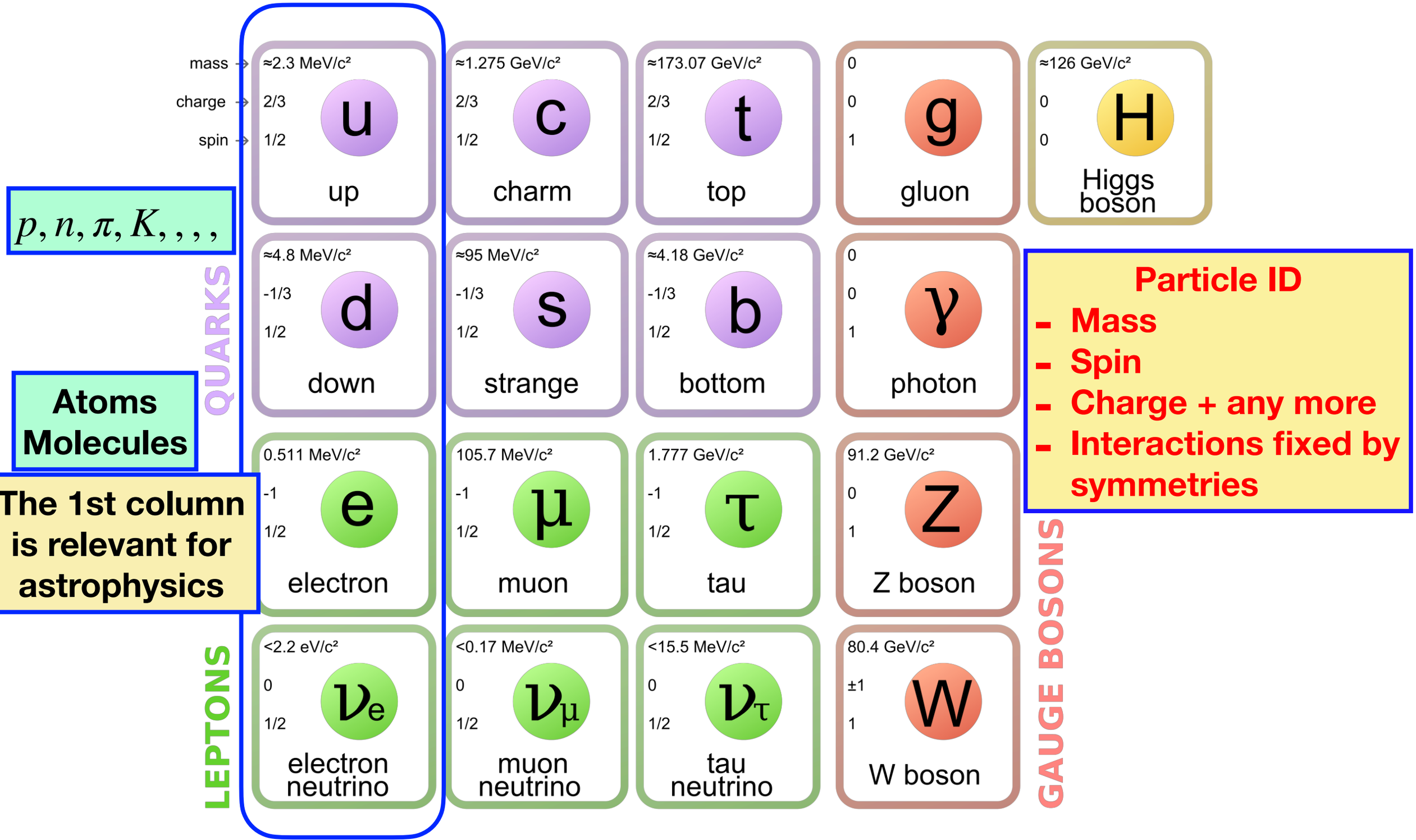
Contents

- SM for particle physics
- DM Overview
  - Particle physics approach based on Quantum Field Theory : global vs. local gauge symmetry for DM stability or longevity
  - Key issues: unitarity and renormalizability, gauge invariance (both SM and dark gauge symmetries)
  - Particle physics + Cosmology : DR, Inflation, H_0 , σ_8 , etc.

Periodic Table for Fundamental Particles



SM for particle physics

$$\mathcal{L}_{MSM} = -\frac{1}{2g_s^2}\mathrm{Tr}G_{\mu\nu}G^{\mu\nu} - \frac{1}{2g^2}\mathrm{Tr}W_{\mu\nu}W^{\mu\nu}$$
$$-\frac{1}{4g'^2}B_{\mu\nu}B^{\mu\nu} + i\frac{\theta}{16\pi^2}\mathrm{Tr}G_{\mu\nu}\tilde{G}^{\mu\nu} + M_{Pl}^2 R$$
$$+|D_\mu H|^2 + \bar{Q}_i i\not{D} Q_i + \bar{U}_i i\not{D} U_i + \bar{D}_i i\not{D} D_i$$
$$+\bar{L}_i i\not{D} L_i + \bar{E}_i i\not{D} E_i - \frac{\lambda}{2}\left(H^\dagger H - \frac{v^2}{2}\right)^2$$
$$-\left(h_u^{ij} Q_i U_j \tilde{H} + h_d^{ij} Q_i D_j H + h_l^{ij} L_i E_j H + c.c.\right). (1)$$

Renormalizable part

+ ∞ # of higher dim (nonrenormalizable) operators (why neutrinos are light, proton lives very very long)

QFT + conservation laws (symmetries):

- $E, \vec{p}, \vec{J}$ + Special Relativity : Poincare sym
- Exact charge conservation : local gauge sym

QED Contributions

$a_\mu^{QED} = (1/2)(\alpha/\pi)$ Schwinger 1948

$+ \; 0.765857426\,(16)\,(\alpha/\pi)^2$

Sommerfield; Petermann; Suura&Wichmann ’57; Elend ’66; MP ’04

$+ \; 24.05050988\,(28)\,(\alpha/\pi)^3$

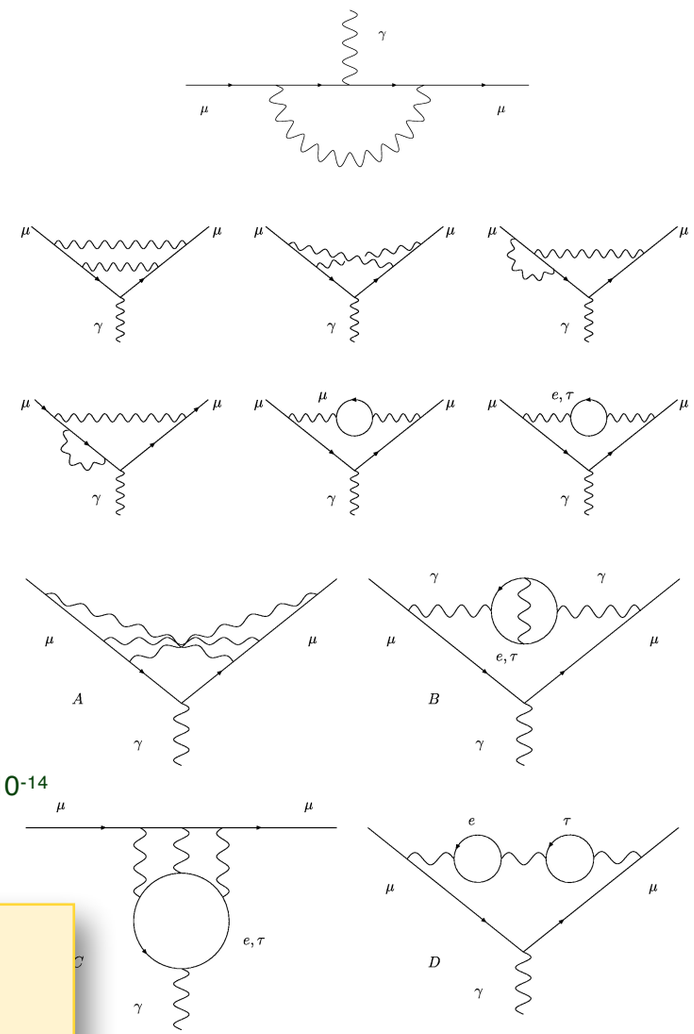
Remiddi, Laporta, Barbieri … ; Czarnecki, Skrzypek ’99; MP ’04;
Friot, Greynat & de Rafael ’05, Ananthanarayan, Friot, Ghosh 2020

$+ \; 130.8780\,(60)\,(\alpha/\pi)^4$

Kinoshita & Lindquist ’81, … , Kinoshita & Nio ’04, ’05;
Aoyama, Hayakawa,Kinoshita & Nio, 2007, Kinoshita et al. 2012 & 2015;
Steinhauser et al. 2013, 2015 & 2016 (all electron & τ loops, analytic);
Laporta, PLB 2017 (mass independent term) COMPLETED²!

$+ \; 750.86\,(88)\,(\alpha/\pi)^5$ COMPLETED!

Kinoshita et al. ‘90, Yelkhovsky, Milstein, Starshenko, Laporta,…
Aoyama, Hayakawa, Kinoshita, Nio 2012, 2015, 2017 & 2019.
Volkov 1909.08015: $A_1^{(10)}$[no lept loops] at variance, but negligible $\delta a_\mu \sim 6\times10^{-14}$



Adding up, we get:

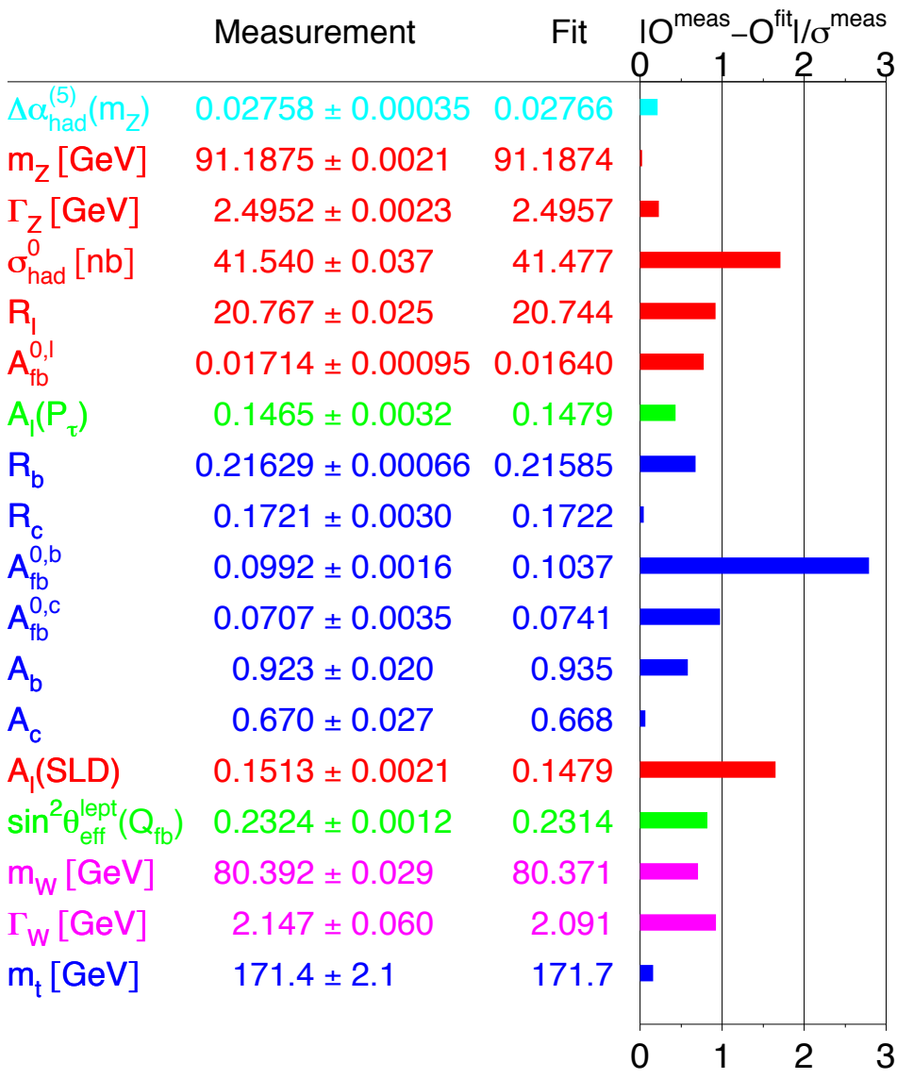
$a_\mu^{QED} = 116584718.931\,(19)(100)(23) \times 10^{-11}$

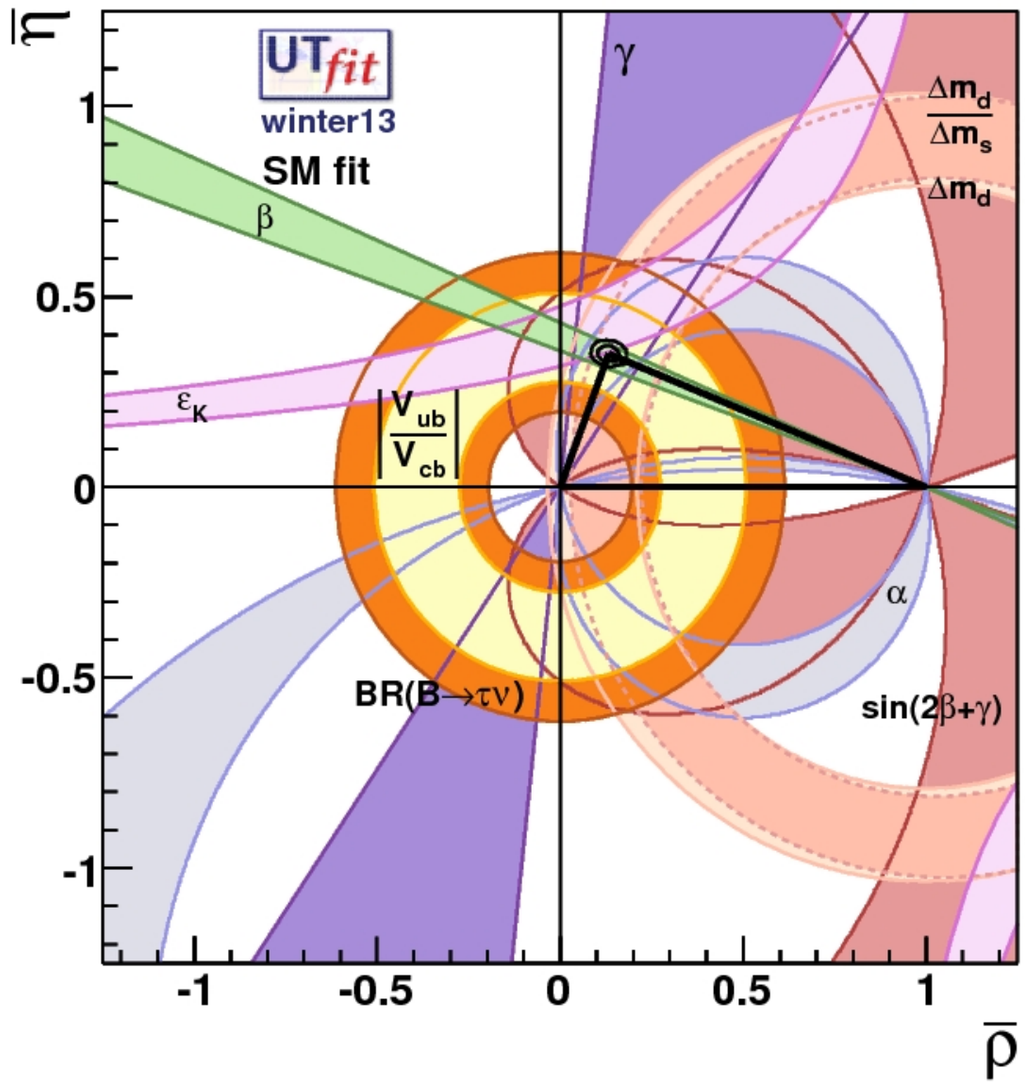
mainly from 4-loop coeff. unc. 6-loop from α(Cs)

α = 1/137.035999046(27) [0.2ppb] Parker et al 2018 WP20 value

Shift down in $a_\mu^{QED} \sim 1.4 \times 10^{-12}$ with new LKB Paris α(Rb) value (Morel et al 2020)

EWPT & CKM

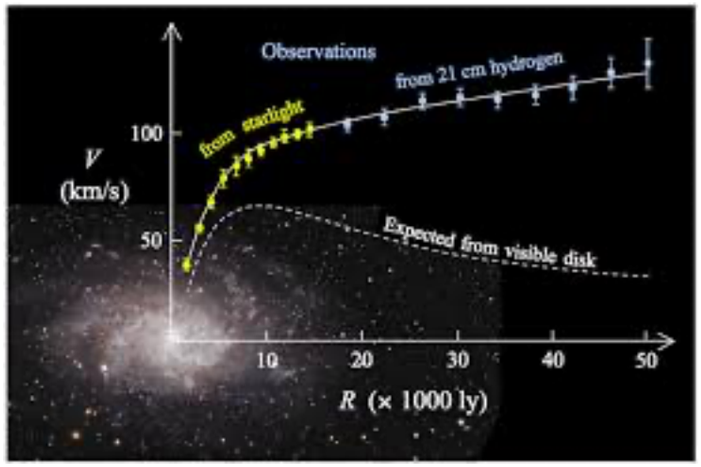


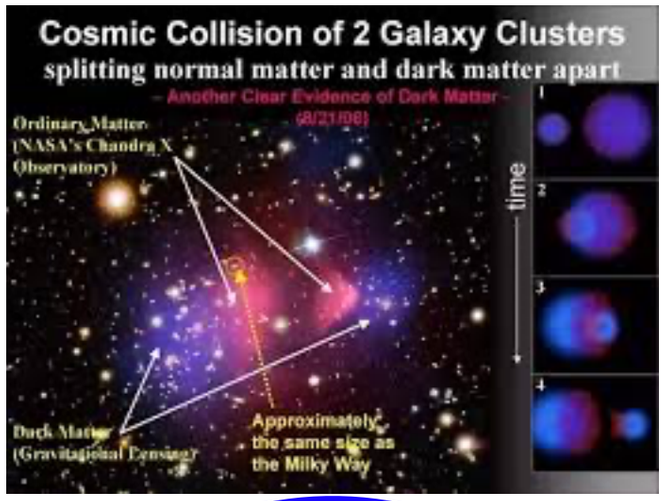


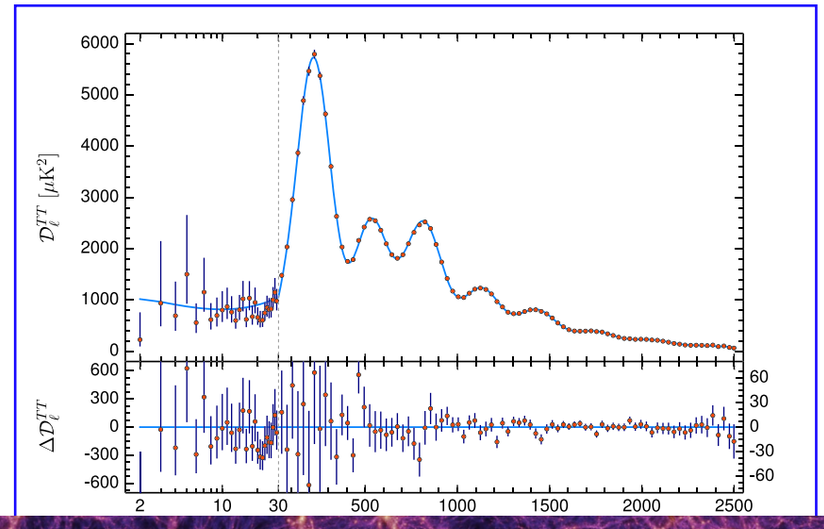
Almost Perfect & No New Physics @ LHC !

DM Overview

Evidences for DM

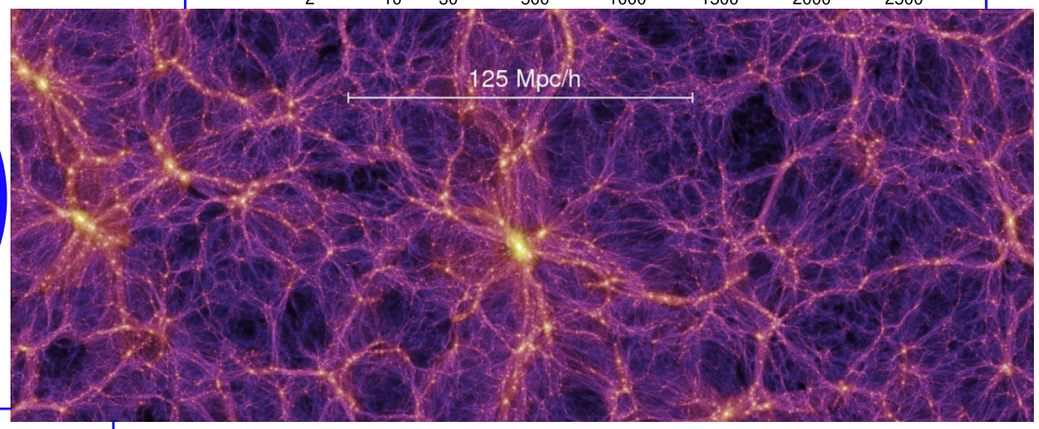


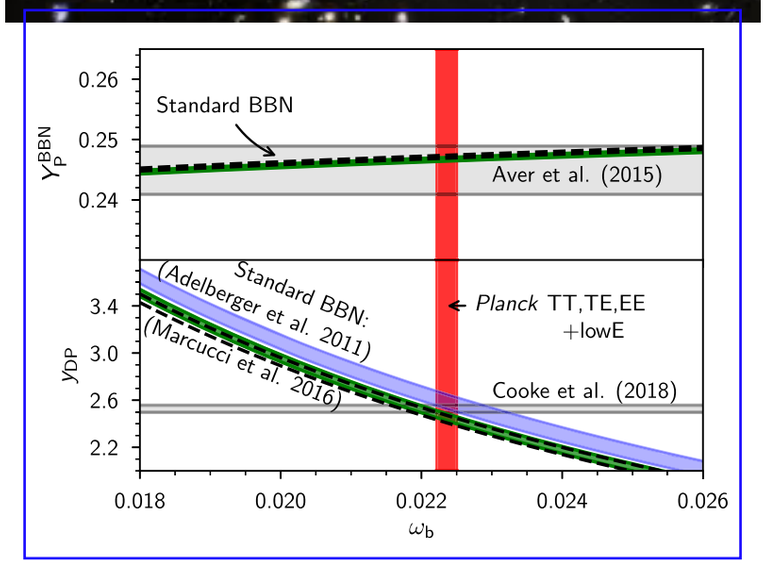


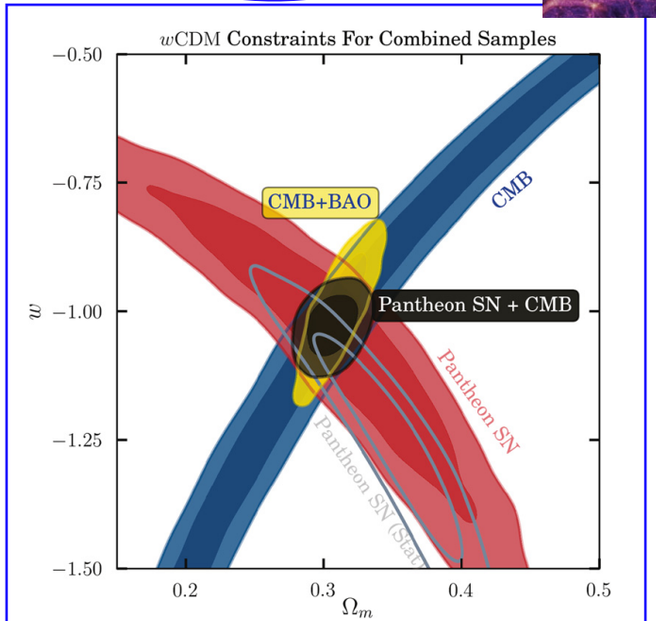


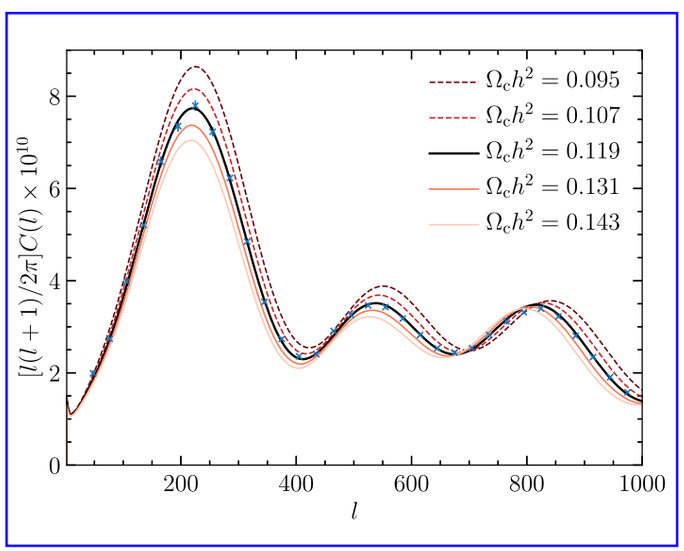


GRAVITY

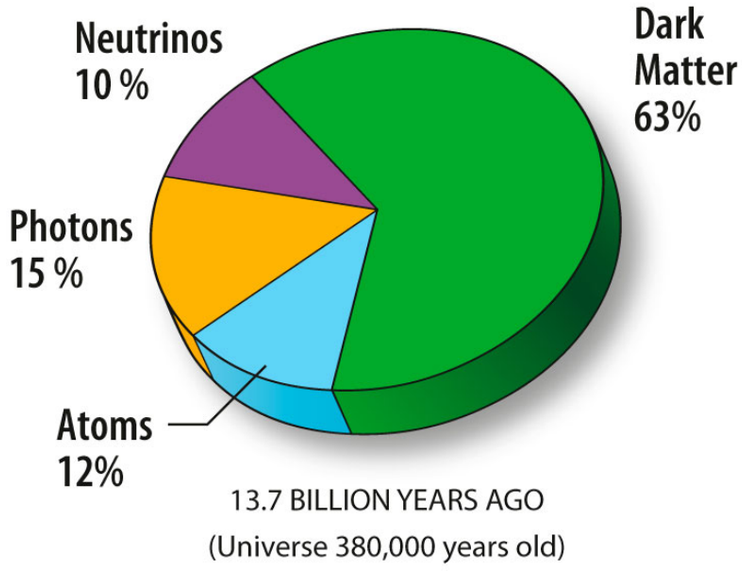


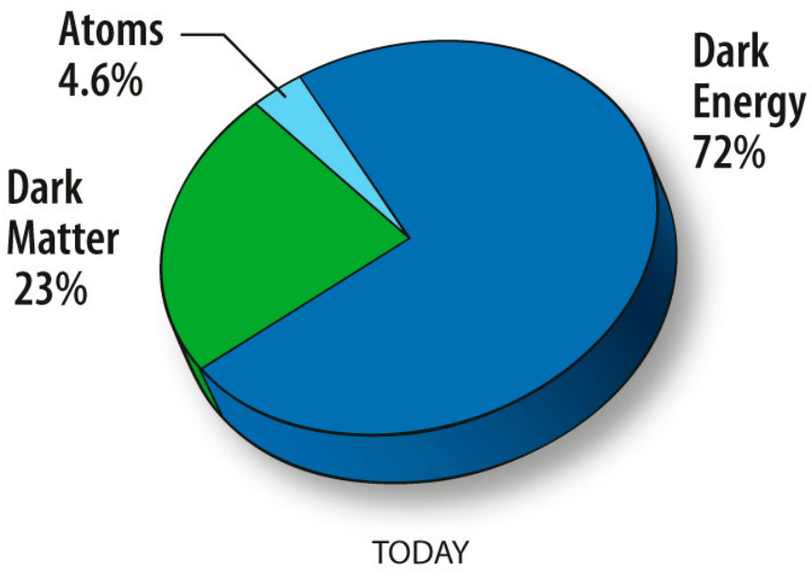


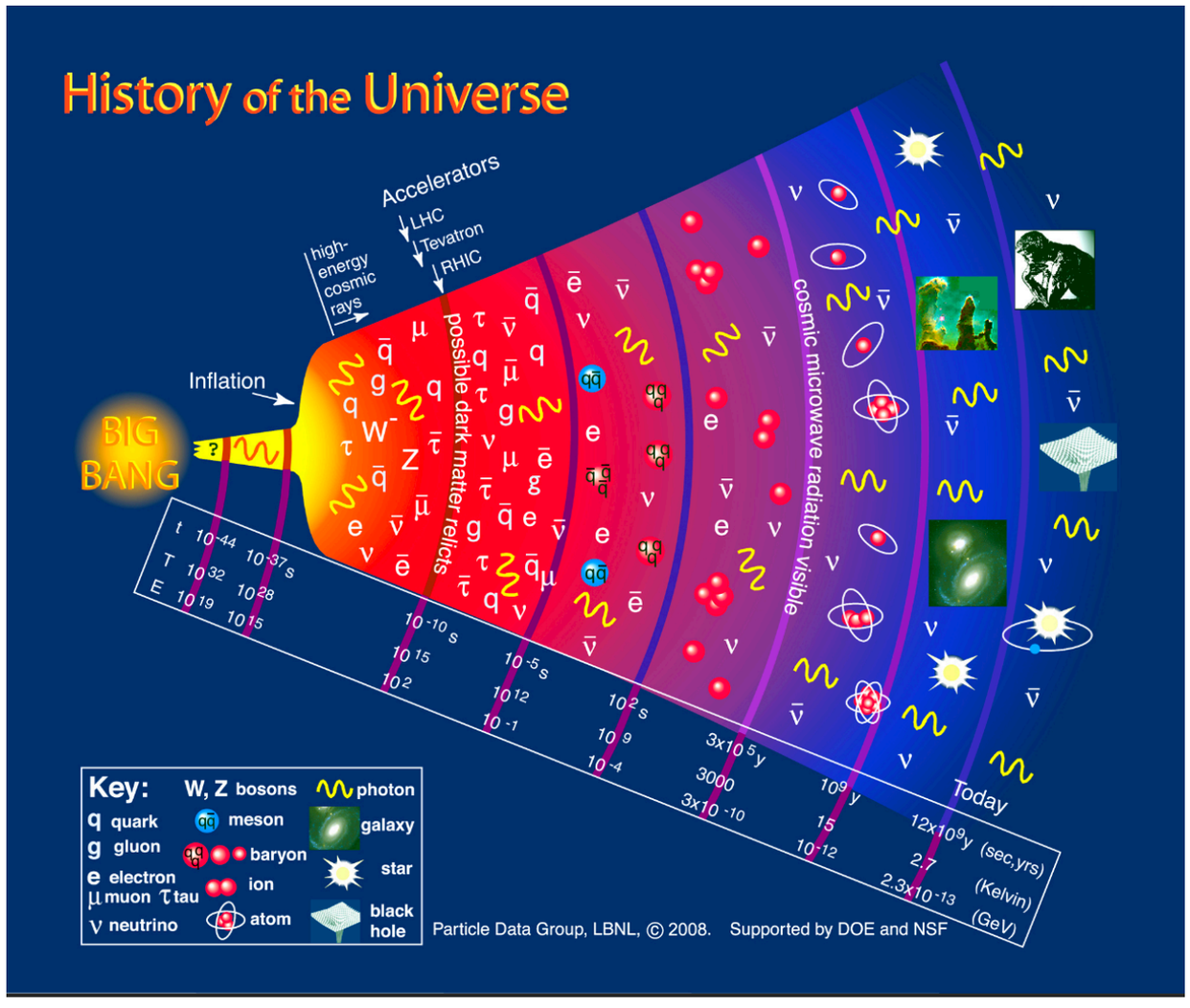




Cos. Concordance Model







KNOWNS

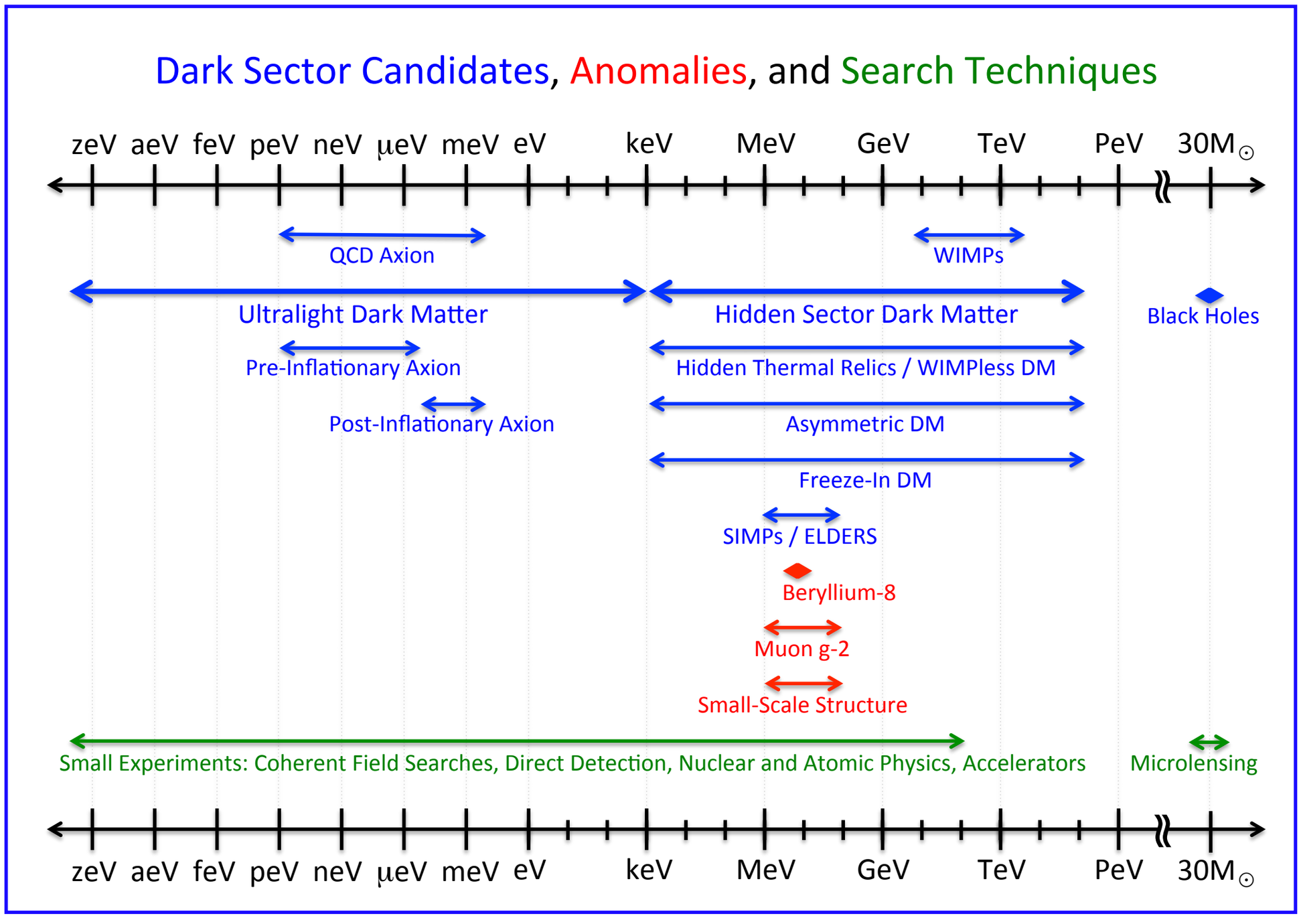
- Feels Gravity > Currently evidences come only thru this
- Its lifetime >> Age of Universe
- $\rho(\simeq m) \gg \ p(\simeq 0)$ (Nonrel.)
- $\Omega_{\rm DM} \sim 5\ \Omega_{\rm Baryon}$
- $\rho_{\rm local} \sim 0.3 {\rm GeV/cm}^3$
- It forms a halo, not a disk

UNKNOWNS

- Mass, Spin ?
- How many species ?
- Any internal quantum #'s ?
- Any internal structures ?
- Interactions w/ SM particles ?
- DM self int. ? ($\sigma_{\chi\chi}/m_\chi \lesssim 1 g/cm^2$)
- Almost nothing known about particle physics nature of DM

Domestic Activities (Th)

[US Cosmic Visions:…., arXiv:1707.04591]



Portals to DM

- Higgs portal : $H^\dagger HS,\ H^\dagger HS^2,\ H^\dagger H\phi^\dagger\phi$

ϕ : Dark Scalars

- U(1) Vector portal : $\epsilon B_{\mu\nu}X^{\mu\nu}$

X_μ : Dark photon

- Neutrino portal : $\overline{N_R}(\widetilde{H}l_L+\phi^\dagger\psi)$

ψ : Dark fermion
~ Sterile ν

- (Dark) Axion portal (HSLee et al)
- So on & on & on …
- Eventually “Portal” is what we observe in the experiments

Portals to DM

- Higgs portal : $H^\dagger H S,\ H^\dagger H S^2,\ H^\dagger H \phi^\dagger \phi$
- U(1) Vorta
- Neutrino portal : $\overline{N_R}(\widetilde{H} l_L +$
- (Dark) Axion portal (HSLee
- So on, & on & on , …
- Eventually “Portal” is what we observe in experiments

Singlet Portals to Dark sector w/ local dark gauge sym
(Baek, Park, Ko, arXiv:1303.4280 [hep-ph])

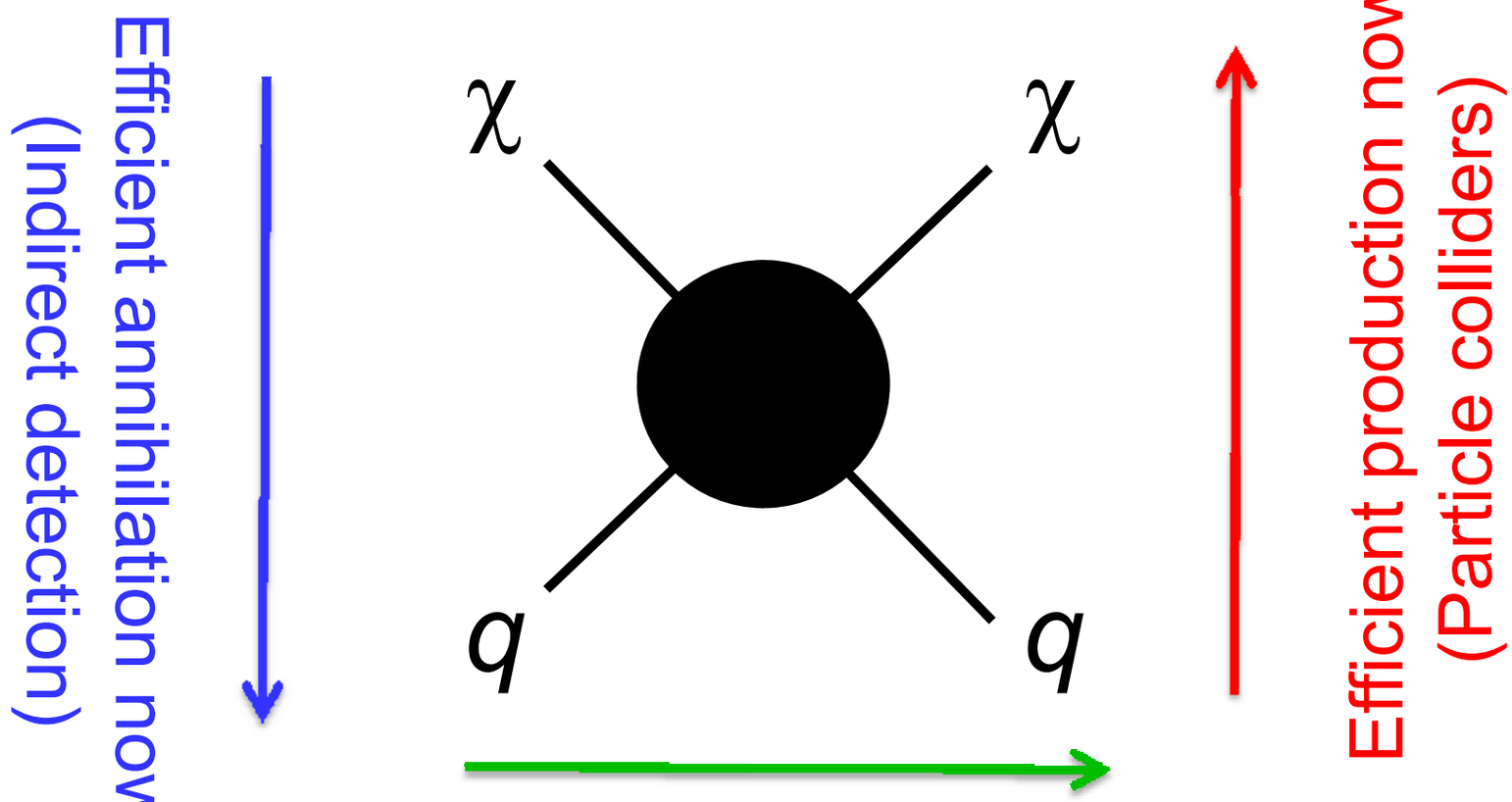
DM stability is guaranteed by
Local gauge symmetry
OR
DM longevity is gauranteed by
Accidental global sym

Search for WIMP

- Direct Detections
- Indirect Detections (Current Universe, Early Universe)
- Collider Searches
- Quantum Force and search for the 5th force
- DM EFT/Simplified model : Not good for collider searches
  $\longrightarrow$ Dark Higgs is important !
- Theoretical consistency (unitarity, gauge invariance, renornalizabiyity) important for DM model buildings

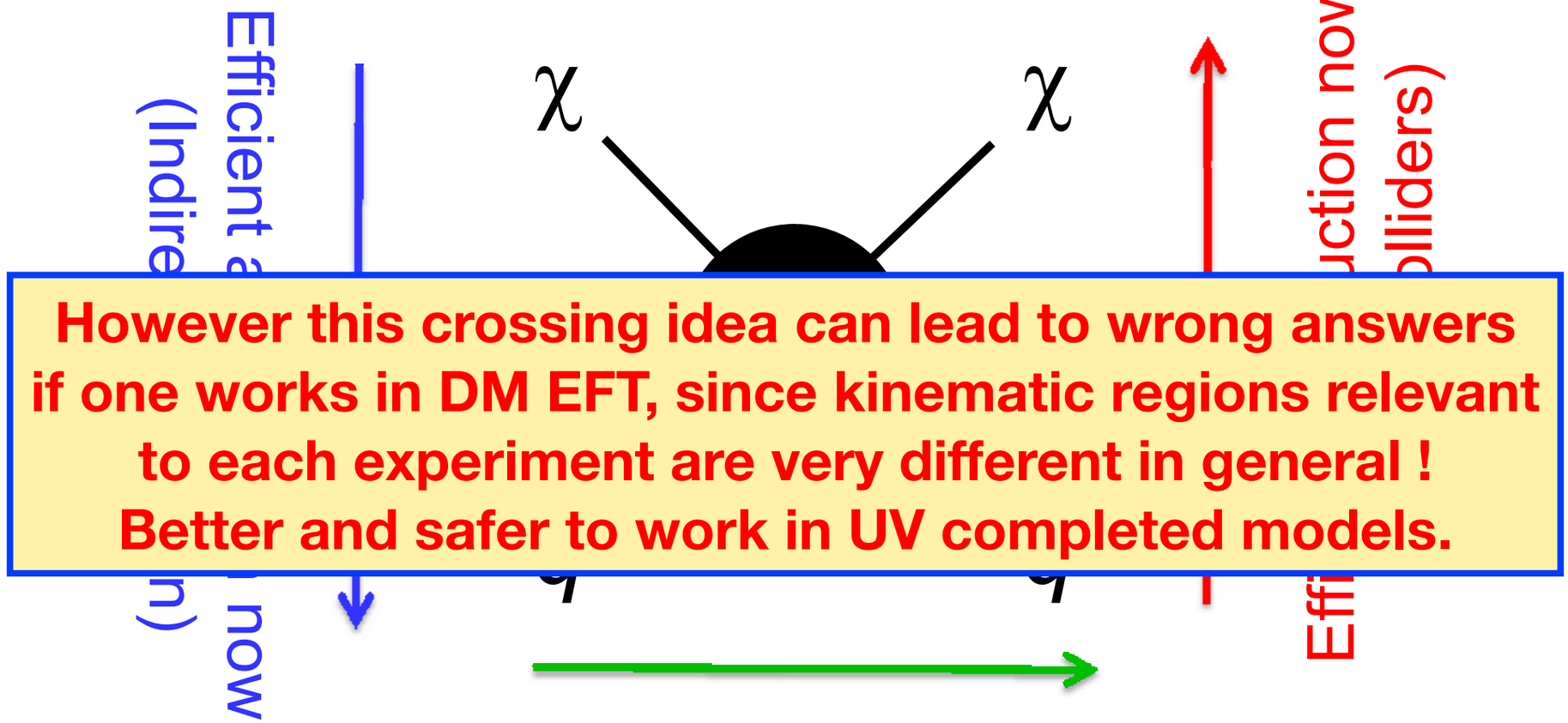
Crossing & WIMP detection

Correct relic density → Efficient annihilation then



Crossing & WIMP detection

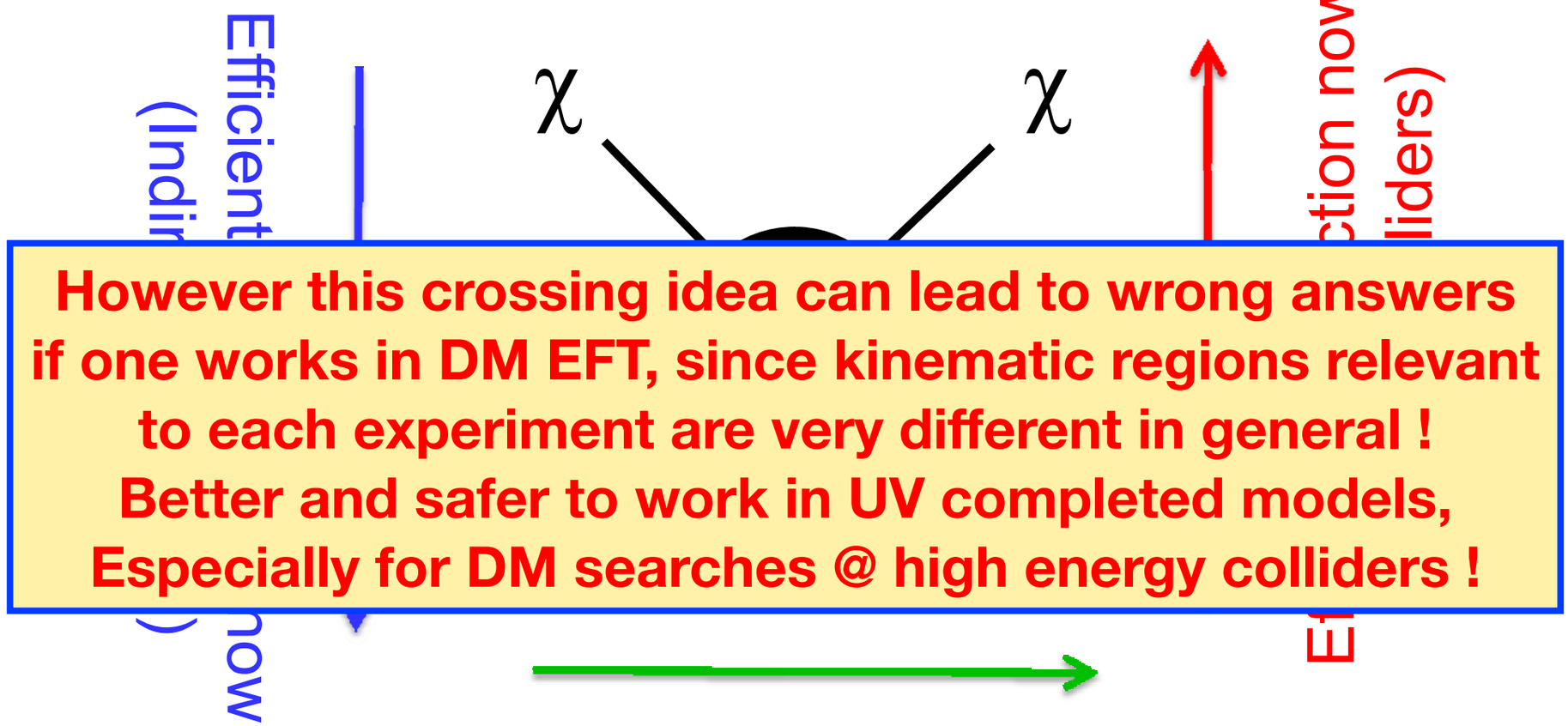
Correct relic density → Efficient annihilation then



However this crossing idea can lead to wrong answers if one works in DM EFT, since kinematic regions relevant to each experiment are very different in general ! Better and safer to work in UV completed models.

Efficient scattering now
(Direct detection)

Furthermore one can consider on-shell mediators, dark radiation and inelastic DM, etc..



However this crossing idea can lead to wrong answers if one works in DM EFT, since kinematic regions relevant to each experiment are very different in general !
Better and safer to work in UV completed models, Especially for DM searches @ high energy colliders !

Dark sector parameter space for a fixed m_{DM}

m_{DM}/m_{ϕ}

$\chi + \chi \to \phi + \phi$

P-wave annihilation
For fermion DM χ

1

$\chi + \chi \to \phi + \gamma'$

P-wave annihilation
For scalar DM χ

$\chi + \chi \to \phi + \gamma'$

Higgs Portal DM
Along the y-axis

These two channels are possible for light DM,
only if we include dark Higgs boson !

1/2

$\chi + \chi \to \mathrm{SM} + \mathrm{SM}$

$\chi + \chi \to \gamma' + \gamma'$

0

1/2

1

$m_{DM}/m_{\gamma'}$

DM EFT, including
Higgs portal DM EFT

Models w/o dark Higgs
Along the x-axis

χ : dark matter
γ' : dark photon
ϕ : dark Higgs

Dark Gauge Symmetry

Z2 real scalar DM

- Simplest DM model with Z2 symmetry : $S \to -S$

$$\mathcal{L} = \frac{1}{2}\partial_\mu S \partial^\mu S - \frac{1}{2}m_S^2 S^2 - \frac{\lambda_S}{4!}S^4 - \frac{\lambda_{SH}}{2}S^2 H^\dagger H.$$

- Global Z2 could be broken by gravity effects (higher dim operators)

- e.g. consider Z2 breaking dim-5 op : $\frac{1}{M_{\text{Planck}}} S O^{(4)}_{\text{SM}}$

- Lifetime of EW scale mass “S” is too short to be a DM

- Similarly for singlet fermion DM

Fate of CDM with Z_2 sym

(Baek,Ko,Park,arXiv:1303.4280)

Consider Z_2 breaking operators such as

$$\frac{1}{M_{\rm Planck}} S O_{\rm SM}$$

keeping dim-4 SM operators only

The lifetime of the Z_2 symmetric scalar CDM S is roughly given by

$$\Gamma(S) \sim \frac{m_S}{M^2_{\rm Planck}} \sim (\frac{m_S}{100{\rm GeV}}) 10^{-37} GeV$$

- Global Z2 cannot save EW scale DM from decay with long enough lifetime

The lifetime is too short for ~100 GeV DM

Fate of CDM with Z_2 sym

Spontaneously broken local U(1)x can do the job to some extent, but there is still a problem

Let us assume a local $U(1)_X$ is spontaneously broken by $\langle \phi_X \rangle \neq 0$ with

$$Q_X(\phi_X) = Q_X(X) = 1$$

Then, there are two types of dangerous operators:

$\phi_X^\dagger X H^\dagger H$, and $\phi_X^\dagger X O_{\rm SM}^{(dim-4)}$

Problematic !

Perfectly fine !

Higgs is not good for DM stability/longvity

- These arguments will apply to DM models based on ad hoc symmetries (Z_2,Z_3 etc.)

- One way out is to implement Z_2 symmetry as local U(1) symmetry (arXiv:1407.6588 with Seungwon Baek and Wan-Il Park);

- See a paper by Ko and Tang on local Z_3 scalar DM, and another by Ko, Omura and Yu on inert 2HDM with local $U(1)_H$

- DM phenomenology richer and DM stability/ longevity on much solider ground

arXiv:1407.6588 w/ WIPark and SBaek

$$Q_X(\phi) = 2, \quad Q_X(X) = 1$$

$$\mathcal{L} = \mathcal{L}_{\rm SM} + -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} - \frac{1}{2}\epsilon X_{\mu\nu}B^{\mu\nu} + D_\mu\phi_X^\dagger D^\mu\phi_X - \frac{\lambda_X}{4}\left(\phi_X^\dagger\phi_X - v_\phi^2\right)^2 + D_\mu X^\dagger D^\mu X - m_X^2 X^\dagger X$$
$$- \frac{\lambda_X}{4}\left(X^\dagger X\right)^2 - \left(\mu X^2\phi^\dagger + H.c.\right) - \frac{\lambda_{XH}}{4}X^\dagger X H^\dagger H - \frac{\lambda_{\phi_X H}}{4}\phi_X^\dagger\phi_X H^\dagger H - \frac{\lambda_{XH}}{4}X^\dagger X\phi_X^\dagger\phi_X$$

The lagrangian is invariant under $X \to -X$ even after $U(1)_X$ symmetry breaking.

Unbroken Local Z2 symmetry
Gauge models for excited DM

$X_R \to X_I\gamma_h^*$ followed by $\gamma_h^* \to \gamma \to e^+e^-$ **etc.**

The heavier state decays into the lighter state

The local Z2 model is not that simple as the usual
Z2 scalar DM model (also for the fermion CDM)

Local dark gauge symmetry

- Better to use local gauge symmetry for DM stability
  (Baek,Ko,Park,arXiv:1303.4280)

- Success of the Standard Model of Particle Physics lies in "local gauge symmetry" without imposing any internal global symmetries
- Electron stability : U(1)em gauge invariance, electric charge conservation, massless photon
- Proton longevity : baryon # is an accidental sym of the SM
- No gauge singlets in the SM ; all the SM fermions chiral

- Dark sector with (excited) dark matter, dark radiation and force mediators might have the same structure as the SM
- "Chiral dark gauge theories without any global sym"
- Origin of DM stability/longevity from dark gauge sym, and not from dark global symmetries, as in the SM
- Just like the SM (conservative)

In QFT,

- DM could be absolutely stable due to unbroken local gauge symmetry (DM with local Z_2, Z_3 etc.) or topology (hidden sector monopole + vector DM + dark radiation)
- Longevity of DM could be due to some accidental symmetries (hidden sector pions and baryons)
- Kinematically long-lived if DM is very light (axion, sterile ν_s , etc..)

Higgs Portal DM : EFT vs. UV completions

$\Gamma_{\rm inv}(H \to VV)$ for $m_V \to 0$

arXiv: 2112.11983, PRD 105 (2022) 015007,with S. Baek, W.I. Park
And references therein by P. Ko et al

Higgs portal DM models

$$\mathcal{L}_{\rm scalar} = \frac{1}{2}\partial_\mu S \partial^\mu S - \frac{1}{2}m_S^2 S^2 - \frac{\lambda_{HS}}{2} H^\dagger H S^2 - \frac{\lambda_S}{4} S^4$$

$$\mathcal{L}_{\rm fermion} = \overline{\psi}\left[i\gamma\cdot\partial - m_\psi\right]\psi - \frac{\lambda_{H\psi}}{\Lambda} H^\dagger H\ \overline{\psi}\psi$$

$$\mathcal{L}_{\rm vector} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{1}{2}m_V^2 V_\mu V^\mu + \frac{1}{4}\lambda_V (V_\mu V^\mu)^2 + \frac{1}{2}\lambda_{HV} H^\dagger H V_\mu V^\mu.$$

All invariant under ad hoc Z2 symmetry

arXiv:1112.3299, … 1402.6287, etc.

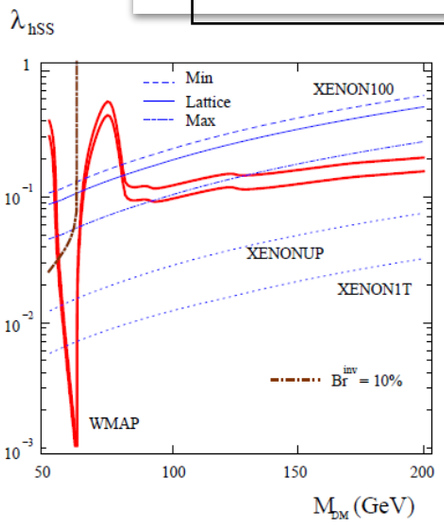


FIG. 1. Scalar Higgs-portal parameter space allowed by WMAP (between the solid red curves), XENON100 and $\mathrm{BR}^{\rm inv} = 10\%$ for $m_h = 125$ GeV. Shown also are the prospects for XENON upgrades.

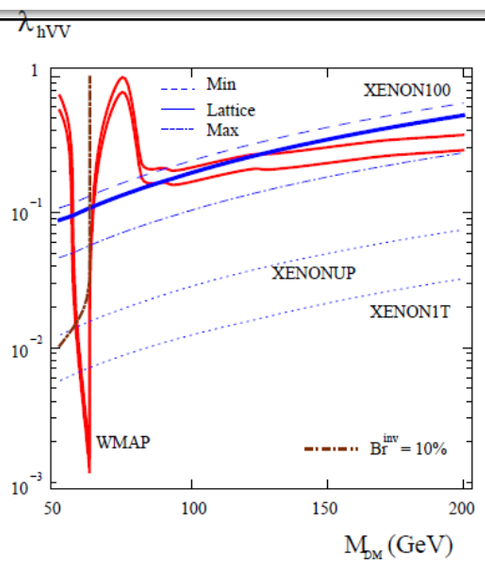


FIG. 2. Same as Fig. 1 for vector DM particles.

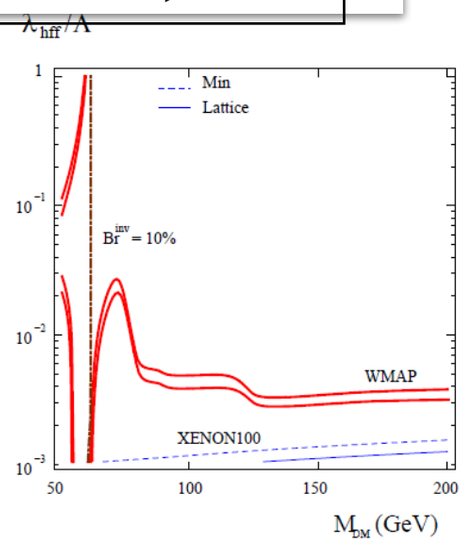


FIG. 3. Same as in Fig.1 for fermion DM; λ_{hff}/Λ is in GeV^{-1}.

Higgs portal DM as examples

$$\mathcal{L}_{\rm scalar} = \frac{1}{2}\partial_\mu S \partial^\mu S - \frac{1}{2}m_S^2 S^2 - \frac{\lambda_{HS}}{2} H^\dagger H S^2 - \frac{\lambda_S}{4} S^4$$

$$\mathcal{L}_{\rm fermion} = \overline{\psi}\left[i\gamma\cdot\partial - m_\psi\right]\psi - \frac{\lambda_{H\psi}}{\Lambda} H^\dagger H\ \overline{\psi}\psi$$

$$\mathcal{L}_{\rm vector} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + \frac{1}{2}m_V^2 V_\mu V^\mu + \frac{1}{4}\lambda_V (V_\mu V^\mu)^2 + \frac{1}{2}\lambda_{HV} H^\dagger H V_\mu V^\mu .$$

All invariant under ad hoc Z2 symmetry

arXiv:1112.3299, … 1402.6287, etc. | And Revived recent papers

We need to include dark Higgs or singlet scalar to get renormalizable/unitary models for Higgs portal singlet fermion or vector DM

[NB: UV Completions : Not unique]

$m_h = 125$ GeV. Shown also are the prospects for XENON upgrades.

FIG. 2. Same as Fig. 1 for vector DM particles.

FIG. 3. Same as in Fig.1 for fermion DM; λ_{hff}/Λ is in GeV^{-1}.

Models for HP SFDM & VDM

UV Completion of HP Singlet Fermion DM (SFDM)

$$
\begin{aligned}
\mathcal{L} &= \mathcal{L}_{\rm SM} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H \\
&\quad + \frac{1}{2}(\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu_S^3 S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4 \\
&\quad + \overline{\psi}(i \not{\partial} - m_{\psi_0})\psi - \lambda S \overline{\psi}\psi
\end{aligned}
$$

UV Completion of HP VDM

$$
\begin{aligned}
\mathcal{L}_{VDM} = & -\frac{1}{4} X_{\mu\nu} X^{\mu\nu} + (D_\mu \Phi)^\dagger (D^\mu \Phi) - \frac{\lambda_\Phi}{4} \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2} \right)^2 \\
& - \lambda_{H\Phi} \left(H^\dagger H - \frac{v_H^2}{2} \right) \left(\Phi^\dagger \Phi - \frac{v_\Phi^2}{2} \right) \ ,
\end{aligned}
$$

- **The simplest UV completions in terms of # of new d.o.f.**
- **At least, 2 more parameters, (m_ϕ , $\sin\alpha$) for DM physics**

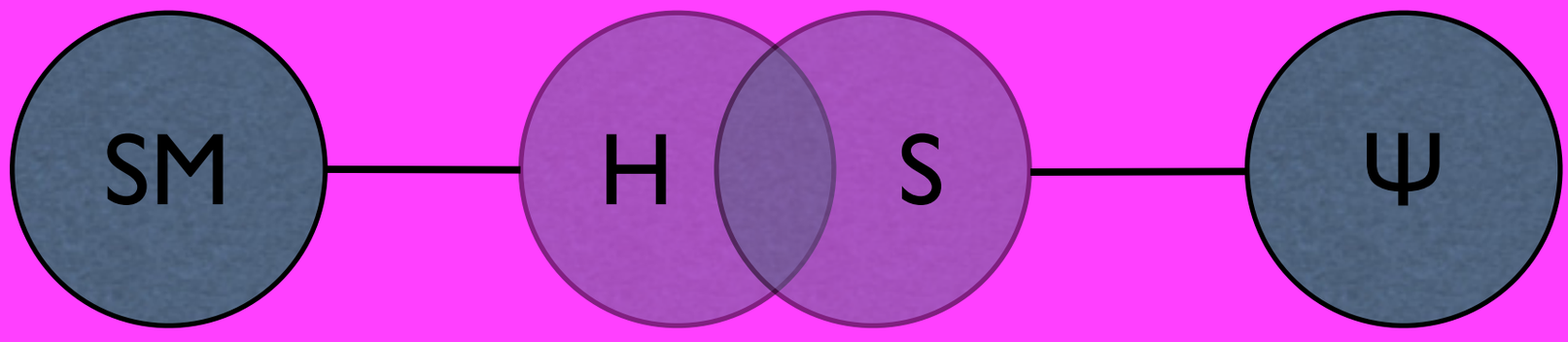
UV Completion for HP FDM

Baek, Ko, Park, arXiv:1112.1847

$$\begin{aligned}\mathcal{L} &= \mathcal{L}_{\rm SM} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H \\ &+ \frac{1}{2}(\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu_S^3 S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4 \\ &+ \overline{\psi}(i \not{\partial} - m_{\psi_0})\psi - \lambda S \overline{\psi}\psi\end{aligned}$$

mixing

invisible decay



Production and decay rates are suppressed relative to SM.

Higgs-Singlet Mixing

- Mixing and Eigenstates of Higgs-like bosons

$$\mu_H^2 = \lambda_H v_H^2 + \mu_{HS} v_S + \frac{1}{2}\lambda_{HS} v_S^2,$$

$$m_S^2 = -\frac{\mu_S^3}{v_S} - \mu_S' v_S - \lambda_S v_S^2 - \frac{\mu_{HS} v_H^2}{2 v_S} - \frac{1}{2}\lambda_{HS} v_H^2,$$

at vacuum

$$M^2_{\text{Higgs}} \equiv \begin{pmatrix} m^2_{hh} & m^2_{hs} \\ m^2_{hs} & m^2_{ss} \end{pmatrix} \equiv \begin{pmatrix} \cos\alpha & \sin\alpha \\ -\sin\alpha & \cos\alpha \end{pmatrix} \begin{pmatrix} m_1^2 & 0 \\ 0 & m_2^2 \end{pmatrix} \begin{pmatrix} \cos\alpha & -\sin\alpha \\ \sin\alpha & \cos\alpha \end{pmatrix}$$

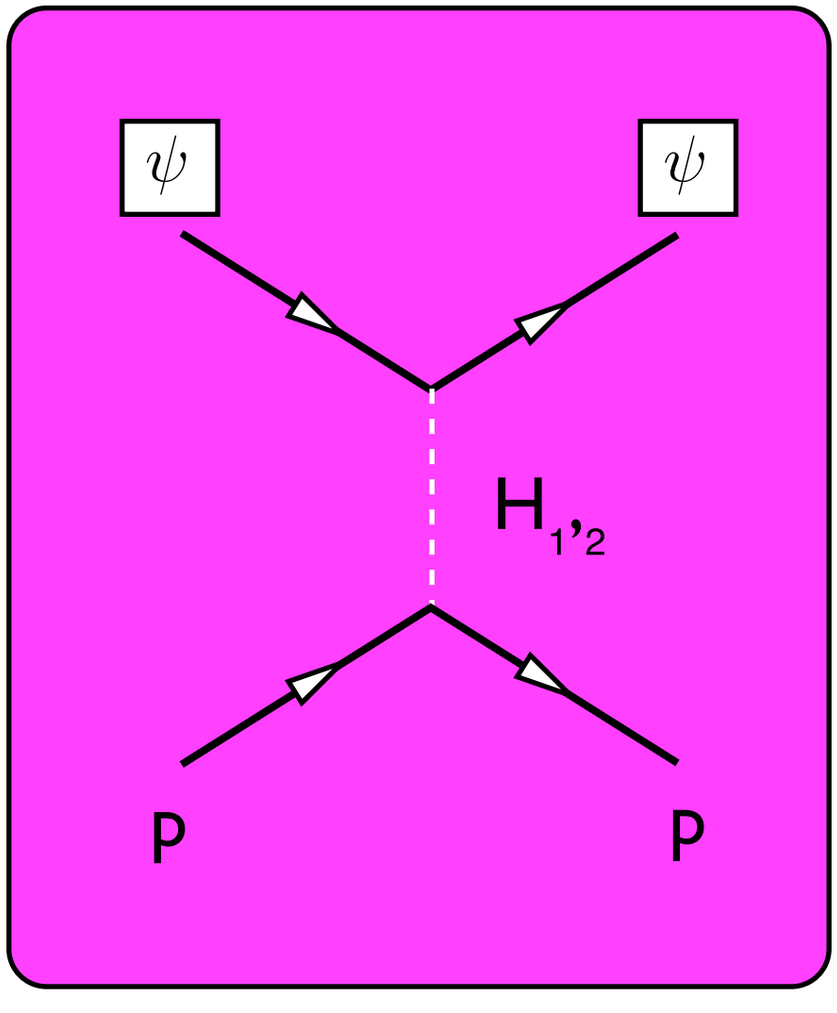
$$H_1 = h\cos\alpha - s\sin\alpha,$$
$$H_2 = h\sin\alpha + s\cos\alpha.$$

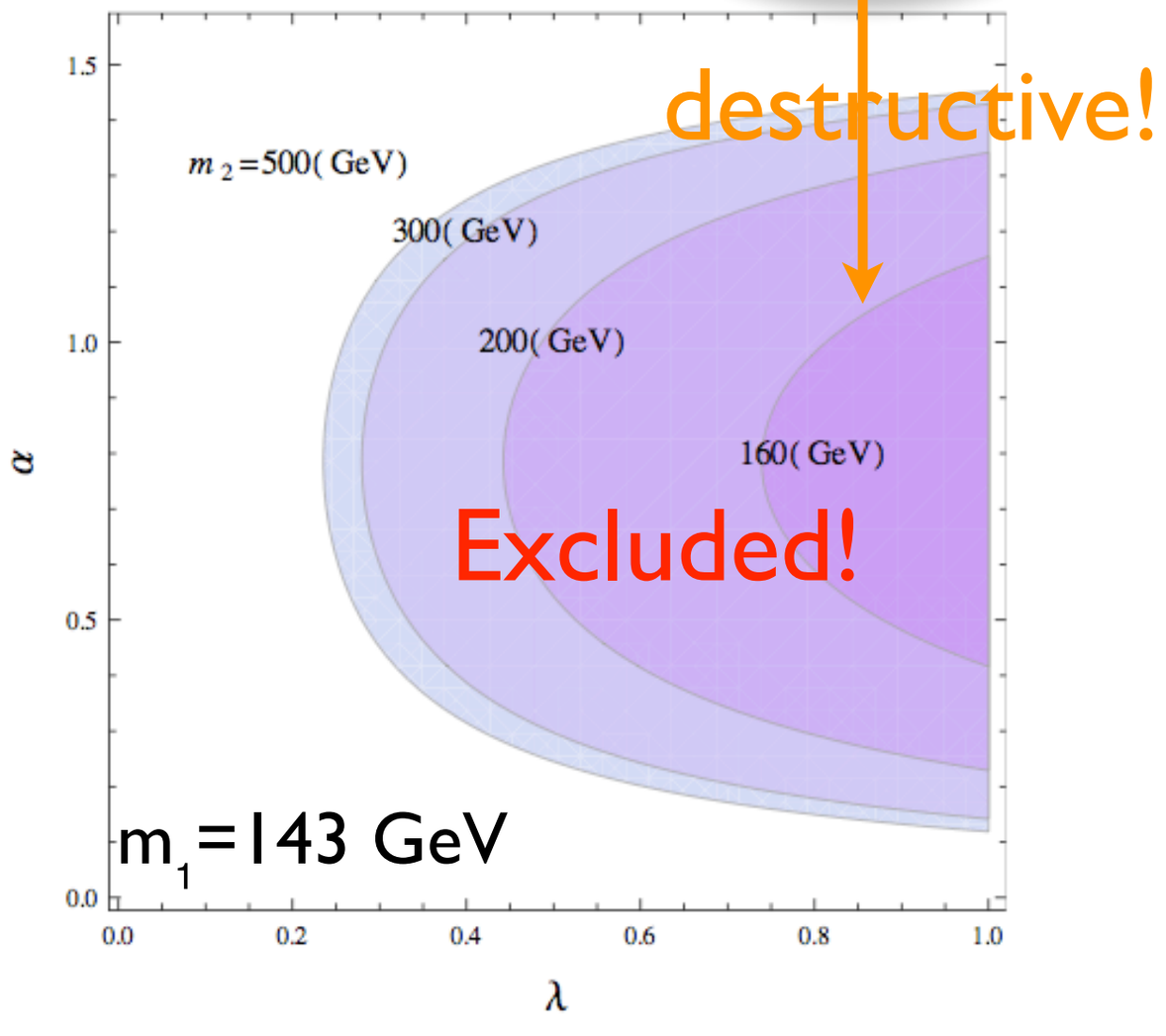
Mixing of Higgs and singlet

Constraints

- Dark matter to nucleon cross section (constraint)

$$\sigma_p \approx \frac{1}{\pi}\mu^2\lambda_p^2 \simeq 2.7\times 10^{-2}\frac{m_p^2}{\pi}\left|\left(\frac{m_p}{v}\right)\lambda \sin\alpha\cos\alpha\left(\frac{1}{m_1^2}-\frac{1}{m_2^2}\right)\right|^2$$





Low energy pheno.

- Universal suppression of collider SM signals

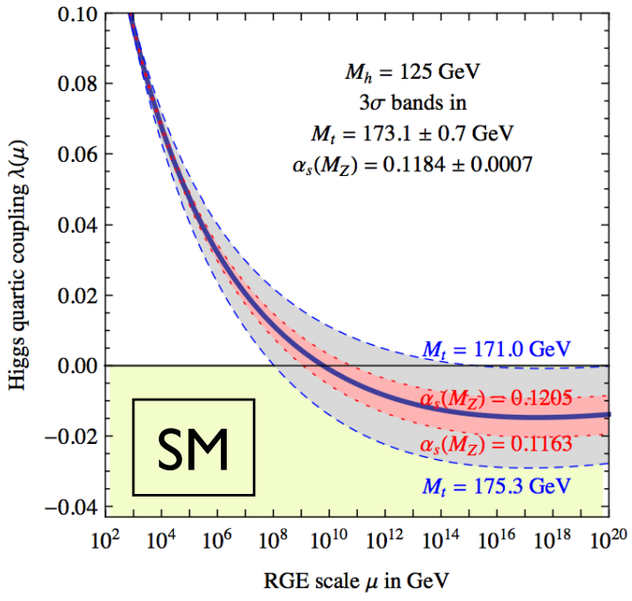
[See 1112.1847, Seungwon Baek, P. Ko & WIP]

- If "$m_h > 2\, m_\phi$", non-SM Higgs decay!

- Tree-level shift of $\lambda_{H,SM}$ (& loop correction)

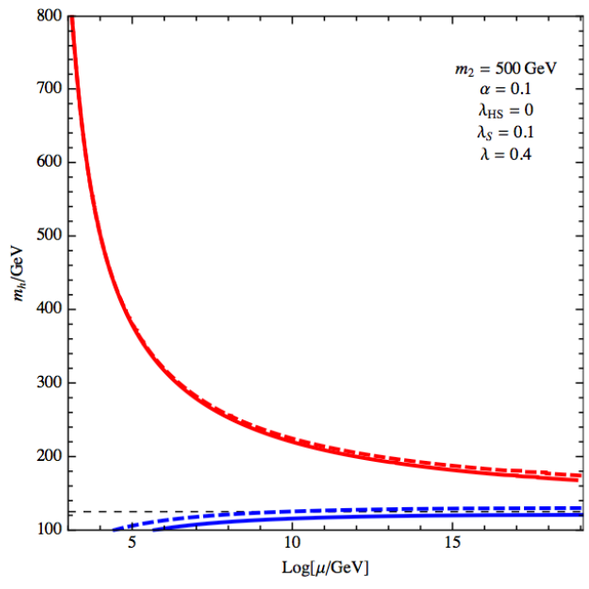
$$\lambda_{\Phi H} \Rightarrow \lambda_H = \left[1 + \left(\frac{m_\phi^2}{m_h^2} - 1\right)\sin^2\alpha\right]\lambda_H^{\rm SM}$$

⇨ If "$m_\phi > m_h$", vacuum instability can be cured.



[G. Degrassi et al., 1205.6497]

α



[S. Baek, P. Ko, WIP & E. Senaha, JHEP(2012)]

UV Completion of HP VDM

[S Baek, P Ko, WI Park, E Senaha, arXiv:1212.2131 (JHEP)]

$$\mathcal{L}_{VDM} = -\frac{1}{4}X_{\mu\nu}X^{\mu\nu} + (D_\mu\Phi)^\dagger(D^\mu\Phi) - \frac{\lambda_\Phi}{4}\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)^2$$
$$-\lambda_{H\Phi}\left(H^\dagger H - \frac{v_H^2}{2}\right)\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right) \ ,$$

$X_\mu \equiv V_\mu$ here

$$\boxed{\Phi(x) = (v_\phi + \phi(x))/\sqrt{2}}$$

- There appear a new singlet scalar (dark Higgs) $\phi(x)$ from $\Phi(x)$, which mixes with the SM Higgs boson through Higgs portal interaction ($\lambda_{H\Phi}$ term)
- The effects must be similar to the singlet scalar in the fermion CDM model, and generically true in the DM with dark gauge symmetry
- Can accommodate GeV scale gamma ray excess from GC with $VV \to \phi\phi$
- **Can modify the Higgs inflation : No tight correlation with top mass**

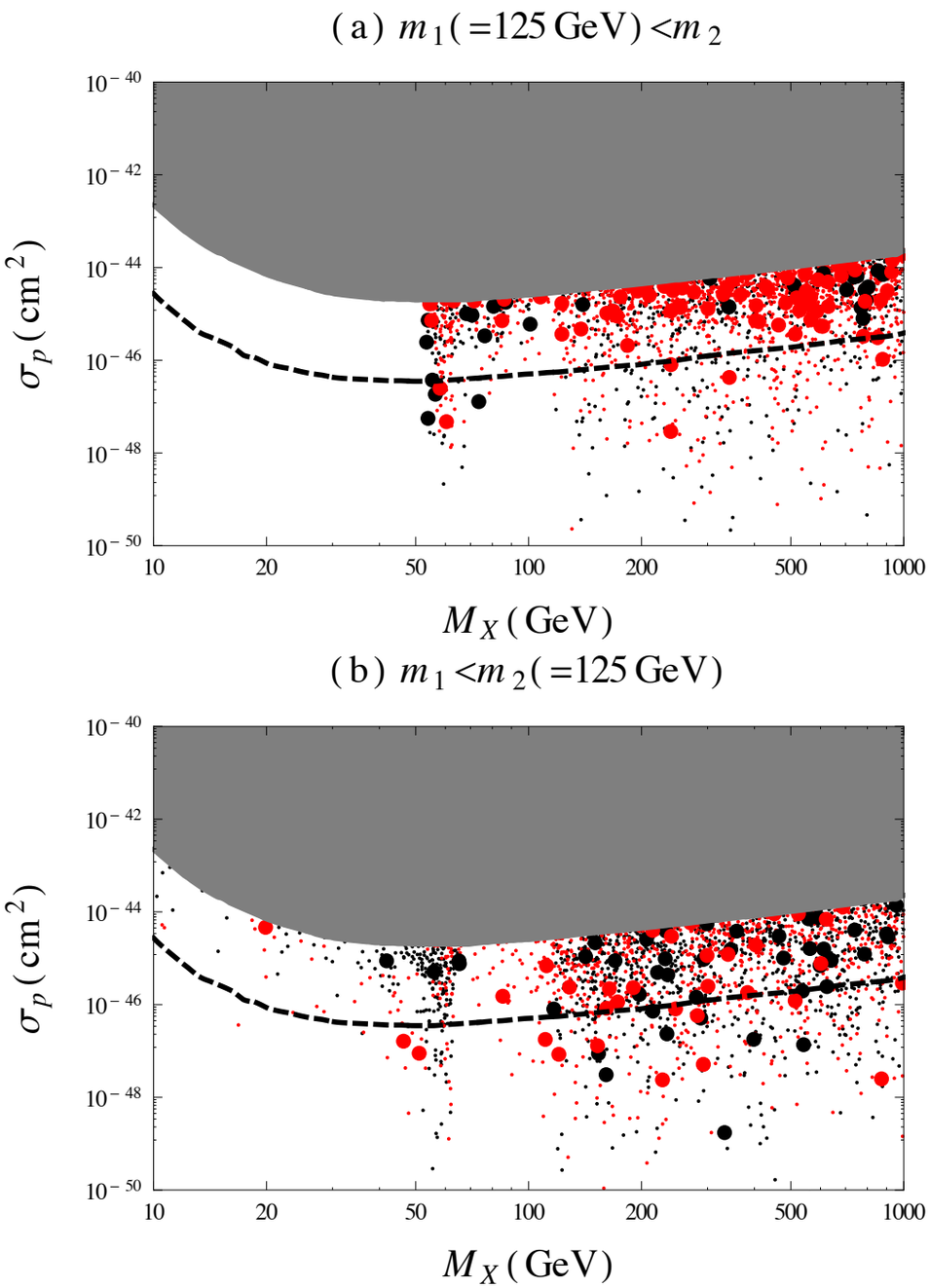


Figure 6. The scattered plot of σ_p as a function of M_X. The big (small) points (do not) satisfy the WMAP relic density constraint within 3 σ, while the red-(black-)colored points gives $r_1 > 0.7 (r_1 < 0.7)$. The grey region is excluded by the XENON100 experiment. The dashed line denotes the sensitivity of the next XENON experiment, XENON1T.

New scalar (Dark Higgs) improves EW vacuum stability

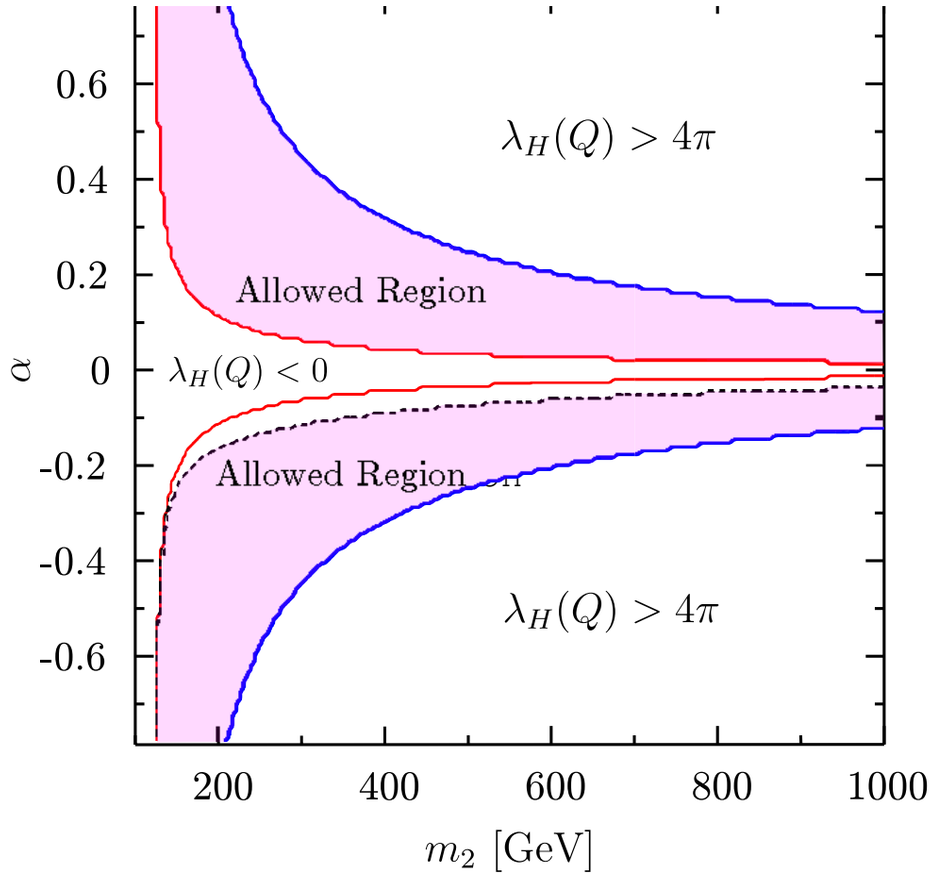


Figure 8. The vacuum stability and perturbativity constraints in the α-m_2 plane. We take $m_1 = 125$ GeV, $g_X = 0.05$, $M_X = m_2/2$ and $v_\Phi = M_X/(g_X Q_\Phi)$.

Interaction Lagrangians

Scalar DM

$$\mathcal{L}^{\rm int}_{\rm SDM} = -h\,\left(\frac{2m_W^2}{v_h}W_\mu^+W^{-\mu} + \frac{m_Z^2}{v_h}Z_\mu Z^\mu\right) - \lambda_{HS}v_h\;hS^2.$$

Singlet FDM

$$\mathcal{L}^{\rm int}_{\rm FDM} = -\left(H_1\cos\alpha + H_2\sin\alpha\right)\left(\sum_f \frac{m_f}{v_h}\bar{f}f - \frac{2m_W^2}{v_h}W_\mu^+W^{-\mu} - \frac{m_Z^2}{v_h}Z_\mu Z^\mu\right)$$
$$+\,g_\chi\left(H_1\sin\alpha - H_2\cos\alpha\right)\;\bar{\chi}\chi\;.$$

Vector DM

$$\mathcal{L}^{\rm int}_{\rm VDM} = -\left(H_1\cos\alpha + H_2\sin\alpha\right)\left(\sum_f \frac{m_f}{v_h}\bar{f}f - \frac{2m_W^2}{v_h}W_\mu^+W^{-\mu} - \frac{m_Z^2}{v_h}Z_\mu Z^\mu\right)$$
$$-\,\frac{1}{2}g_V m_V\left(H_1\sin\alpha - H_2\cos\alpha\right)\;V_\mu V^\mu\;.$$

NB: One can not simply ignore 125 GeV Higgs Boson or singlet scalar by hand, since it would violate gauge invariance and unitarity !

S. Baek, P. Ko, M. Park, WIPark, C.Yu,
arXiv:1506.06556, PLB (2016)

- EFT : Effective operator $\mathcal{L}_{int} = \frac{m_q}{\Lambda_{dd}^3}\bar{q}q\bar{\chi}\chi$
- S.M.: Simple scalar mediator S of
  $\mathcal{L}_{int} = \left(\frac{m_q}{v_H}\sin\alpha\right) S\bar{q}q - \lambda_s \cos\alpha S\bar{\chi}\chi$
- H.M.: A case where a Higgs is a mediator
  $\mathcal{L}_{int} = -\left(\frac{m_q}{v_H}\cos\alpha\right) H\bar{q}q - \lambda_s \sin\alpha H\bar{\chi}\chi$
- H.P.: Higgs portal model as in eq. (2).

$$\frac{d\sigma_i}{dm_{\chi\chi}} \propto \left|\frac{\sin 2\alpha\ g_\chi}{m_{\chi\chi}^2 - m_{H_1}^2 + i m_{H_1}\Gamma_{H_1}} - \frac{\sin 2\alpha\ g_\chi}{m_{\chi\chi}^2 - m_{H_2}^2 + i m_{H_2}\Gamma_{H_2}}\right|^2$$

$$\text{H.P.} \underset{m_{H_2}^2 \gg \hat{s}}{\longrightarrow} \text{H.M.},$$

$$\text{S.M.} \underset{m_S^2 \gg \hat{s}}{\longrightarrow} \text{EFT},$$

$$\text{H.M.} \neq \text{EFT}\,.$$

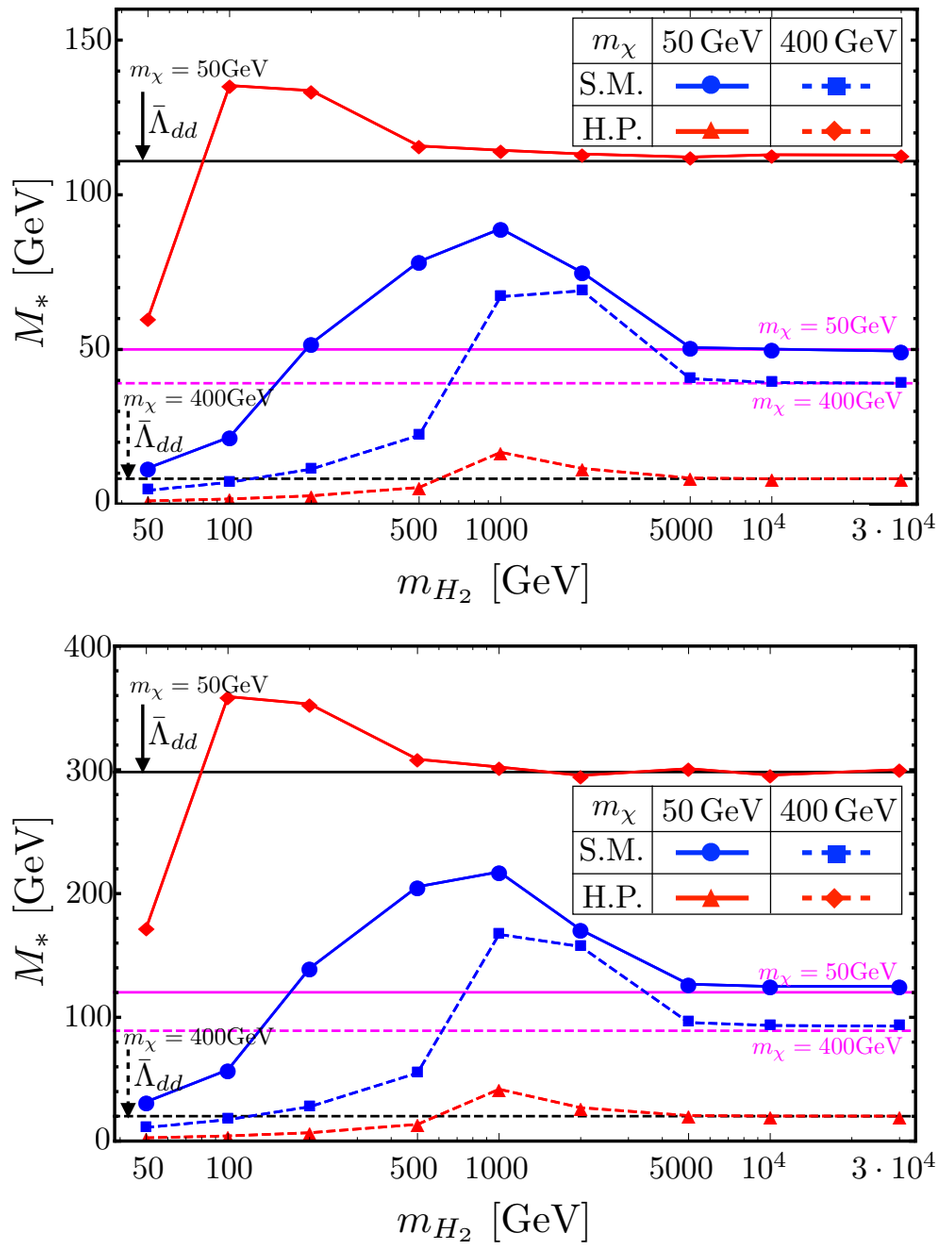
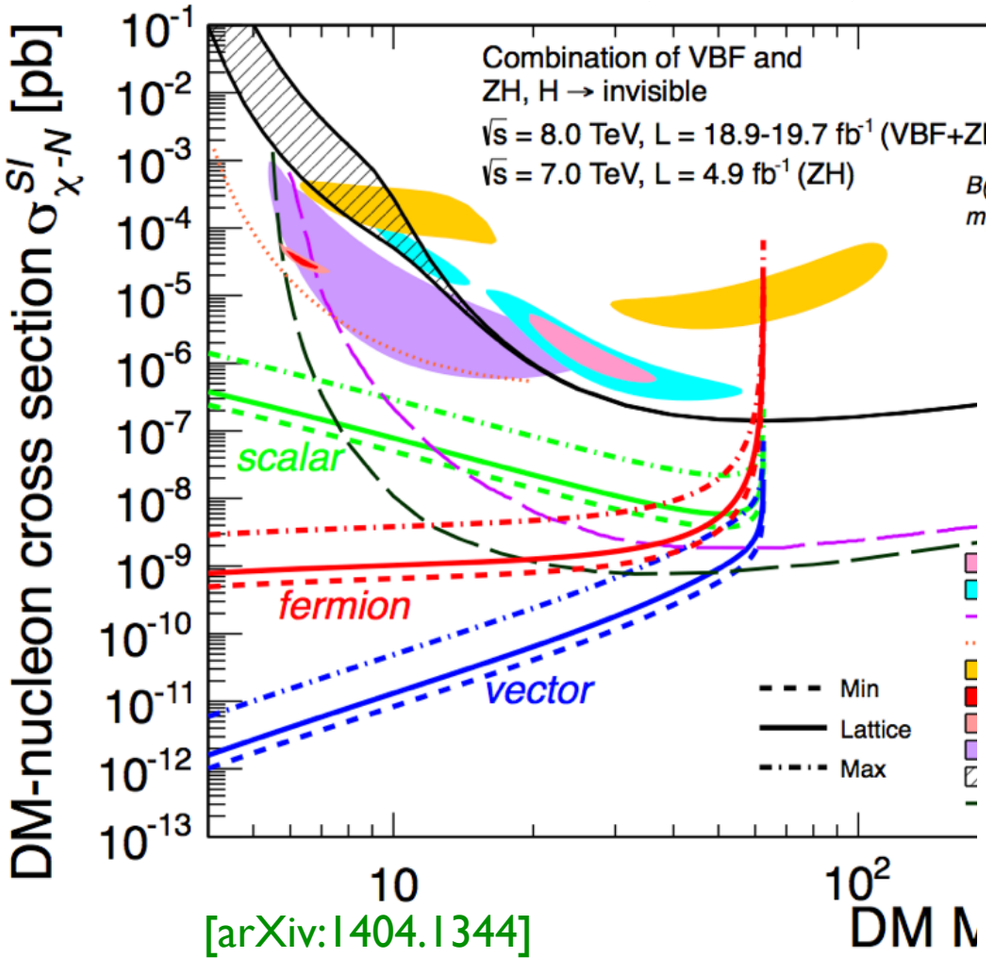


FIG. 3: The experimental bounds on M_* at 90% C.L. as a function of m_{H_2} (m_S in S.M. case) in the monojet+$\not{E}_T$ search (upper) and $t\bar{t} + \not{E}_T$ search (lower). Each line corresponds to the EFT approach (magenta), S.M. (blue), H.M. (black), and H.P. (red), respectively. The bound of S.M., H.M., and H.P., are expressed in terms of the effective mass M_* through the Eq.(16)-(20). The solid and dashed lines correspond to $m_\chi = 50$ GeV and 400 GeV in each model, respectively.

Collider Implications

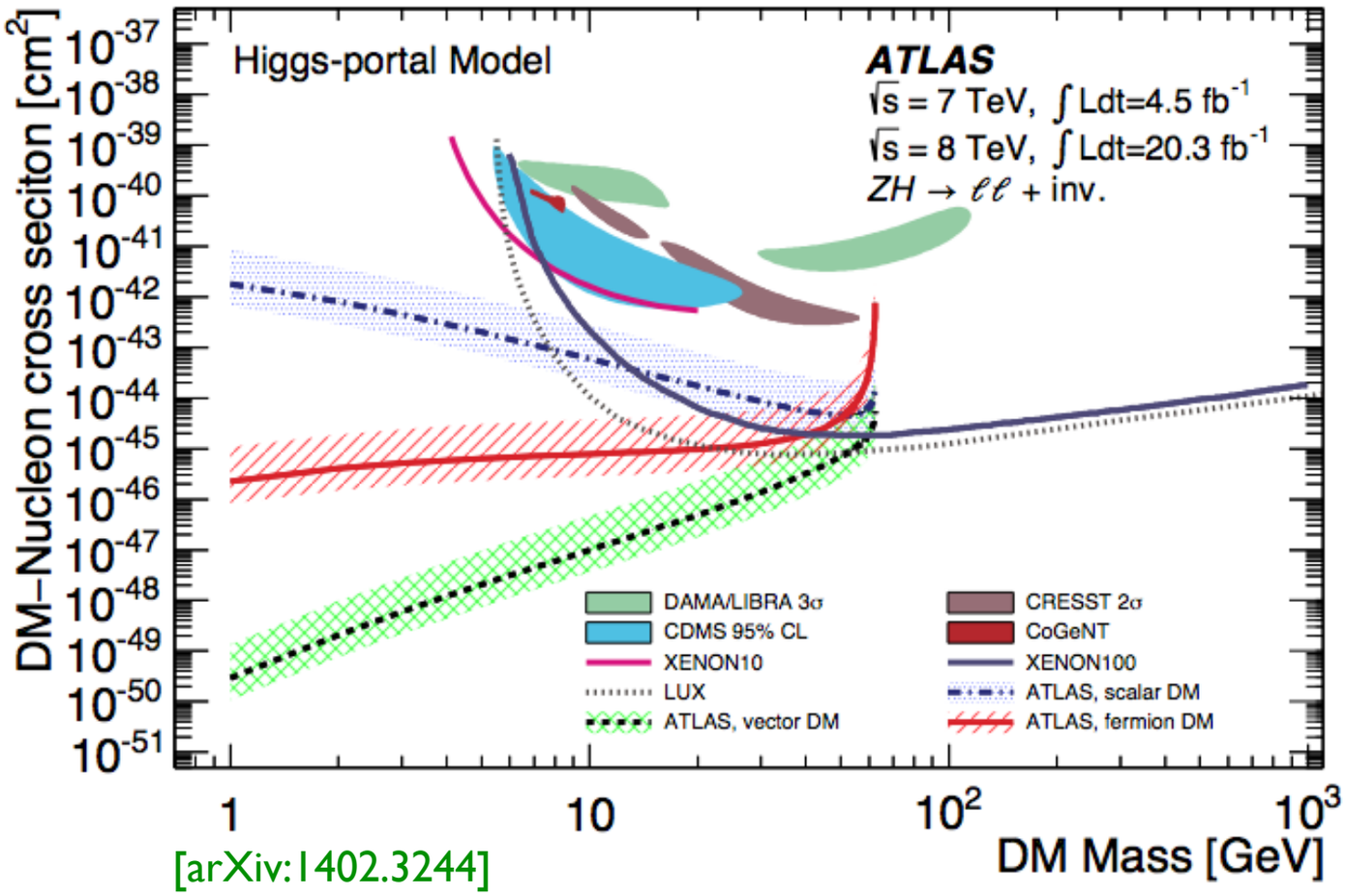
$m_h = 125\text{GeV},\ \text{Br}(H \to \text{inv}) < 0.51$ at 90% CL



[arXiv:1404.1344]

Based on EFTs

$m_h = 125.5\text{GeV},\ \text{Br}(H \to \text{inv}) < 0.52$ at 90% CL



[arXiv:1402.3244]

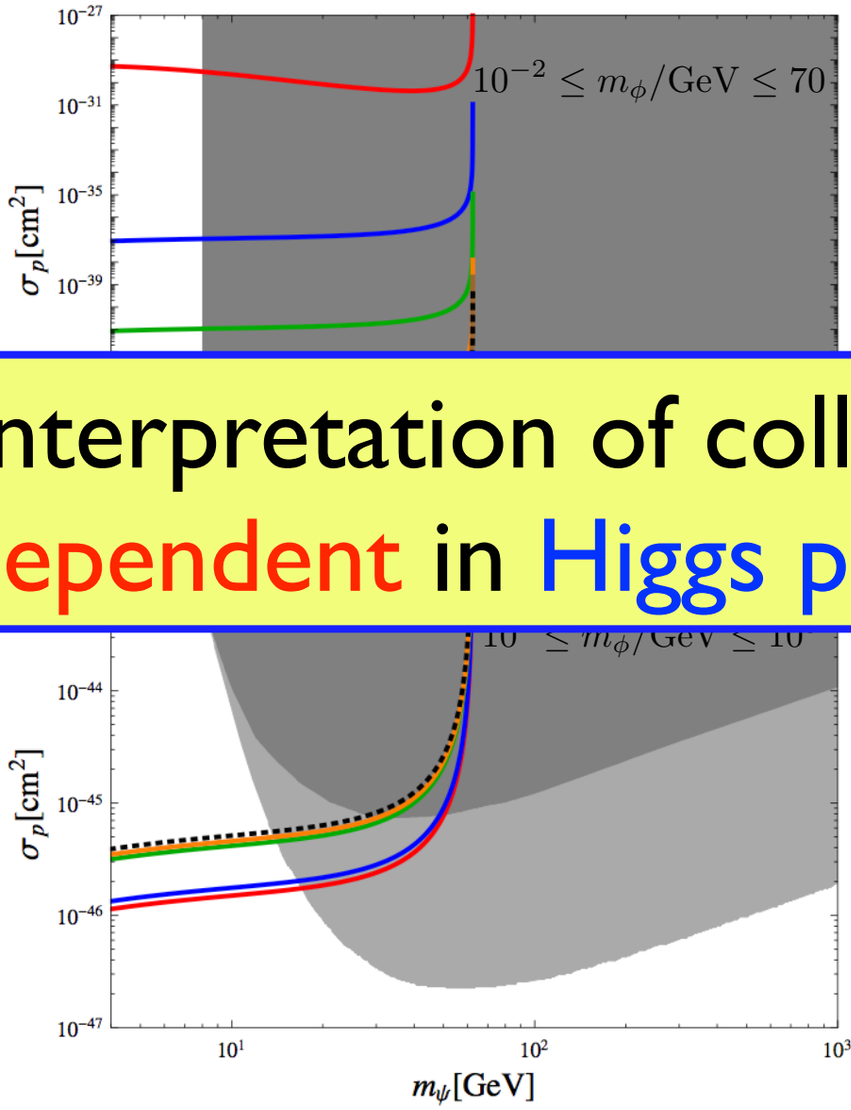
- However, in renormalizable unitary models of Higgs portals, 2 more relevant parameters !

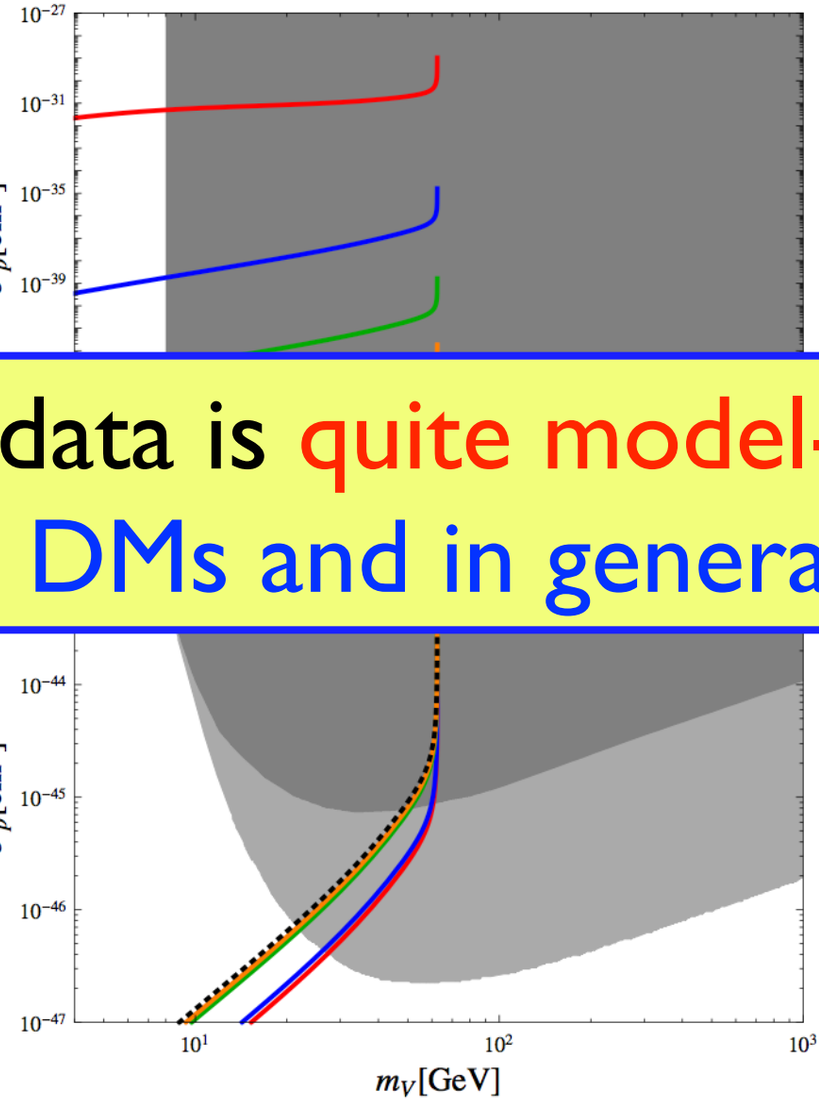
$$\mathcal{L}_{\rm SFDM} = \overline{\psi}\left(i\partial - m_\psi - \lambda_\psi S\right) - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H$$
$$+ \frac{1}{2}\partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \mu_S^3 S - \frac{\mu_S^{'}}{3} S^3 - \frac{\lambda_S}{4} S^4.$$

[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

$$\mathcal{L}_{\rm VDM} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + D_\mu \Phi^\dagger D^\mu \Phi - \lambda_\Phi \left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)^2 - \lambda_{\Phi H}\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)\left(H^\dagger H - \frac{v_H^2}{2}\right)$$

$$\sigma_p^{\rm SI} = (\sigma_p^{\rm SI})_{\rm EFT}\, c_\alpha^4 m_h^4 \mathcal{F}(m_{\rm DM}, \{m_i\}, v)$$
$$\simeq (\sigma_p^{\rm SI})_{\rm EFT}\, c_\alpha^4 \left(1 - \frac{m_h^2}{m_2^2}\right)^2$$





Dashed curve: ATLAS,CMS

Interpretation of collider data is quite model-dependent in Higgs portal DMs and in general

- However, in renormalizable unitary models of Higgs portals, 2 more relevant parameters !

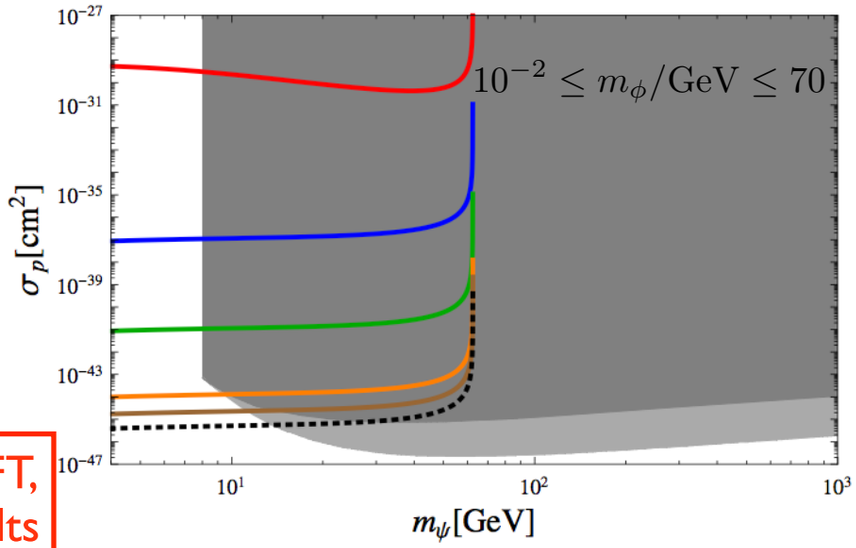
$$\mathcal{L}_{\rm SFDM} = \overline{\psi}\left(i\partial - m_\psi - \lambda_\psi S\right) - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H$$
$$+ \frac{1}{2}\partial_\mu S \partial^\mu S - \frac{1}{2} m_S^2 S^2 - \mu_S^3 S - \frac{\mu_S^{'}}{3} S^3 - \frac{\lambda_S}{4} S^4.$$

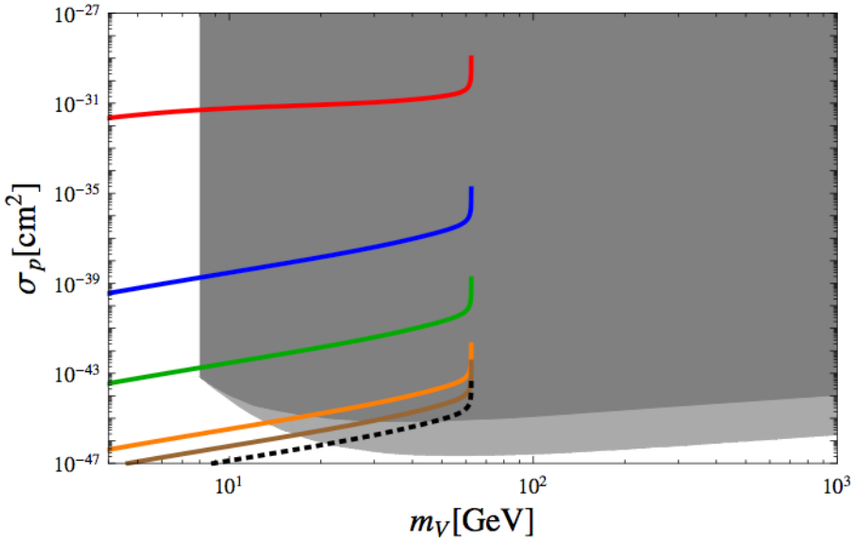
[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

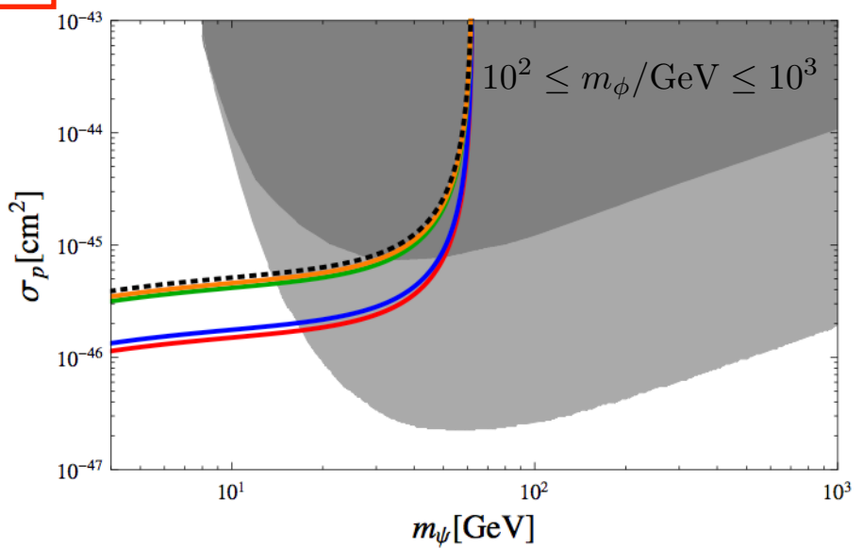
$$\mathcal{L}_{\rm VDM} = -\frac{1}{4} V_{\mu\nu} V^{\mu\nu} + D_\mu \Phi^\dagger D^\mu \Phi - \lambda_\Phi \left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)^2 - \lambda_{\Phi H}\left(\Phi^\dagger\Phi - \frac{v_\Phi^2}{2}\right)\left(H^\dagger H - \frac{v_H^2}{2}\right)$$

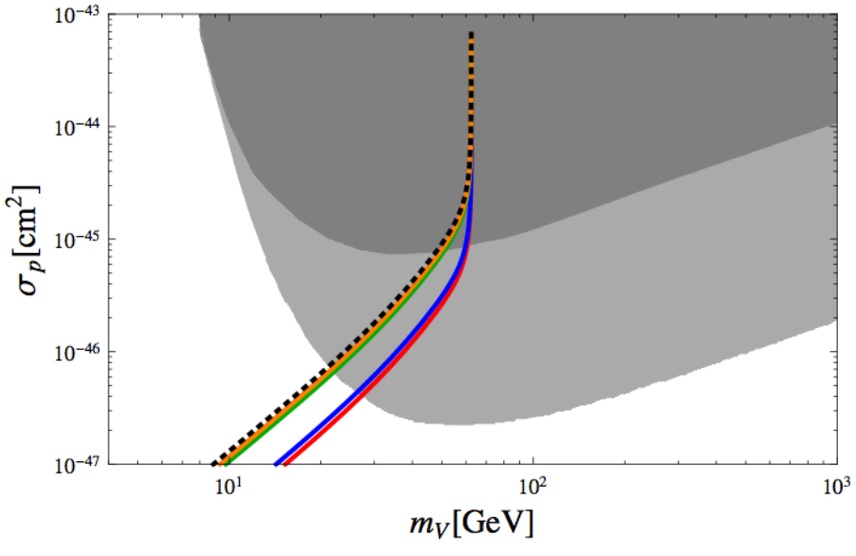
$$\sigma_p^{\rm SI} = (\sigma_p^{\rm SI})_{\rm EFT}\, c_\alpha^4 m_h^4 \mathcal{F}(m_{\rm DM}, \{m_i\}, v)$$
$$\simeq (\sigma_p^{\rm SI})_{\rm EFT}\, c_\alpha^4 \left(1 - \frac{m_h^2}{m_2^2}\right)^2$$

Dashed curves:EFT, ATLAS,CMS results





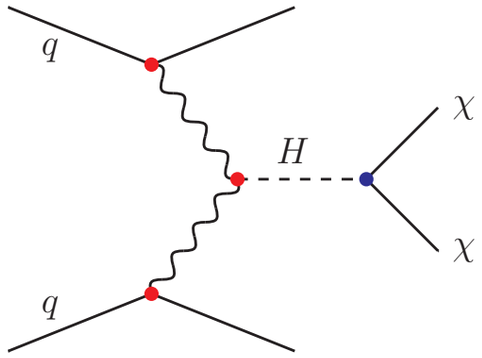




Search for H→ Dark matter (invisible)

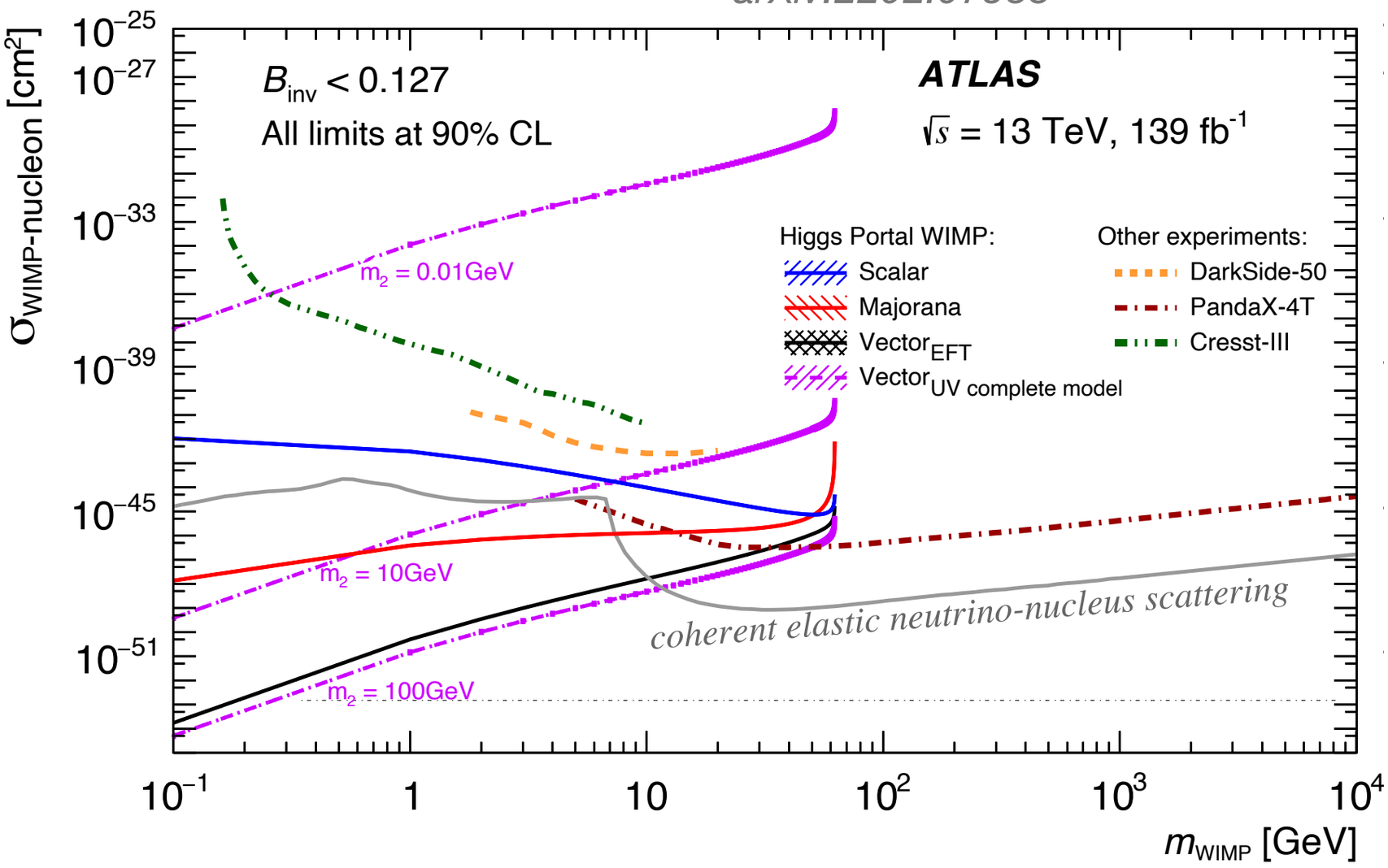
BR(H→invisible) < 14.5% (obs) (10.3% exp.)
from search with VBF topology
(13% limit when combined with Higgs coupling measurements)

ATLAS Highlight talks
By G.Unal @ICHEP2022, and
By M. Cristinziani @ CORFU2022



Now implemented in the ATLAS results,
But only for VDM, and not for SFDM

arXiv:2202.07953



Invisible H decay into a pair of VDM

[arXiv: 1405.3530, S. Baek, P. Ko & WIPark, PRD]

$$(\Gamma_h^{\rm inv})_{\rm EFT} = \frac{\lambda_{VH}^2}{128\pi}\frac{v_H^2 m_h^3}{m_V^4}\times \left(1-\frac{4m_V^2}{m_h^2}+12\frac{m_V^4}{m_h^4}\right)\left(1-\frac{4m_V^2}{m_h^2}\right)^{1/2} \quad (23)$$

Diverge when $m_V \to 0$!!

$m_V \propto g_x Q_\Phi v_\Phi$

$\frac{g_X^2}{m_V^2} = \frac{g_X^2}{g_X^2 Q_\Phi^2 v_\Phi^2} \to \frac{1}{v_\Phi^2} = \text{finite}$

VS.

$$\Gamma_i^{\rm inv} = \frac{g_X^2}{32\pi}\frac{m_i^3}{m_V^2}\left(1-\frac{4m_V^2}{m_i^2}+12\frac{m_V^4}{m_i^4}\right)\left(1-\frac{4m_V^2}{m_i^2}\right)^{1/2}\sin^2\alpha \quad (22)$$

Invisible H decay width : finite for small mV in unitary/renormalizable model

Two Limits for $m_V \to 0$

Also see the addendum: by S Baek, P Ko, WI Park

- $m_V = g_X Q_\Phi v_\Phi$ in the UV completion with dark Higgs boson

- Case I : $g_X \to 0$ with finite $v_\Phi \neq 0$

$$\frac{g_X^2 Q_\Phi^2}{m_V^2} = \frac{g_X^2 Q_\Phi^2}{g_X^2 Q_\Phi^2 v_\Phi^2} = \frac{1}{v_\Phi^2} = \text{finite.}$$

$$\left(\Gamma_h^{\text{inv}}\right)_{\text{UV}} = \frac{1}{32\pi}\frac{m_h^3}{v_\Phi^2}\sin^2\alpha = \Gamma(h \to a_\Phi a_\Phi)$$

with a_Φ being the NG boson for spontaneously broken global $U(1)_X$

- Case II : $v_\Phi \to 0$ with finite $g_X \neq 0$

$$\alpha \xrightarrow{v_\Phi \to 0^+} \frac{2\lambda_{H\Phi} v_\Phi}{\lambda_H v_H}$$

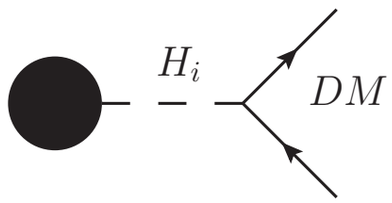
$$\frac{g_X^2 Q_\Phi^2}{m_V^2}\sin^2\alpha \xrightarrow{v_\Phi \to 0^+} \frac{4\lambda_{H\Phi}^2}{\lambda_H^2 v_H^2} = \frac{2\lambda_{H\Phi}^2}{\lambda_H m_h^2} = \text{finite,}$$

$$\left(\Gamma_h^{\text{inv}}\right)_{\text{UV}} \xrightarrow{v_\Phi \to 0^+} \frac{1}{16\pi}\frac{\lambda_{H\Phi}^2 m_h}{\lambda_H}$$

Therefore $\Gamma(h \to VV)$ is finite when $m_V \to 0$ in the UV completions

DM Production @ ILC

P Ko, H Yokoya, arXiv:1603.08802, JHEP



,

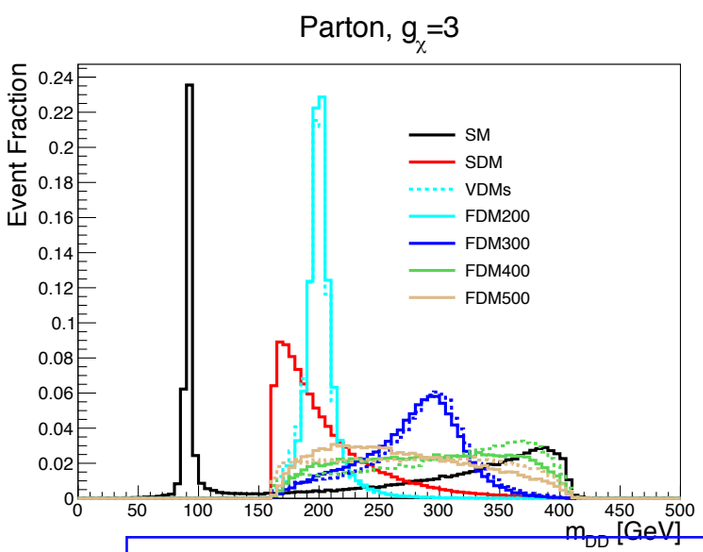
$$t \equiv m_{DD}^2$$

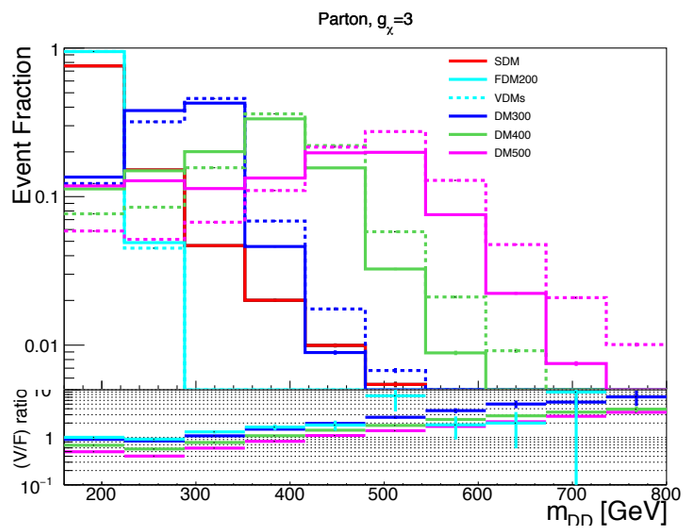
We consider $e^+e^- \to Z* \to ZH_{i=1,2}$ followed by $H_i \to \bar{\chi}\chi$

$$\frac{d\sigma_{\rm SDM}}{dt} \propto \sigma^{h*}_{\rm SDM} \times |\frac{1}{t-m_h^2+im_h\Gamma_h}|^2,$$

$$\frac{d\sigma_{\rm FDM}}{dt} \propto \sigma^{h*}_{\rm FDM} \times |\frac{1}{t-m_{H_1}^2+im_{H_1}\Gamma_{H_1}} - \frac{1}{t-m_{H_2}^2+im_{H_2}\Gamma_{H_2}}|^2 \cdot \left(2t-8m_\chi^2\right),$$

$$\frac{d\sigma_{\rm VDM}}{dt} \propto \sigma^{h*}_{\rm VDM} \times |\frac{1}{t-m_{H_1}^2+im_{H_1}\Gamma_{H_1}} - \frac{1}{t-m_{H_2}^2+im_{H_2}\Gamma_{H_2}}|^2 \cdot \left(2+\frac{(t-2m_D^2)^2}{4m_V^4}\right).$$





Fix DM mass = 80 GeV, sin(alpha) = 0.3, and vary H2 mass (200,300,400,500) GeV

Asymptotic behavior in the full theory ($t \equiv m^2_{\chi\chi}$)

$$\text{ScalarDM}: \quad G(t) \sim \frac{1}{(t-m_H^2)^2 + m_H^2\Gamma_H^2} \tag{5.7}$$

$$\text{SFDM}: \quad G(t) \sim \left|\frac{1}{t-m_1^2+im_1\Gamma_1} - \frac{1}{t-m_2^2+im_2\Gamma_2}\right|^2 \ (t-4m_\chi^2) \tag{5.8}$$

$$\to |\frac{1}{t^2}|^2 \times t \sim \frac{1}{t^3} \ (\text{as } t\to\infty) \tag{5.9}$$

$$\text{VDM}: \quad G(t) \sim \left|\frac{1}{t-m_1^2+im_1\Gamma_1} - \frac{1}{t-m_2^2+im_2\Gamma_2}\right|^2 \ \left[2+\frac{(t-2m_V^2)^2}{4m_V^4}\right] \tag{5.10}$$

$$\to |\frac{1}{t^2}|^2 \times t^2 \sim \frac{1}{t^2} \ (\text{as } t\to\infty) \tag{5.11}$$

Asymptotic behavior w/o the 2nd Higgs (EFT)

$$\text{SFDM}: \quad G(t) \sim \frac{1}{(t-m_H^2)^2 + m_H^2\Gamma_H^2} \ (t-4m_\chi^2)$$

$$\to \frac{1}{t} \ (\text{as } t\to\infty)$$

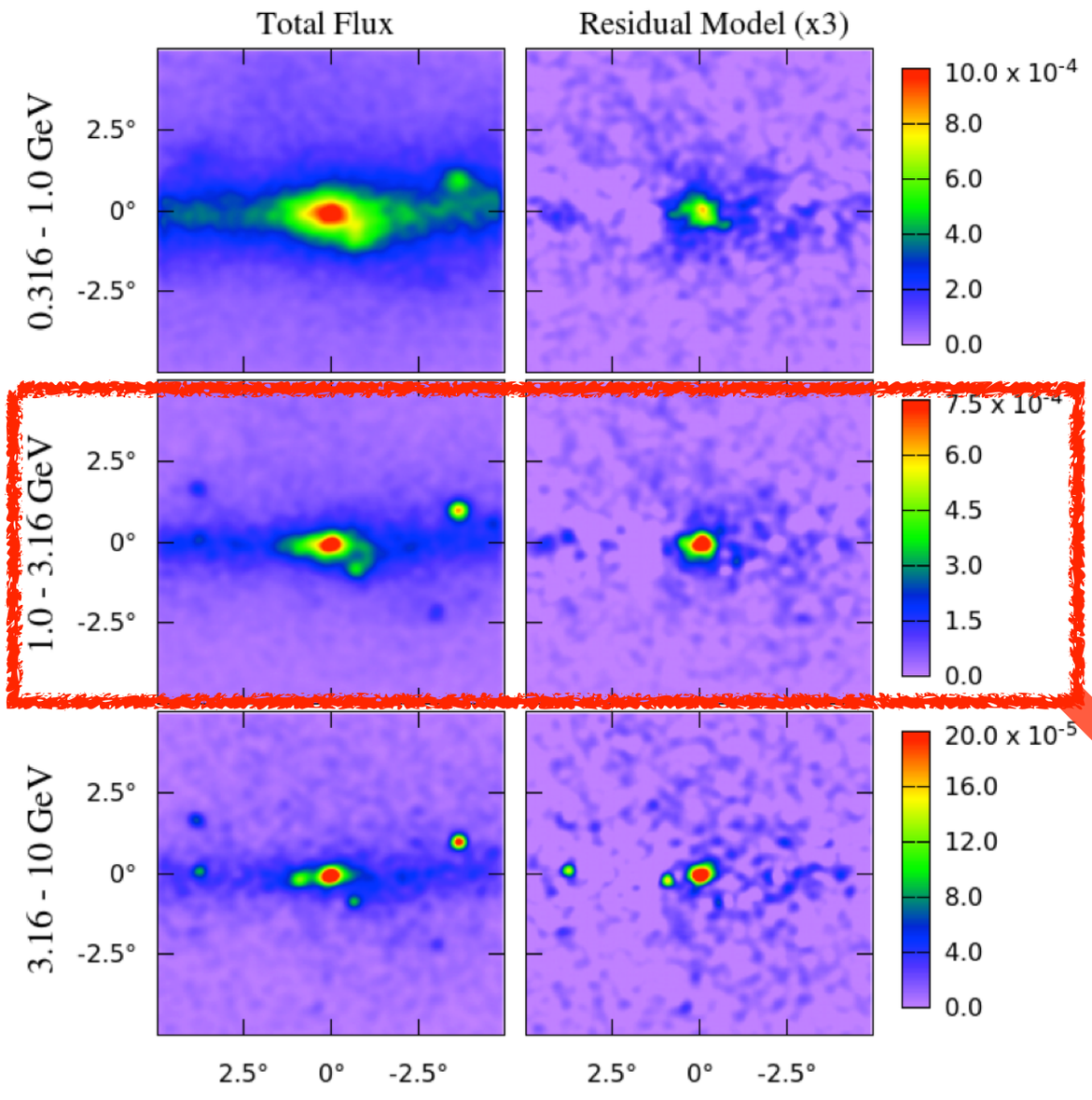
$$\text{VDM}: \quad G(t) \sim \frac{1}{(t-m_H^2)^2 + m_H^2\Gamma_H^2} \ \left[2+\frac{(t-2m_V^2)^2}{4m_V^4}\right]$$

$$\to \text{constant} \ (\text{as } t\to\infty)$$

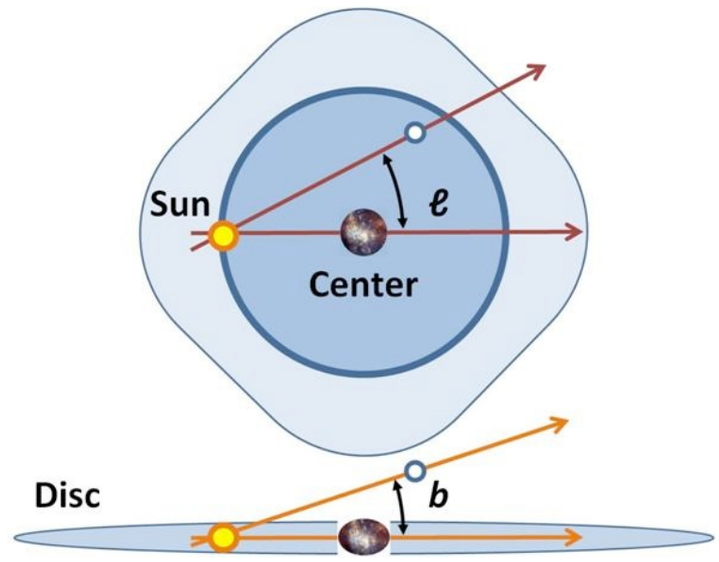
Unitarity is violated in EFT!

Fermi-LAT GC γ-ray

see arXiv:1612.05687 for a recent overview by
C.Karwin, S. Murgia, T. Tait, T.A.Porter, P. Tanedo



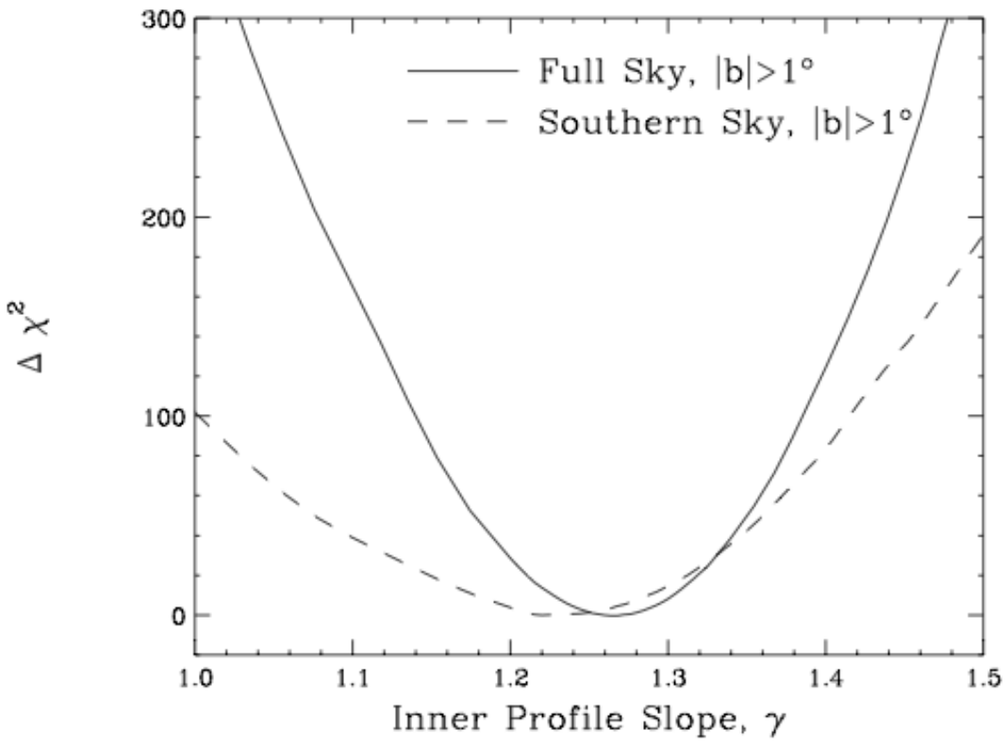
[1402.6703, T. Daylan et.al.]



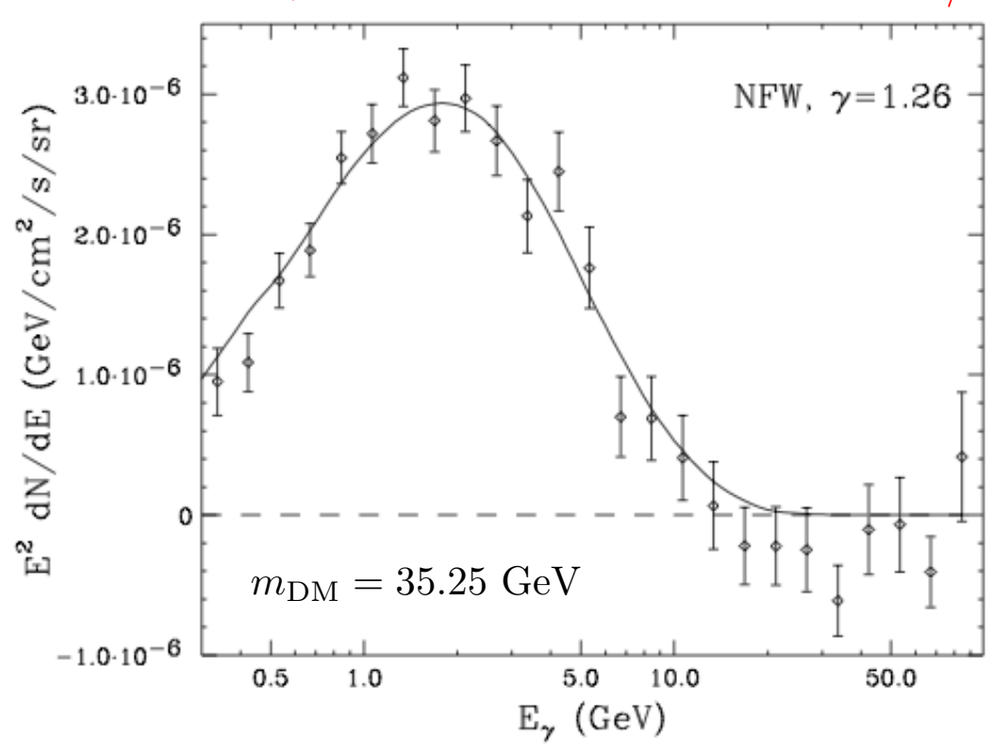
$$\mathrm{GC}: b \sim l \lesssim 0.1^\circ$$

extended
GeV scale excess!

- A DM interpretation



$\mathrm{DM} + \mathrm{DM} \to b\bar{b}$ with $\sigma v = 1.7 \times 10^{-26} \mathrm{cm}^3/\mathrm{s}$



* See "1402.6703, T. Daylan et.al." for other possible channels

- Millisecond Pulars (astrophysical alternative)

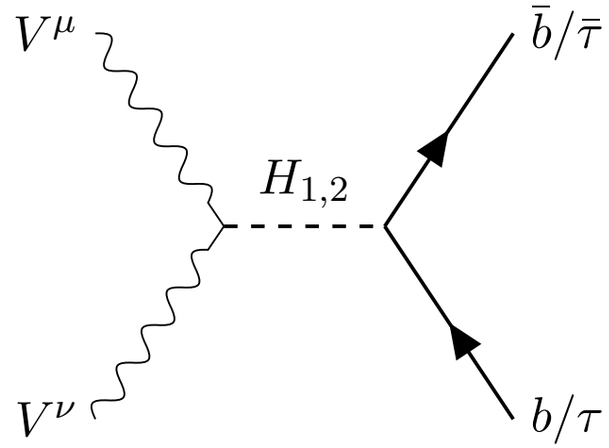
It may or may not be the main source, depending on

- luminosity func.
- bulge population
- distribution of bulge population

* See "1404.2318, Q. Yuan & B. Zhang" and "1407.5625, I. Cholis, D. Hooper & T. Linden"

GC gamma ray in HP VDM

P. Ko, WI Park, Y. Tang. arXiv:1404.5257, JCAP



H2 : 125 GeV Higgs
H1 : absent in EFT

Figure 2. Dominant s channel $b + \bar{b}$ (and $\tau + \bar{\tau}$) production

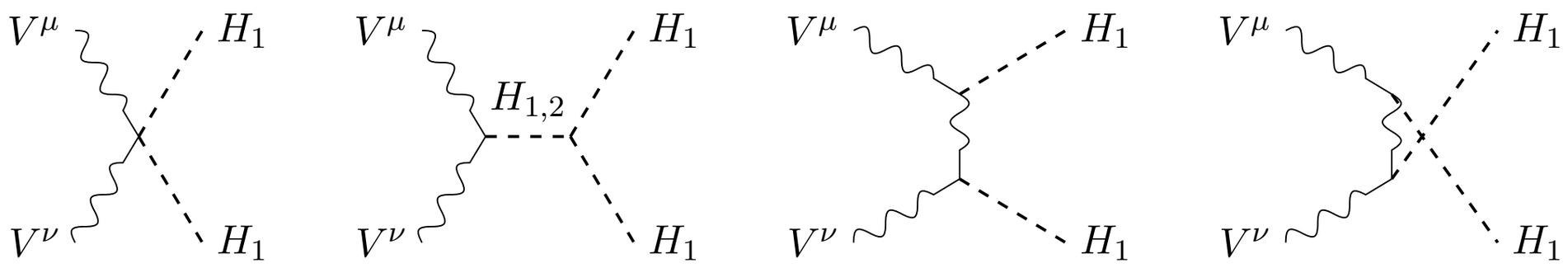


Figure 3. Dominant s/t-channel production of H_1s that decay dominantly to $b + \bar{b}$

Importance of HP VDM with Dark Higgs Boson

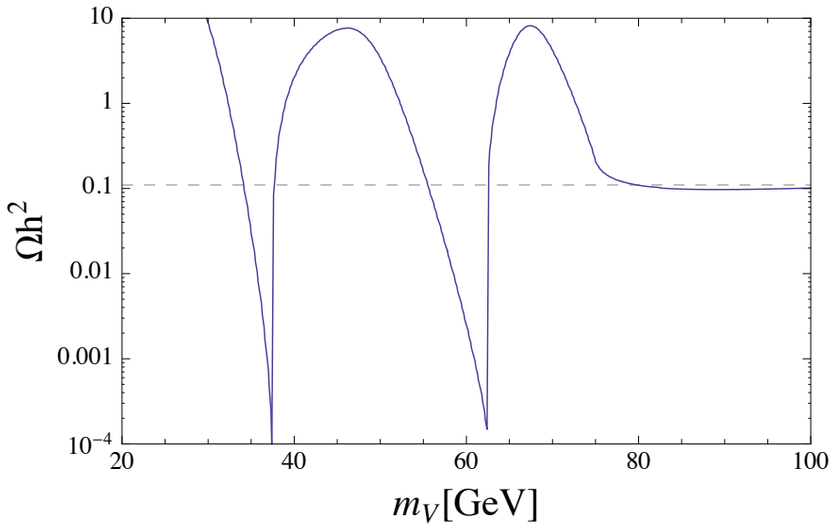


Figure 4. Relic density of dark matter as function of m_ψ for $m_h = 125$, $m_\phi = 75\,\mathrm{GeV}$, $g_X = 0.2$, and $\alpha = 0.1$.

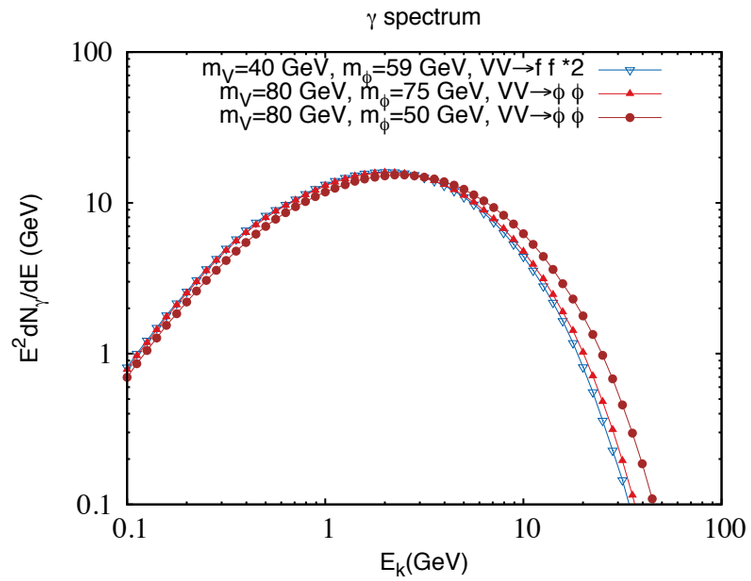


Figure 5. Illustration of γ spectra from different channels. The first two cases give almost the same spectra while in the third case γ is boosted so the spectrum is shifted to higher energy.

This mass range of VDM would have been impossible in the VDM model (EFT)

And No 2nd neutral scalar (Dark Higgs) in EFT

Summary

- Phenomenology of HP VDM and Singlet FDM presented within EFT vs. UV completed models

- EFT approach has a number of drawbacks : non-renormalizable, unitarity violation at high energy colliders, and it applies only if $m_{DM}, m_{\rm SM} \ll m_\phi$ [But we don't know mass scales of dark particles !]

- In particular, one has $\Gamma_{\rm EFT}(H_{125} \to VV) \to \infty$, as $m_V \to 0$, whereas it is finite in UV completed models [Importance of gauge invariance, unitarity and renormalizability]

- The dark Higgs ϕ can play crucial roles in interpreting the DM signatures at colliders, explaining the GC γ-ray excess ($VV \to \phi\phi$), improving vacuum stability up to Planck scale, modifying the Higgs inflation [ϕ should be actively searched for !]

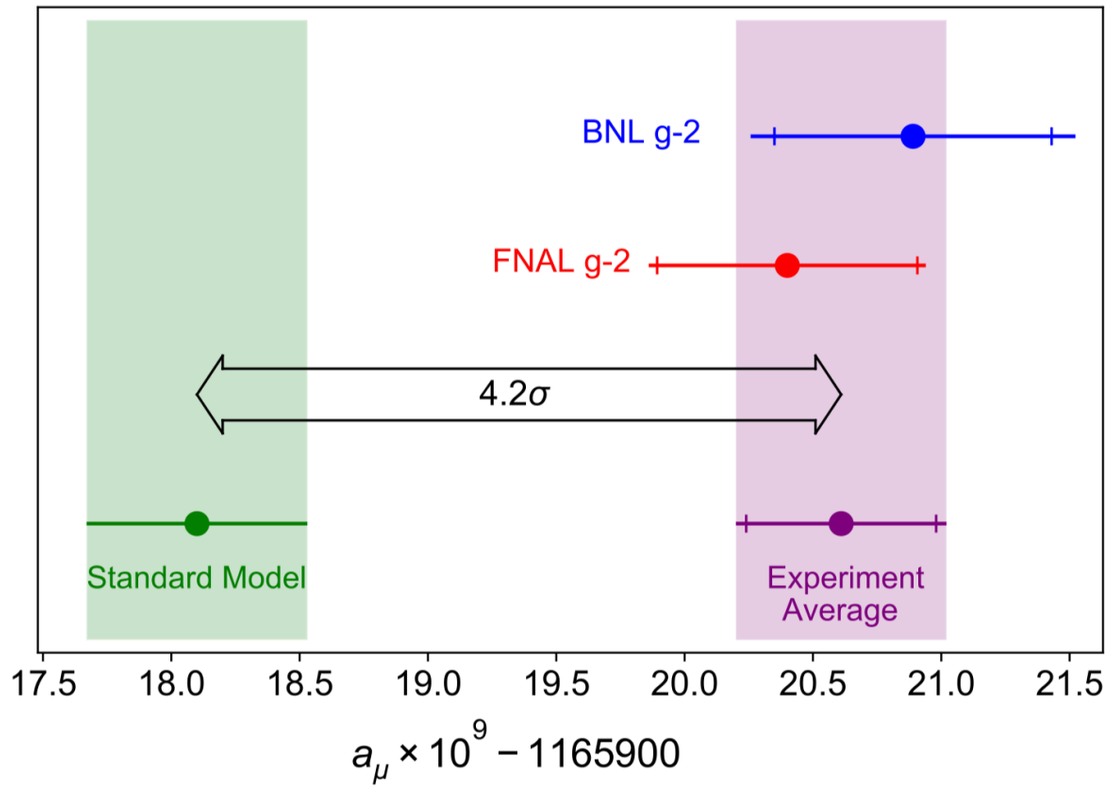
$U(1)_{L_\mu - L_\tau}$ -charged DM : Z' only vs. $Z' + \phi$

arXiv:2204.04889 [hep-ph]
With Seungwon Baek, Jongkuk Kim

SM+$U(1)_{L_\mu - L_\tau}$ gauge sym

- He, Josh, Lew, Volkas, PRD 43, 22; PRD 44, 2118 (1991)
- One of the anomaly free gauge groups without extension of fermion contents
- The simplest anomaly free U(1) extensions that couple to the SM fermions directly
- Can affect the muon g-2, PAMELA e^+ excess, (and B anomalies with extra fermions : Not covered in this talk)

Muon g-2



The Muon g-2 Collaboration, 2104.03281

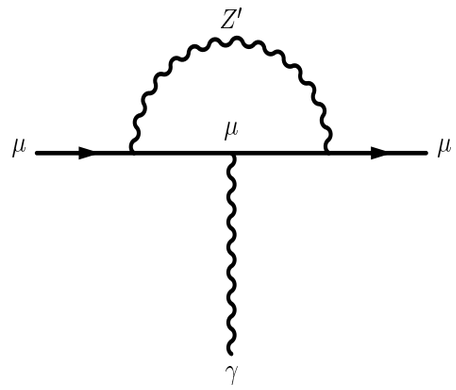
Excellent example for graduate students

- **Relativistic E&M (spinning particle in EM fields)**
- **Special relativity (time dilation)**
- **(V-A) structure of charged weak interaction**

Muon (g-2) in $U(1)_{\mu-\tau}$ Model

Baek, Deshpande, He, Ko : hep-ph/0104141
Baek, Ko : arXiv:0811.1646 [hep-ph]

$$\begin{array}{ll} L_L^e: (1,2,-1)(0) & e_R: (1,1,-2)(0) \\ L_L^\mu: (1,2,-1)(2a) & \mu_R: (1,1,-2)(2a) \\ L_L^\tau: (1,2,-1)(-2a) & \mu_R: (1,1,-2)(-2a). \end{array}$$



$$\Delta a_\mu = \frac{\alpha'}{2\pi}\int_0^1 dx \frac{2m_\mu^2 x^2(1-x)}{x^2 m_\mu^2 + (1-x)M_{Z'}^2} \approx \frac{\alpha'}{2\pi}\frac{2m_\mu^2}{3M_{Z'}^2}$$

$$Z' \to \mu^+\mu^-, \tau^+\tau^-, \nu_\alpha\bar{\nu}_\alpha \text{ (with } \alpha = \mu \text{ or } \tau), \ \psi_D\overline{\psi}_D$$

$\Gamma(Z' \to \mu^+\mu^-) = \Gamma(Z' \to \tau^+\tau^-) = 2\Gamma(Z' \to \nu_\mu\bar{\nu}_\mu) = 2\Gamma(Z' \to \nu_\tau\bar{\nu}_\tau) = \Gamma(Z' \to \psi_D\bar{\psi}_D)$

if $M_{Z'} \gg m_\mu, m_\tau, M_{\rm DM}$. The total decay rate of Z' is approximately given by

$$\Gamma_{\rm tot}(Z') = \frac{\alpha'}{3} M_{Z'} \times 4(3) \approx \frac{4(\text{or } 3)}{3} \text{ GeV} \left(\frac{\alpha'}{10^{-2}}\right) \left(\frac{M_{Z'}}{100\text{GeV}}\right)$$

$$\begin{aligned} q\bar{q} \text{ (or } e^+e^-) &\to \gamma^*, Z^* \to \mu^+\mu^- Z', \tau^+\tau^- Z' \\ &\to Z^* \to \nu_\mu\bar{\nu}_\mu Z', \nu_\tau\bar{\nu}_\tau Z' \end{aligned}$$

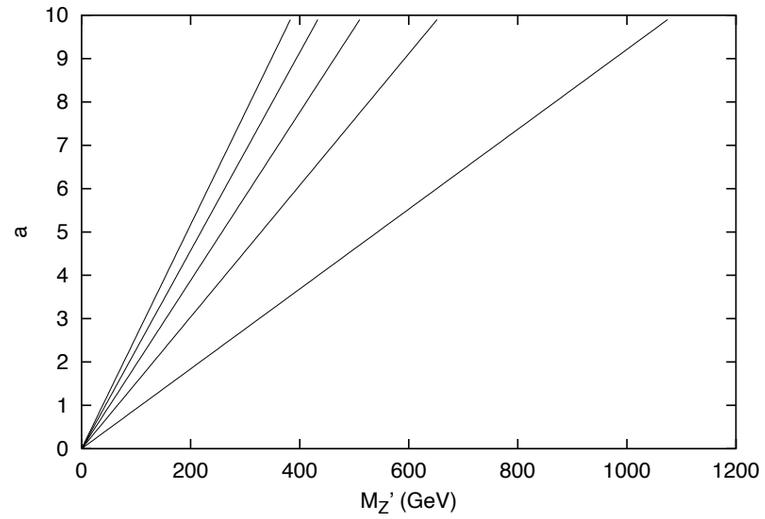


FIG. 2. Δa_μ on the a vs. $m_{Z'}$ plane in case b). The lines from left to right are for Δa_μ away from its central value at $+2\sigma, +1\sigma, 0, -1\sigma$ and -2σ, respectively.

Baek and Ko, arXiv:0811.1646, for PAMELA e^+ excess

$$\mathcal{L}_{\rm Model} = \mathcal{L}_{\rm SM} + \mathcal{L}_{\rm New}$$

$$\mathcal{L}_{\rm New} = -\frac{1}{4} Z'_{\mu\nu} Z'^{\mu\nu} + \overline{\psi_D} i D\cdot\gamma \psi_D - M_{\psi_D}\overline{\psi_D}\psi_D + D_\mu \phi^* D^\mu \phi$$
$$-\lambda_\phi (\phi^*\phi)^2 - \mu_\phi^2 \phi^*\phi - \lambda_{H\phi}\phi^*\phi H^\dagger H.$$

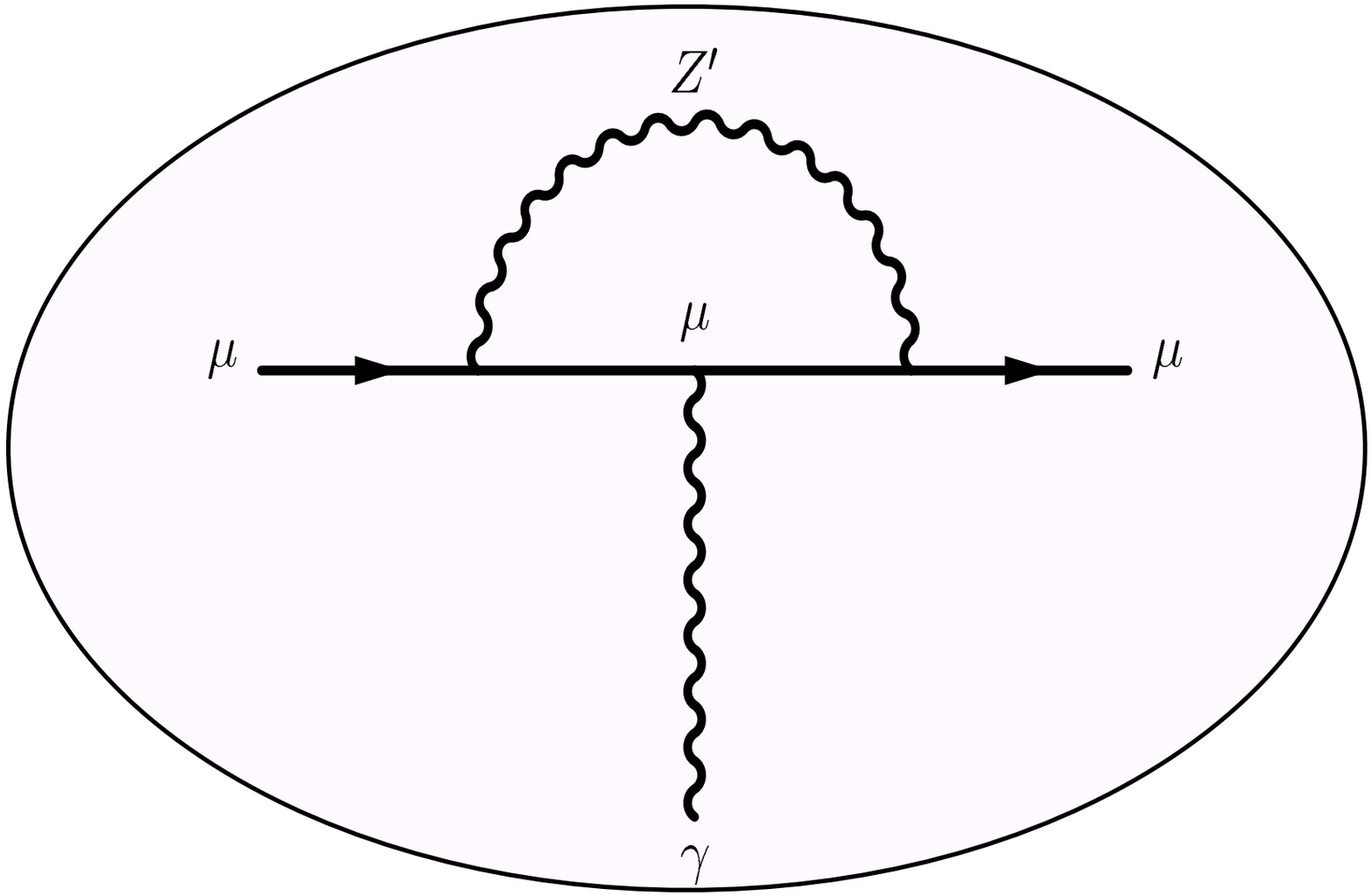
Here we ignored kinetic mixing for simplicity

$$D_\mu = \partial_\mu + ieQA_\mu + i\frac{e}{s_W c_S}(I_3 - s_W^2 Q)Z_\mu + ig' Y' Z'_\mu$$

muon g-2, Leptophilc DM, Collider Signature

Muon (g-2)

$$\Delta a_\mu = a_\mu^{\rm exp} - a_\mu^{\rm SM} = (302 \pm 88) \times 10^{-11}.$$



$$\Delta a_\mu = \frac{\alpha^{'}}{2\pi} \int_0^1 dx \frac{2m_\mu^2 x^2(1-x)}{x^2 m_\mu^2 + (1-x) M_{Z'}^2} \approx \frac{\alpha^{'}}{2\pi} \frac{2m_\mu^2}{3M_{Z'}^2}$$

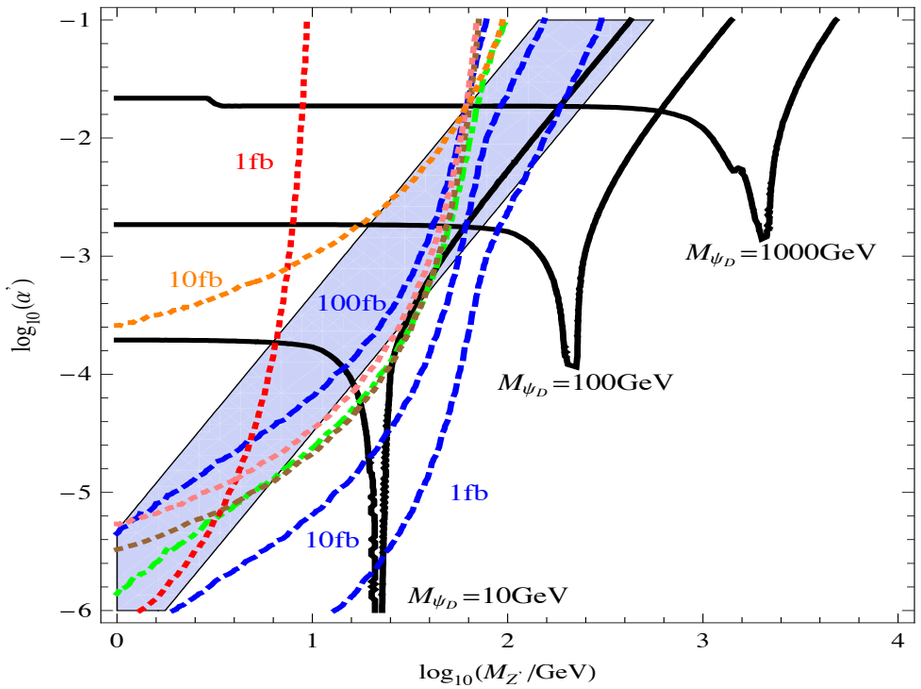


Figure 1: The relic density of CDM (black), the muon $(g-2)_\mu$ (blue band), the production cross section at B factories (1 fb, red dotted), Tevatron (10 fb, green dotdashed), LEP (10 fb, pink dotted), LEP2 (10 fb, orange dotted), LHC (1 fb, 10 fb, 100 fb, blue dashed) and the Z^0 decay width (2.5×10^{-6} GeV, brown dotted) in the $(\log_{10}\alpha', \log_{10} M_{Z'})$ plane. For the relic density, we show three contours with $\Omega h^2 = 0.106$ for $M_{\psi_D} = 10$ GeV, 100 GeV and 1000 GeV. The blue band is allowed by $\Delta a_\mu = (302 \pm 88) \times 10^{-11}$ within 3 σ.

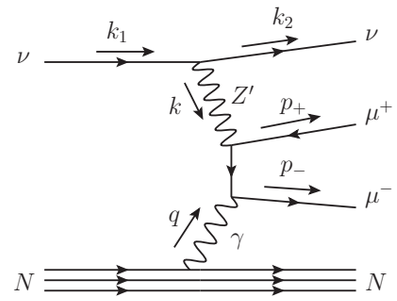


FIG. 1. The leading order contribution of the Z′ to neutrino trident production (another diagram with μ^+ and μ^- reversed i in g' ε

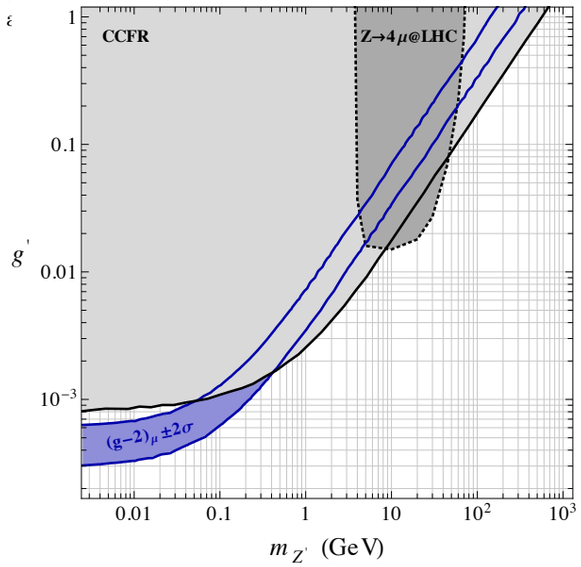


FIG. 2. Parameter space for the Z′ gauge boson. The light-grey area is excluded at 95% C.L. by the CCFR measurement of the neutrino trident cross-section. The grey region with the dotted contour is excluded by measurements of the SM

Seungwon Baek, Pyungwon Ko, arXiv:0811.1646, JCAP(2009) about PAMELA e^+ excess

Altmannshofer et al. arXiv:1406.2332 [hep-ph]

Neutrino trident puts strong constraints on this model

One can evade the neutrino trident constraint, if one introduces New fermions and generate muon g-2 at loop level w/ new fermions !

Z' Only

- Consider light Z' and $g_X \sim (\text{a few}) \times 10^{-4}$ for the muon g-2. Then
- $\chi\bar{\chi} \to Z'^{*} \to f_{\rm SM}\bar{f}_{\rm SM}$: dominant annihilation channel
- $g_X \sim 10^{-4}$ is too small for $\chi\bar{\chi} \to Z'Z'$ to be effective for $\Omega_\chi h^2$
- $m_{Z'} \sim 2m_{\rm DM}$ with the s-channel Z' resonance for the correct relic density
- Many recent studies on this case:

  - Asai, Okawa, Tsumura, 2011.03165
  - Holst, Hooper, Krnjaic, 2107.09067
  - Drees and Zhao, arXiv:2107.14528
  - And some earlier papers

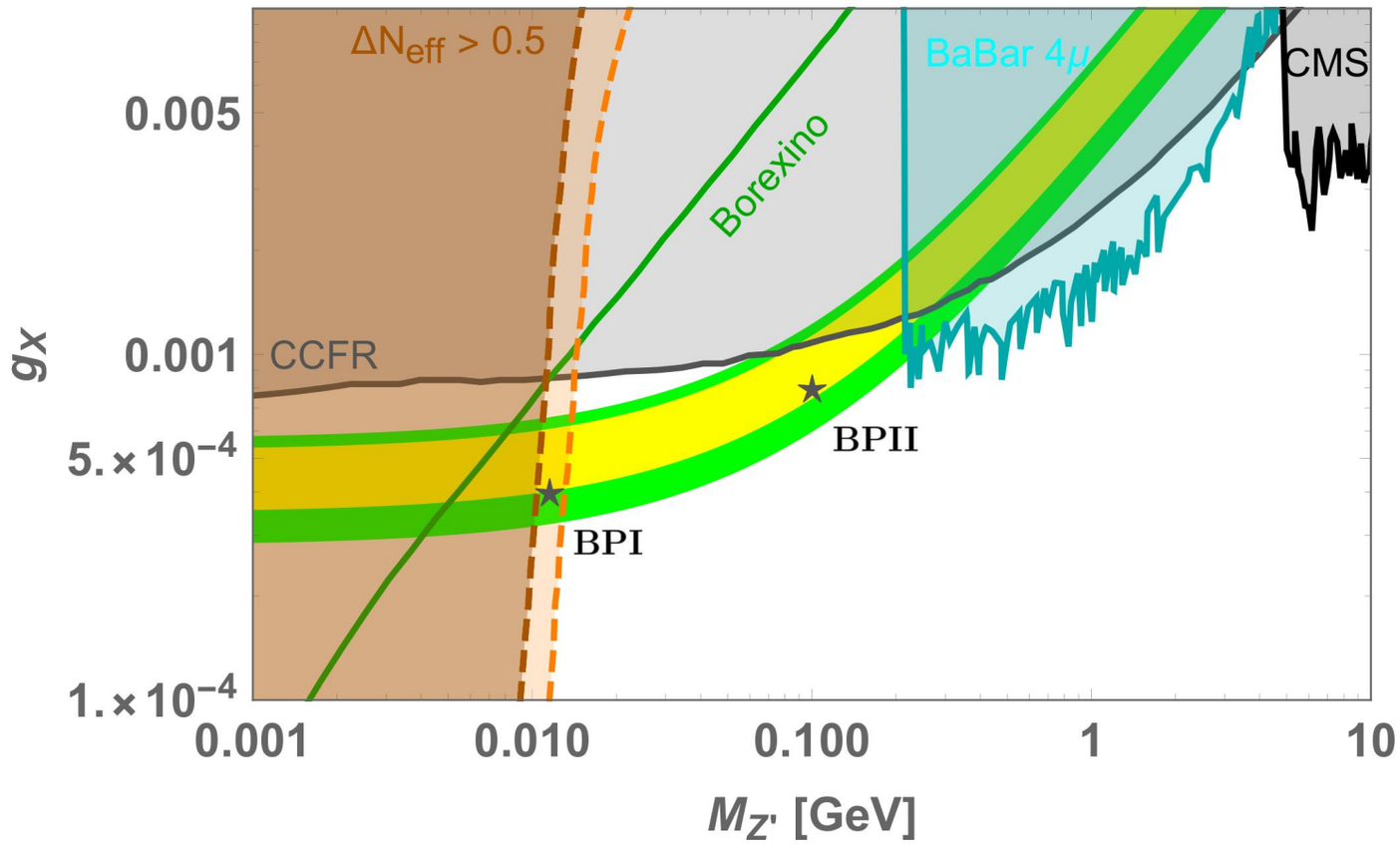


FIG. 1. Regions inside the yellow and Green shaded areas by the Δa_μ are allowed at 1σ and 2σ C.L.. Cyan, black, and orange regions are excluded by other experimental bounds. Above green solid line is ruled out by the Borexino experiment. Region inside the orange area can resolve the Hubble tension. We take two Benchmark Points (BP) $(M_{Z'}, g_X)$ as **BPI** $=(11.5\,\mathrm{MeV}, 4\times10^{-4})$ and **BPII** $= (100\,\mathrm{MeV}, 8\times10^{-4})$.

$U(1)_{L_\mu - L_\tau}$ -charged DM

: Z' only vs. $Z' + \phi$

cf: Let me call Z' , $U(1)_{L_\mu - L_\tau}$ gauge boson,
"dark photon", since it couples to DM

Models with Φ

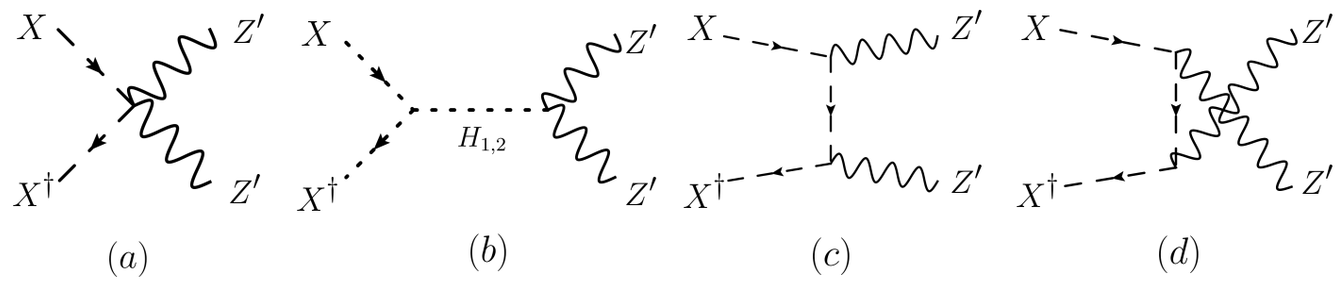
TABLE I: $U(1)$ charge assignments of newly introduced particles and SM particles. The other SM particles are singlet.

Field	Z'_μ	$X(\chi)$	Φ	$L_\mu = (\nu_{L\mu}, \mu_L), \mu_R$	$L_\tau = (\nu_{L\tau}, \tau_L), \tau_R$
spin	1	0 (1/2)	0	1/2	1/2
$U(1)$ charge	0	$Q_X(Q_\chi)$	Q_Φ	+1	-1

We Consider Both Complex Scalar (X) and Dirac Fermion DM (χ)

- Physics depends on Q_Φ , Q_X and Q_χ
- $Q_\Phi = 2Q_{X(\chi)}$ and $3Q_X$ need special cares, since there are extra gauge invariant op's that break $U(1) \to Z_2$, Z_3 after $U(1)$ is spontaneously broken by nonzero VEV of Φ

Complex Scalar DM (generic with $Q_\Phi \neq Q_X, etc$)



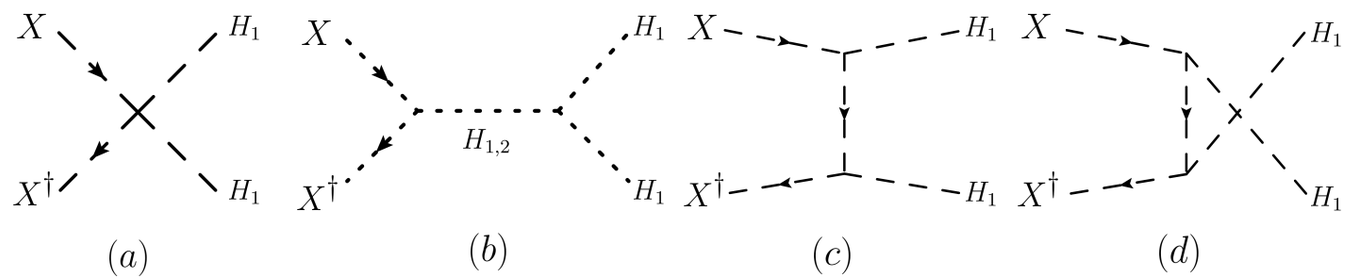


FIG. 2. (*Top*) Feynman diagrams for Complex scalar DM annihilating to a pair of Z' bosons. (*Bottom*) Feynman diagrams for Complex scalar DM annihilating to a pair of H_1 bosons.

$H_2 \simeq H_{125}$ **and** $H_1 \simeq \phi$ **(dark Higgs)**

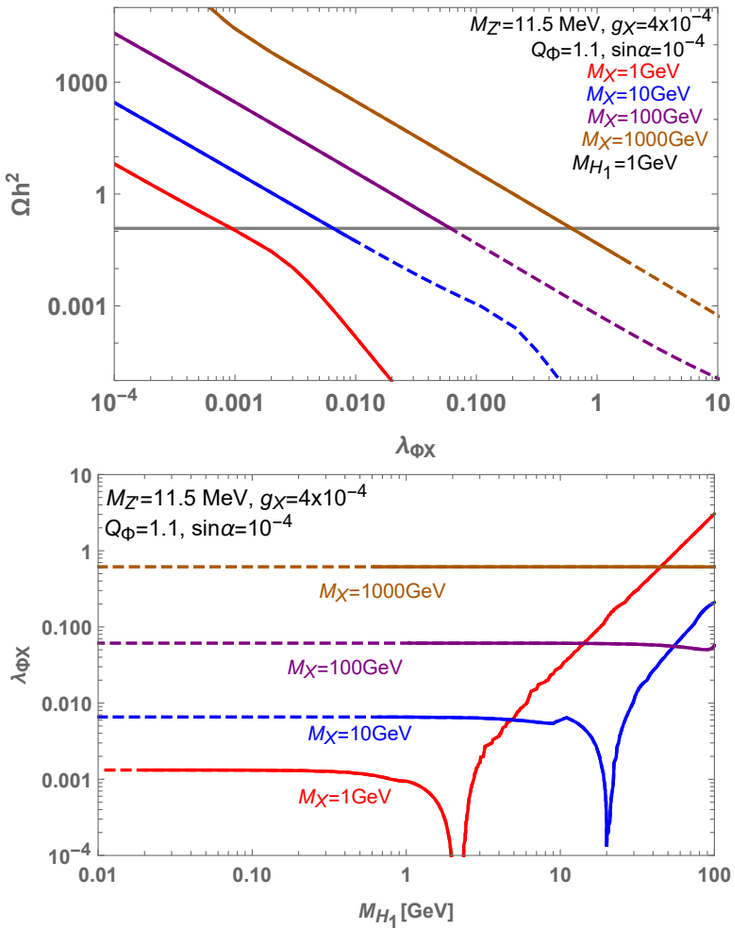


FIG. 3. *Top*: relic abundance of complex scalar DM as functions of $\lambda_{\Phi X}$ for [**BPI**] for $M_X = 1,\ 10, 100,\ 1000$GeV, respectively. We assumed $Q_\Phi = 1.1$, $M_{H_1} = 1$GeV, and $\sin\alpha = 10^{-4}$. Solid (Dashed) lines represent the region where bounds on DM direct detection are satisfied (ruled out). *Bottom*: the preferred parameter space in the $(M_{H_1}, \lambda_{\Phi X})$ plane for $\lambda_{HX} = 0$.

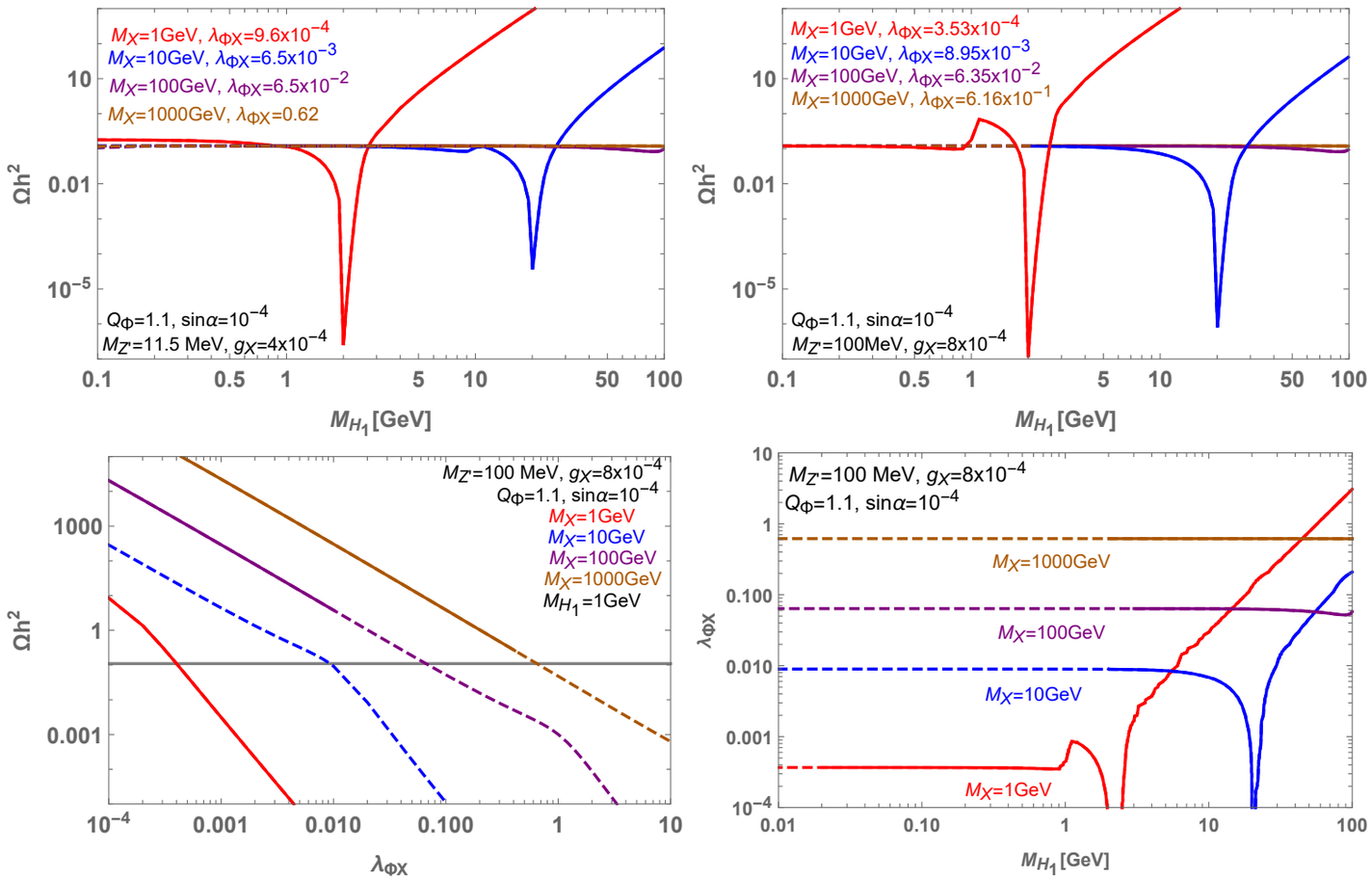


FIG. 7. The (*Top*) plots show the relic abundance of complex scalar DM for $Q_\Phi = 1.1$ as functions of dark Higgs mass M_{H_1} for [**BPI**] (*Left*) and [**BPII**] (*Right*). The (*Bottom*) plots show the relic density as functions of $\lambda_{\Phi X}$ (*Left*) and the preferred parameter space in the $(M_{H_1}, \lambda_{\Phi X})$ plane for $\lambda_{HX} = 0$ (*Right*) for [**BPII**] . We take four different DM masses, $M_X = 1,\ 10, 100,\ 1000$GeV, respectively. Solid (Dashed) lines represent the region where bounds on DM direct detection are satisfied (ruled out).

DM mass : much wider range than $m_{Z'} \sim 2m_{\rm DM}$ due to dark Higgs boson contributions

Complex Scalar DM:

$U(1)_{L_\mu - L_\tau} \to Z_2$ ($Q_\Phi = 2Q_X$)

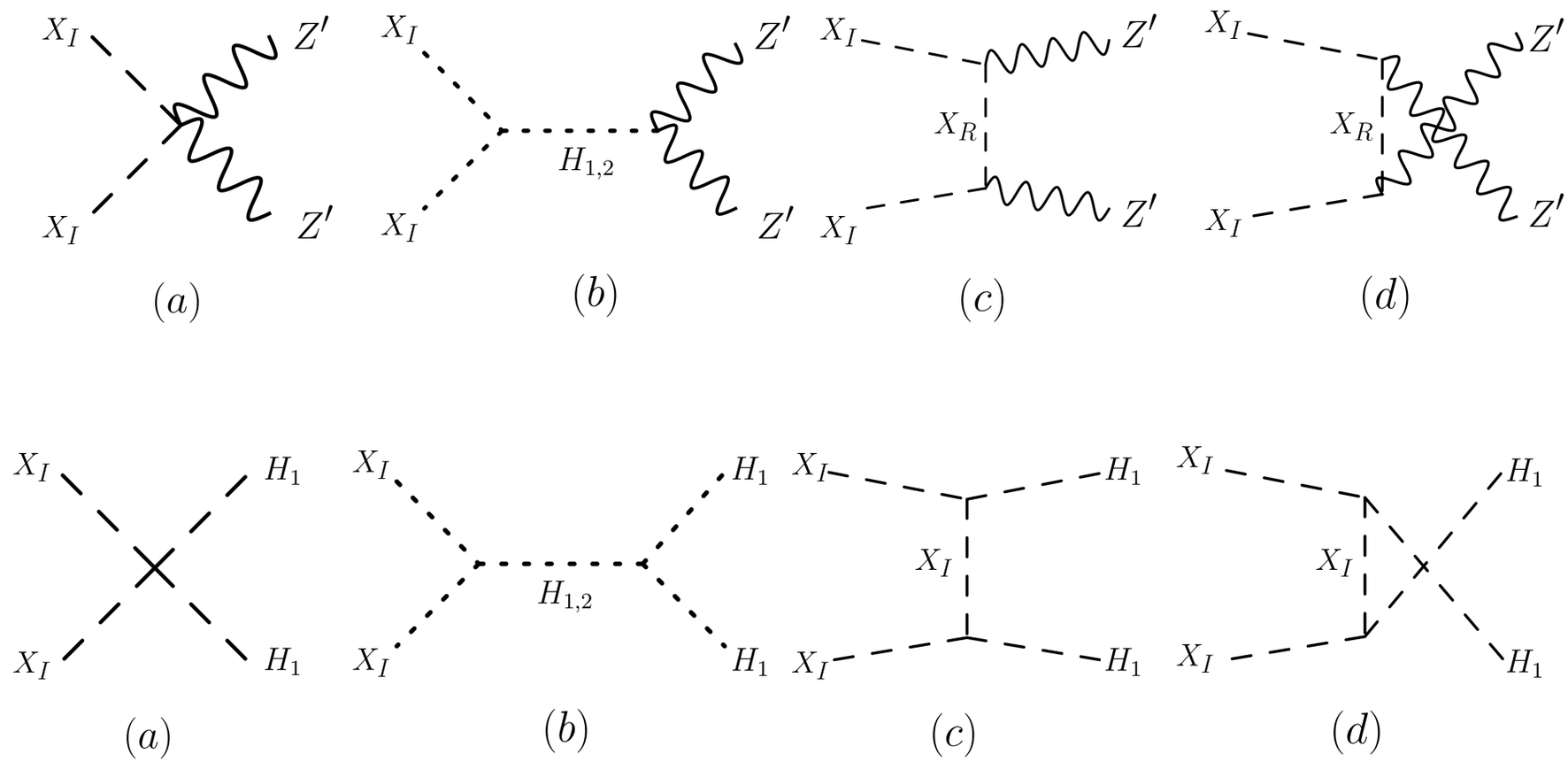


FIG. 8. (*Top*) Feynman diagrams for local Z_2 scalar DM annihilatiing to a pair of Z' bosons. (*Bottom*) Feynman diagrams for local Z_2 scalar DM annihilatiing to a pair of H_1 bosons, which is mostly dark Higgs-like.

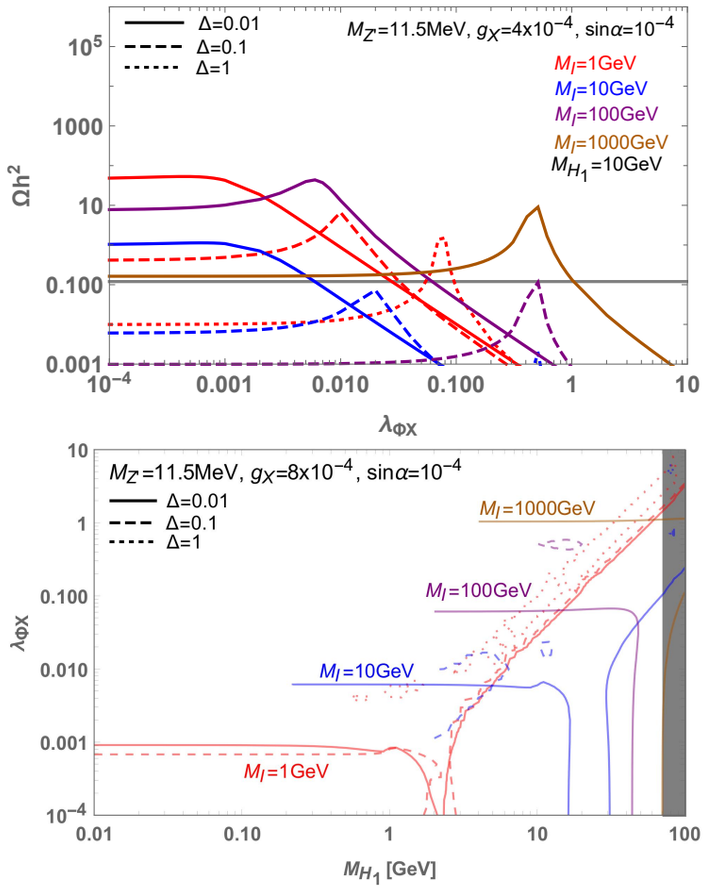


FIG. 4. *Top*: Relic abundance of local Z_2 scalar DM as functions of $\lambda_{\Phi X}$ for [**BPI**] and different values of mass splittings (Δ). We take $\lambda_{HX} = 0$, $M_{H_1} = 10$GeV, and $s_\alpha = 10^{-4}$. All the curves satisfy the DM direct detection bound. *Bottom*: The preferred parameter space in the $(M_{H_1}, \lambda_{\Phi X})$ plane for different values of Δ. The gray area is excluded by the perturbative condition.

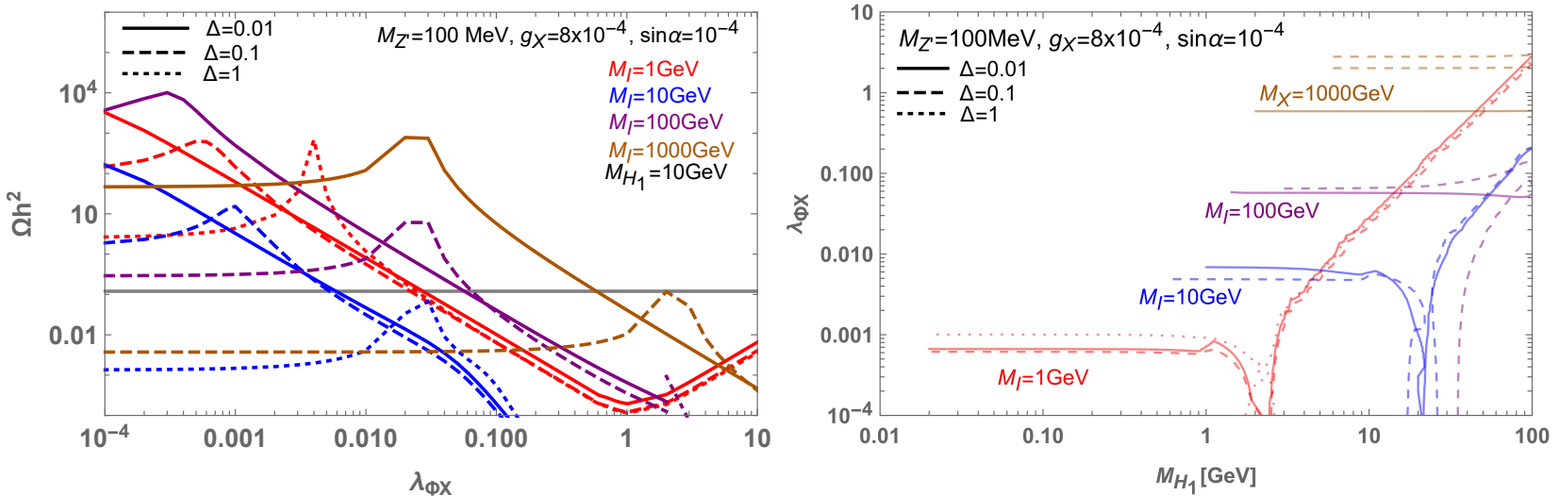


FIG. 9. (*Left*) Relic abundance of local Z_2 scalar DM in case of [**BPII**]. We take $\lambda_{HX} = 0$, $M_{H_1} = 10$GeV, and $s_\alpha = 10^{-4}$. All the lines satisfy the DM direct detection bound. (*Right*) Relic abundance of local Z_2 scalar DM in the $(M_{H_1}, \lambda_{\Phi X})$ plane.

DM mass : much wider range than $m_{Z'} \sim 2m_{\rm DM}$ due to dark Higgs boson contributions

Complex Scalar DM:

$U(1)_{L_\mu - L_\tau} \to Z_3$ ($Q_\Phi = 3Q_X$)

Local Z_3 DM Model : first considered by Ko, Tang: arXiv:1402.6449 (SIDM), 1407.5492 (GC γ-ray excess)

$$V = -\mu_H^2 H^\dagger H + \lambda_H \left(H^\dagger H\right)^2 - \mu_\phi^2 \phi_X^\dagger \phi_X + \lambda_\phi \left(\phi_X^\dagger \phi_X\right)^2 + \mu_X^2 X^\dagger X + \lambda_X \left(X^\dagger X\right)^2$$
$$+ \lambda_{\phi H} \phi_X^\dagger \phi_X H^\dagger H + \lambda_{\phi X} X^\dagger X \phi_X^\dagger \phi_X + \lambda_{HX} X^\dagger X H^\dagger H + \left(\lambda_3 X^3 \phi_X^\dagger + H.c.\right) \quad (2.1)$$

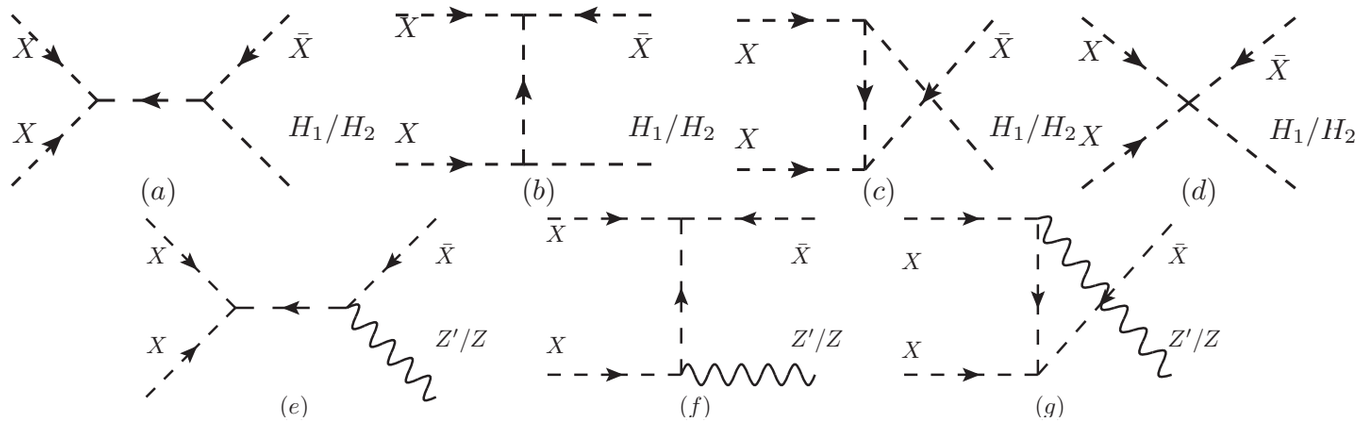
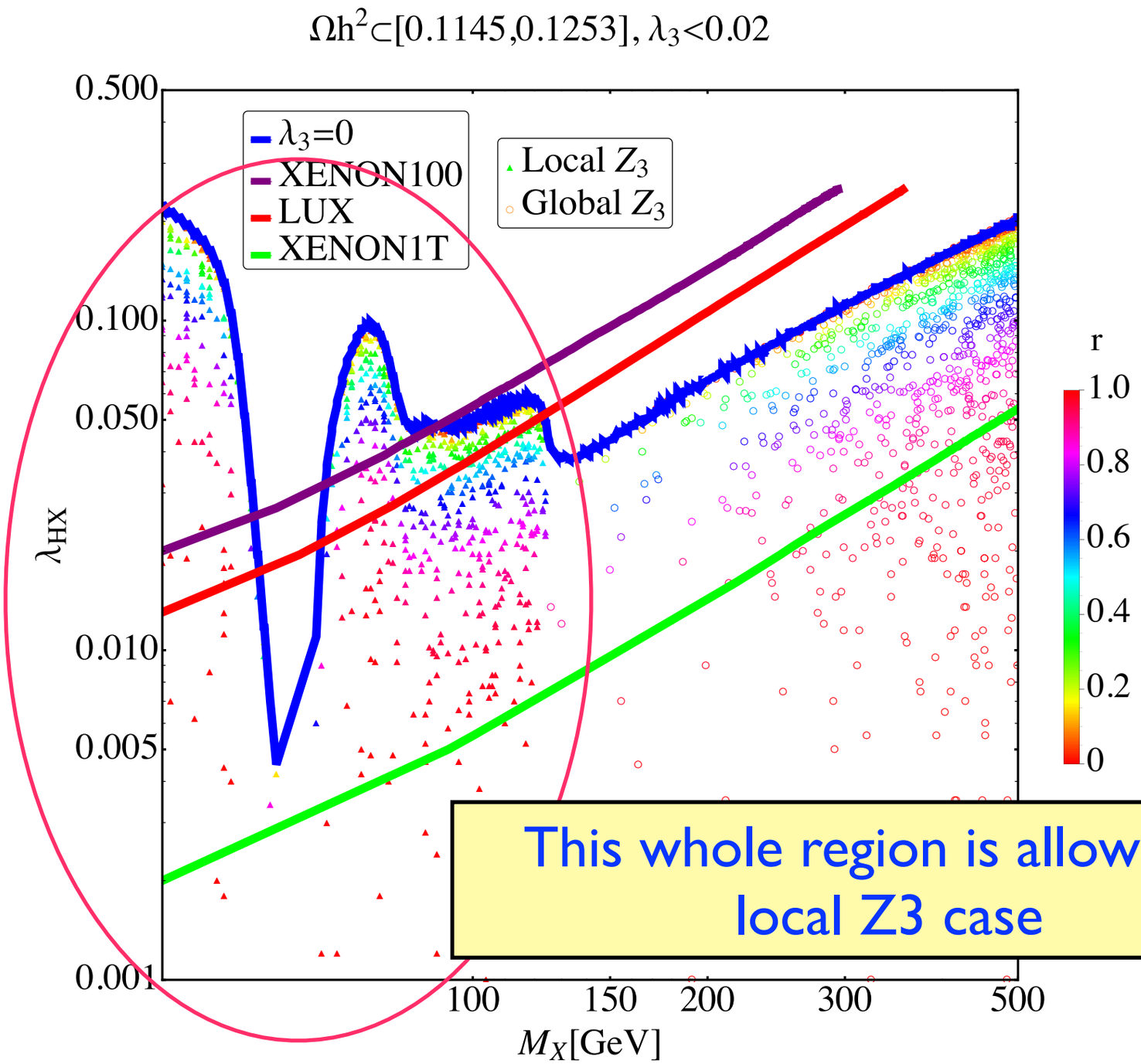


FIG. 1: Feynman diagrams for dark matter semi-annihilation. Only (a), (b), and (c) with H_1 as final state appear in the global Z_3 model, while all diagrams could contribute in local Z_3 model.

ϕ and Z' : present only in models with dark gauge symmetries, And not in models with global dark symmetries

Dark $U(1) \to Z_3$



This whole region is allowed in local Z3 case

- Blue band marks the upper bound,
- All points are allowed in our local Z3 model,1402.6449
- only circles are allowed in global Z3 model,1211.1014

$$r \equiv \frac{1}{2} \frac{v\sigma^{XX \to X^* Y}}{v\sigma^{XX^* \to YY} + \frac{1}{2} v\sigma^{XX \to X^* Y}}.$$

$U(1)_{L_\mu - L_\tau} \to Z_3$

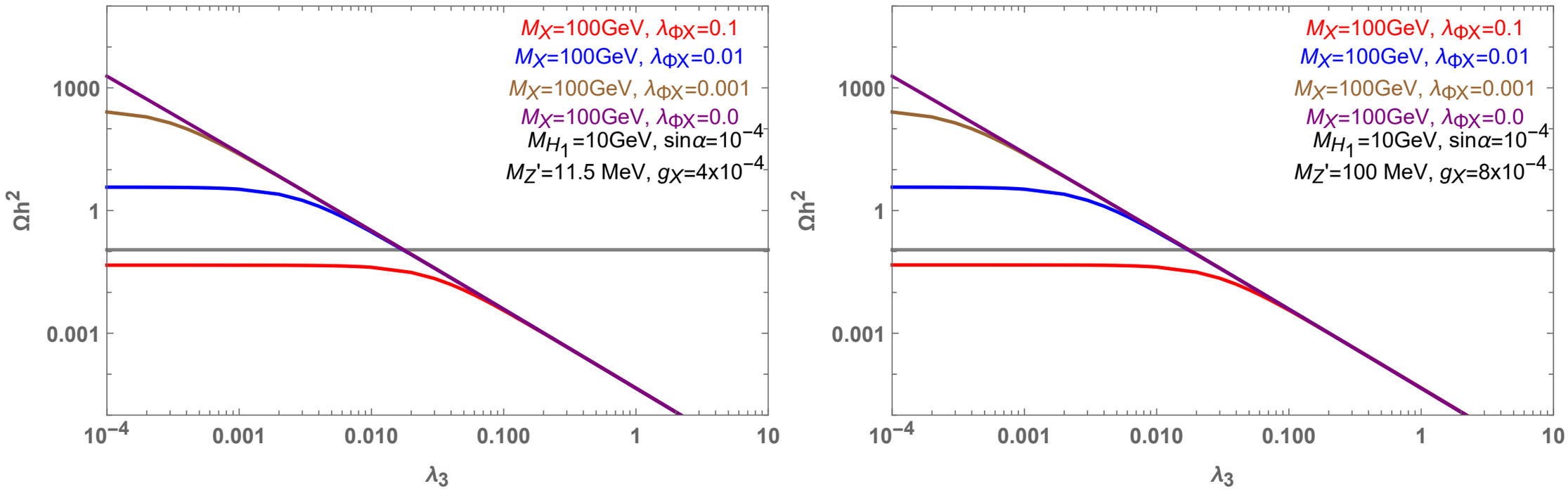


FIG. 10. Relic abundance of Z_3 scalar DM for the [**BPI**] (*Left*) and the [**BPII**] (*Right*), respectively. Here we fixed $\lambda_{HX} = 0$ for simplicity.

- $g_X \sim O(10^{-4})$: very small. $XX \to X^\dagger Z'$ is not important
- λ_3 controlling $XX \to X^\dagger H_1$ is an important parameter

DM mass : much wider range than $m_{Z'} \sim 2m_{\rm DM}$ due to dark Higgs boson contributions

Dirac fermion DM:

$$U(1)_{L_\mu - L_\tau} \to Z_2 \; (Q_\Phi = 2Q_\chi)$$

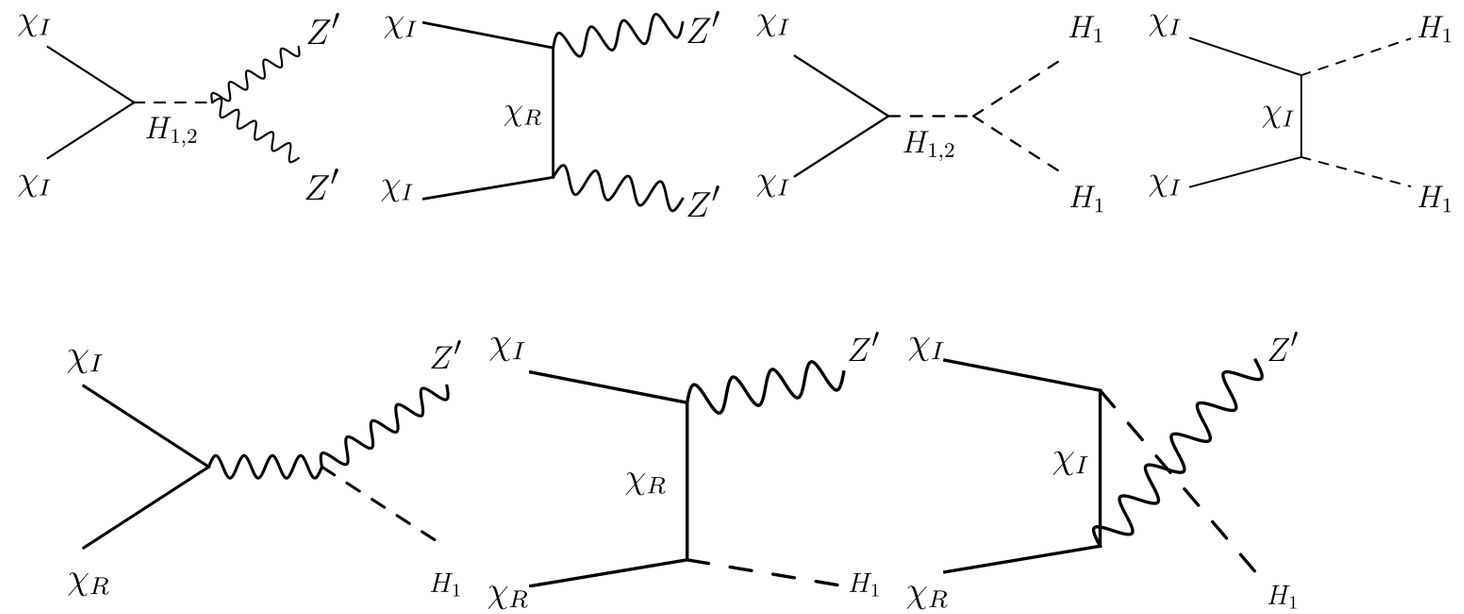


FIG. 5. Feynman diagrams of local Z_2 fermion DM (co-)annihilating into a pair of Z' bosons and H_1 bosons (*Top*), and $Z' + H_1$ (*Bottom*).

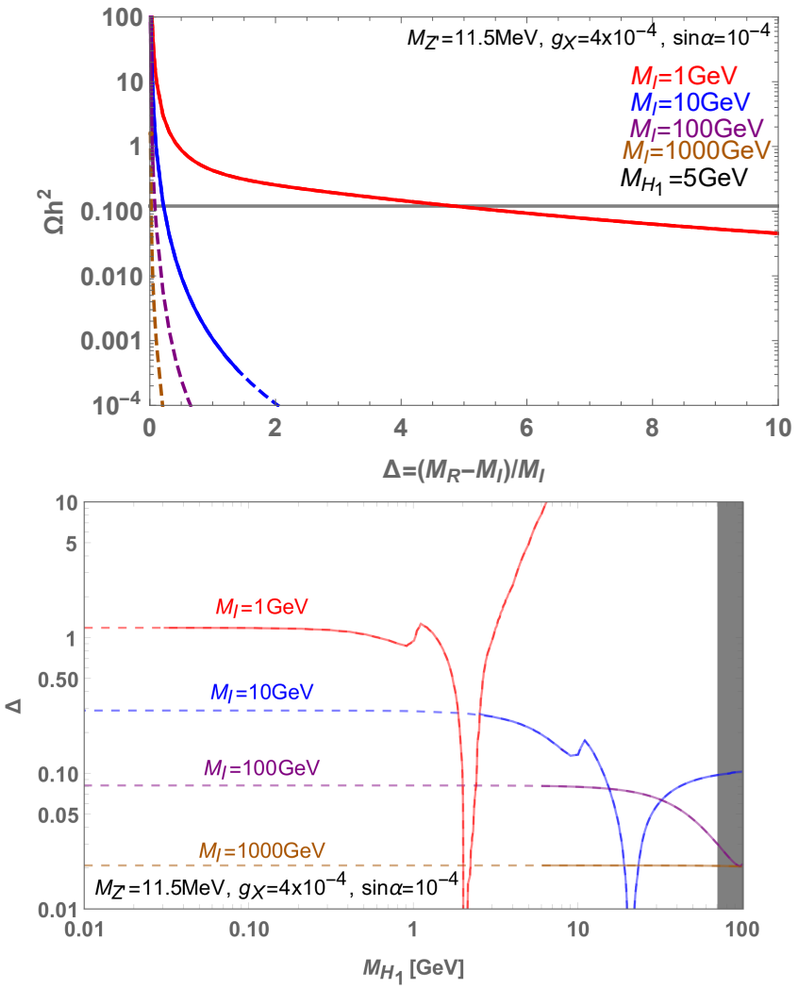


FIG. 6. *Top*: Dark matter relic density as functions of mass splitting Δ for [**BPI**] and for different values of DM mass, $M_I = 1, 10, 100, 1000$GeV. Solid (Dashed) lines denote the region where bounds on DM direct detection are satisfied (ruled out). *Bottom*: Preferred parameter space in the (M_{H_1}, Δ) plane for different DM masses. The gray region is ruled out by the perturbativity condition on λ_Φ.

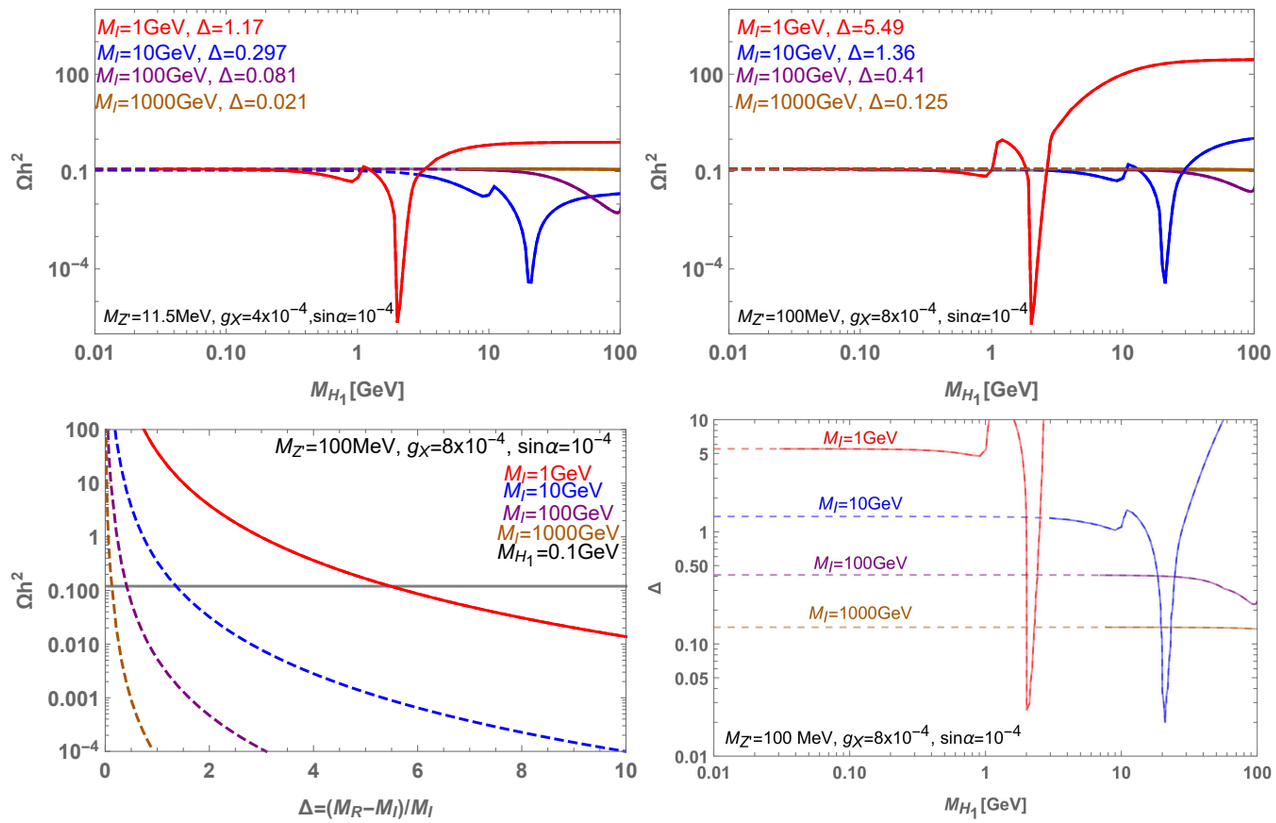


FIG. 11. (*Top*) Dark matter relic density as functions of dark Higgs mass M_{H_1} for [**BPI**] (*Left*) and [**BPII**] (*Right*) (*Bottom-Left*) Dark matter relic density as functions of Δ for [**BPII**], and *(Bottom-right)* Preferred parameter region in the (Δ, M_{H_1}) plane. Solid (Dashed) lines denote the region where bounds on DM direct detection are satisfied (ruled out).

DM mass : much wider range than $m_{Z'} \sim 2m_{\rm DM}$ due to dark Higgs boson contributions

Conclusion

- DM physics with massive dark photon can not be complete without including dark gauge symmetry breaking mechanism, e.g. dark Higgs field ϕ, which have been largely ignored by DM community (or some ways other than dark Higgs to provide dark photon mass)

- Many examples show the importance of ϕ in DM phenomenology, astroparticle physics and cosmology

- Once ϕ is included, can accommodate the muon g-2 and thermal DM without the s-channel resonance condition $m_{Z'} \sim 2m_{\rm DM}$

- $m_{\rm DM}$: essentially free, whereas $m_{Z'} \sim O(10-100)$ MeV and $g_X \sim O(10^{-4})$ can explain the muon (g-2)

Higgs-Portal Assisted Higgs Inflation

arXiv:1405.1635 [hep-ph], JCAP02 (2017) 003

With Jinsu Kim, Wan-Il Park

Higgs Inflation

- Inflation : the main paradigm for very early Universe
- But no very compelling inflation scenarios based on high energy physics
- SM Higgs boson can play a role of inflaton if it has large non minimal coupling [Bezrukov, Shaposhnikov (2007)] or non canonical kinetic term
- Merits: Minimal model, Consistent with Planck data, Can connect low energy ($m_{\rm EW}$) scale to high energy (inflation) scale

Higgs Inflation in SM

(before BICEP2) [Bezrukov and Shaposhnikov, 0710.3755]

$$\frac{\mathcal{L}}{\sqrt{-g}} = -\frac{1}{2\kappa}\left(1+\xi\frac{h^2}{M_{\rm Pl}^2}\right)R+\mathcal{L}_h$$

Nonminimal coupling

$$\epsilon = \frac{M_P^2}{2}\left(\frac{dU/d\chi}{U}\right)^2 \simeq \frac{4M_P^4}{3\xi^2 h^4}$$

$$\eta = M_P^2\frac{d^2U/d\chi^2}{U} \simeq -\frac{4M_P^2}{3\xi h^2}\,,$$

$$\Rightarrow \epsilon \simeq \frac{3}{4}\eta^2$$

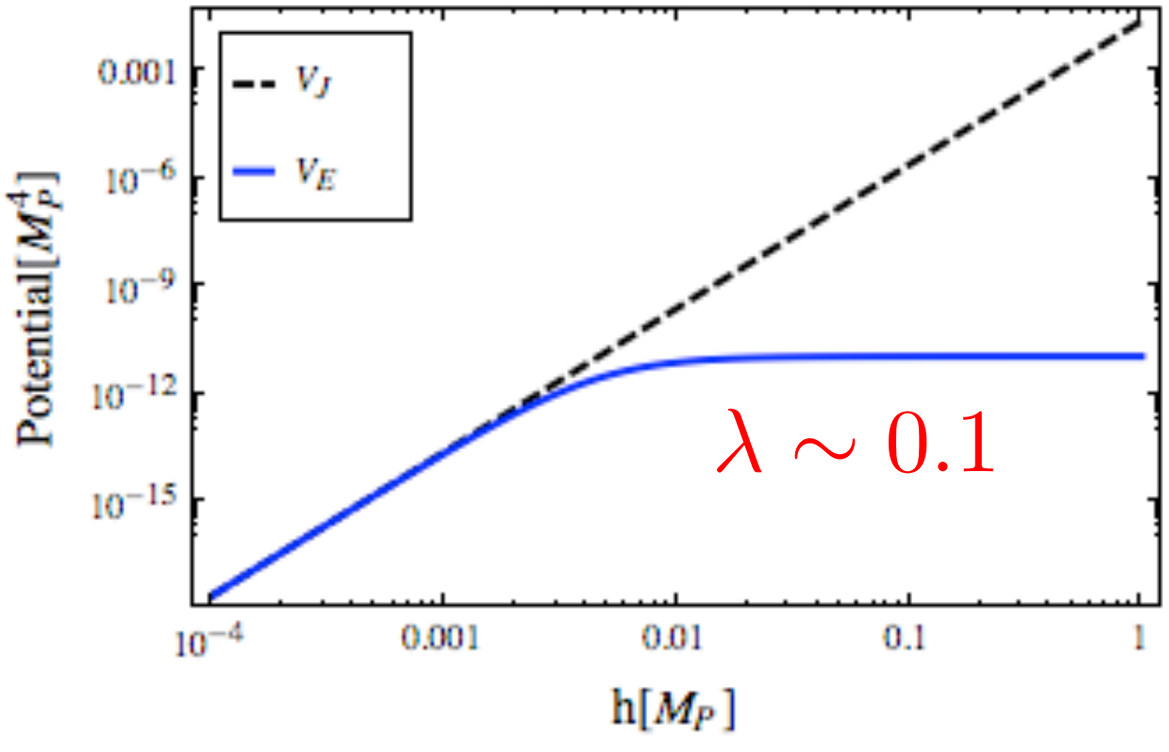
$$n_s = 1-6\epsilon+2\eta \sim 0.96$$

$$\Rightarrow \eta \simeq \frac{1}{2}\left(n_s-1\right)$$

$$\Rightarrow \epsilon \simeq \frac{3}{16}\left(n_s-1\right)^2$$

$$\Rightarrow r \simeq 16\epsilon \simeq 3\left(n_s-1\right)^2 \sim 5\times 10^{-3}$$

$$U(\chi) = \frac{1}{\Omega(\chi)^4}\frac{\lambda}{4}\left(h(\chi)^2-v^2\right)^2$$



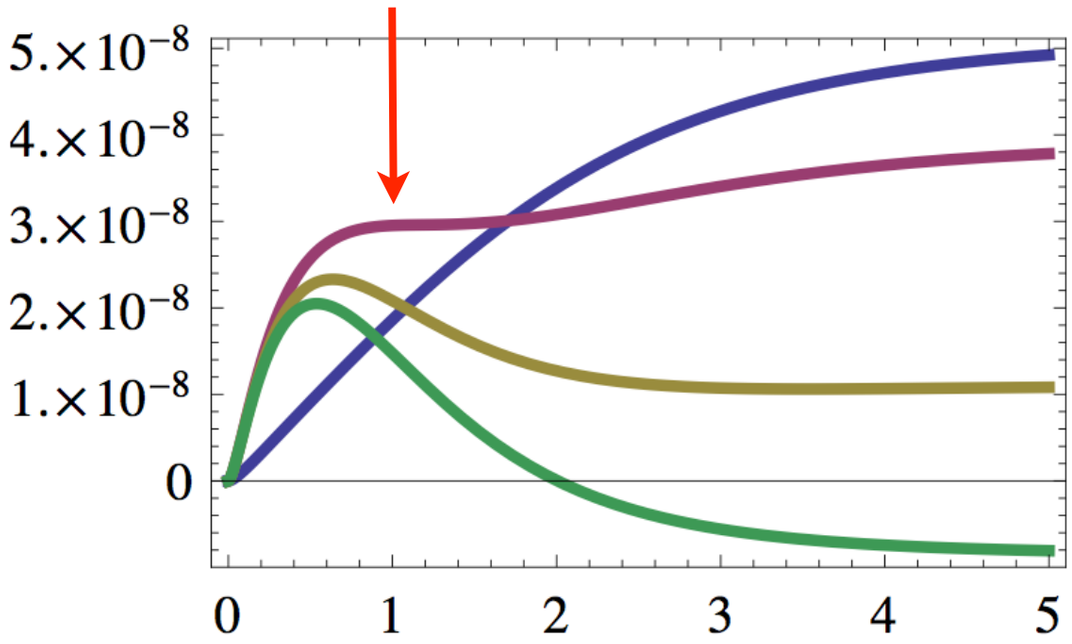
Higgs Inflation in SM

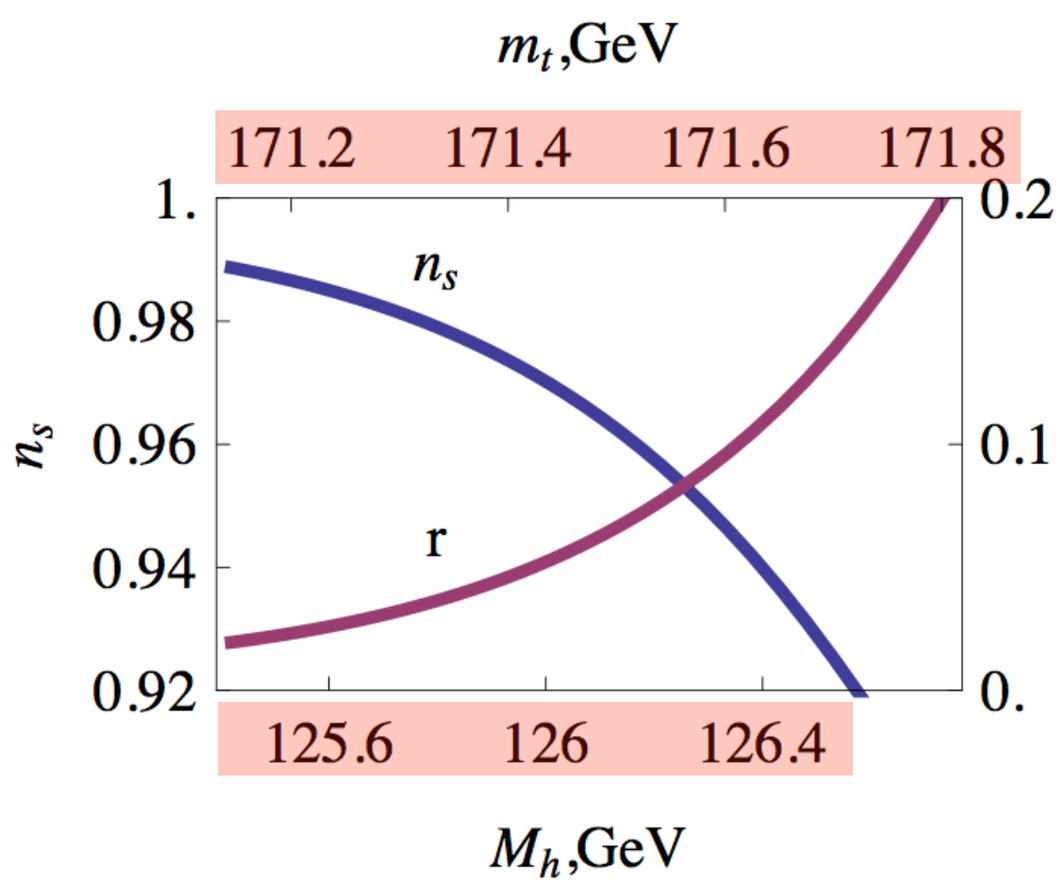
(after BICEP2)

$r_{\rm BICEP2} \sim 0.1$ ⇨ Is Higgs inflation ruled out? No!

$$U(h) = \frac{\lambda}{4\Omega^4}\left(h^2 - v_H^2\right) \to \frac{\lambda(\mu)}{4\Omega^4}\left(h^2 - v_H^2\right)$$

[Hamada, Kawai, Oda and Park, 1403.5043; Bezrukov and Shposhnikov, 1403.6078]





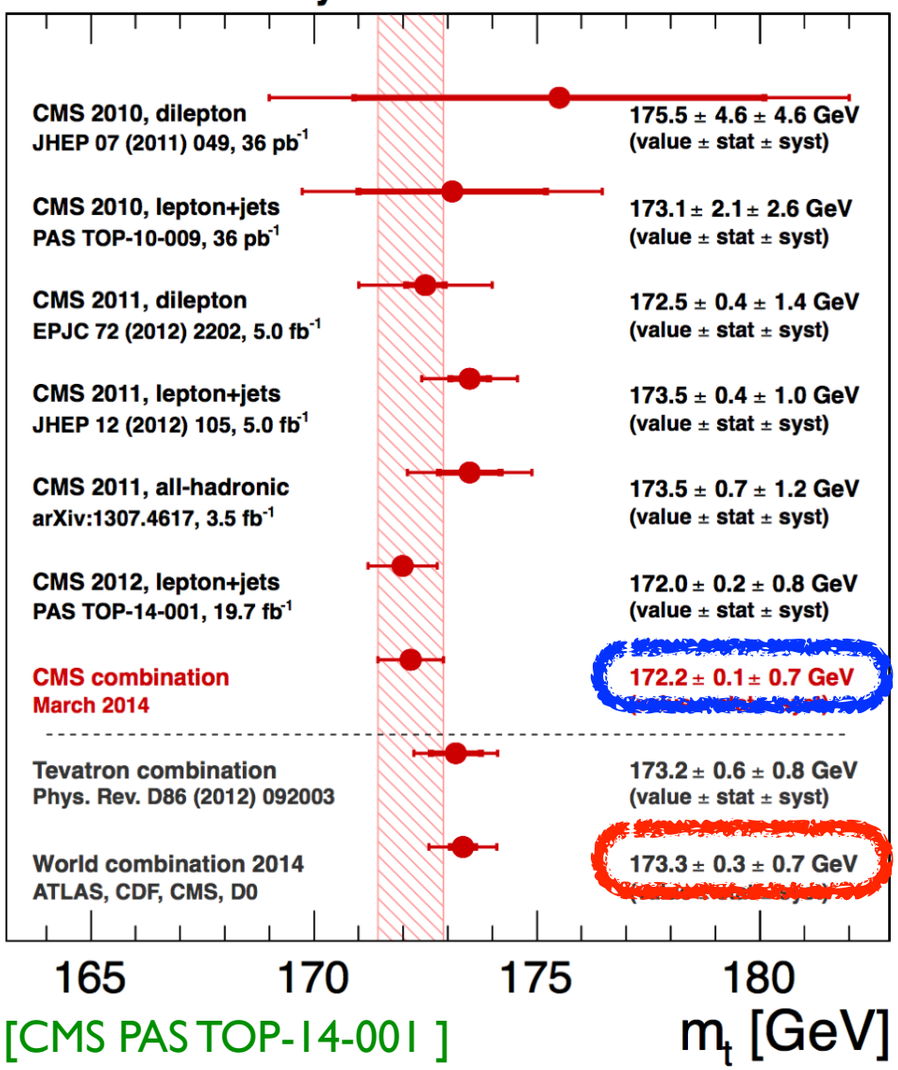
Effects of running on slow-roll parameters

$$\epsilon = \frac{M_{\rm Pl}^2}{2}\left(\frac{dh}{d\chi}\frac{dU}{dh}\right)^2 = \frac{1}{2}\left(4+\frac{\beta_\lambda}{\lambda_H}\right)^2 \frac{M_{\rm Pl}^2/h^2}{\sqrt{\Omega^2+6\xi^2h^2/M_{\rm Pl}^2}} \approx \frac{1}{12}\left(4+\frac{\beta_\lambda}{\lambda_H}\right)^2 \frac{M_{\rm Pl}^4}{\xi^2 h^4} \tag{17}$$

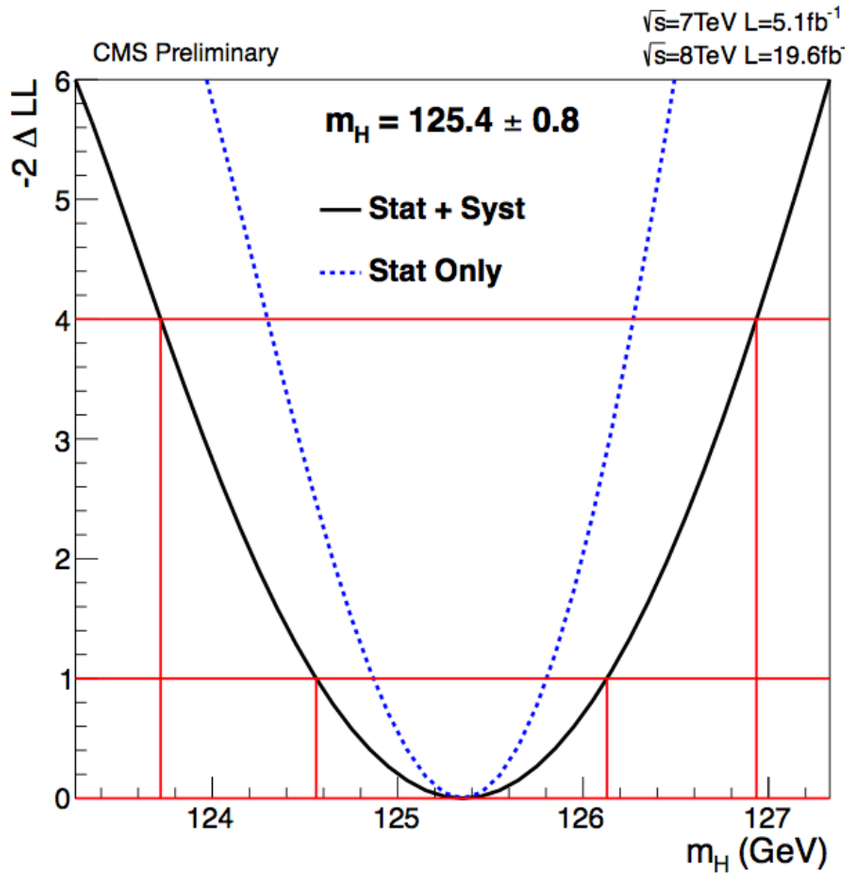
$$\begin{aligned}\eta &= \frac{M_{\rm Pl}^2}{U}\frac{dh}{d\chi}\frac{d}{dh}\left(\frac{dh}{d\chi}\frac{dU}{dh}\right) \\ &= \left(4+\frac{\beta_\lambda}{\lambda_H}\right)\frac{M_{\rm Pl}^2}{h^2}\frac{\Omega^2}{\Omega^2+6\xi^2h^2/M_{\rm Pl}^2}\left\{\frac{1}{\Omega^2}\frac{\beta_\lambda}{\lambda_H}\left[1+\frac{d\ln\left(\beta_\lambda/\lambda_H\right)/d\ln\varphi}{4+\beta_\lambda/\lambda_H}\right]+3-2\frac{d\ln\Omega^2}{d\ln h}-\frac{\xi\left(1+6\xi\right)h^2/M_{\rm Pl}^2}{1+\xi\left(1+6\xi\right)h^2/M_{\rm Pl}^2}\right\} \\ &\simeq -\frac{1}{3}\left(4+\frac{\beta_\lambda}{\lambda_H}\right)\frac{M_{\rm Pl}^2}{\xi h^2}\left\{1-\frac{M_{\rm Pl}^2}{2\xi h^2}\frac{\beta_\lambda}{\lambda_H}\left[1+\frac{d\ln\beta_\lambda/d\ln\varphi-\beta_\lambda/\lambda_H}{4+\beta_\lambda/\lambda_H}\right]\right\}\end{aligned} \tag{18}$$

ϵ & η are independent

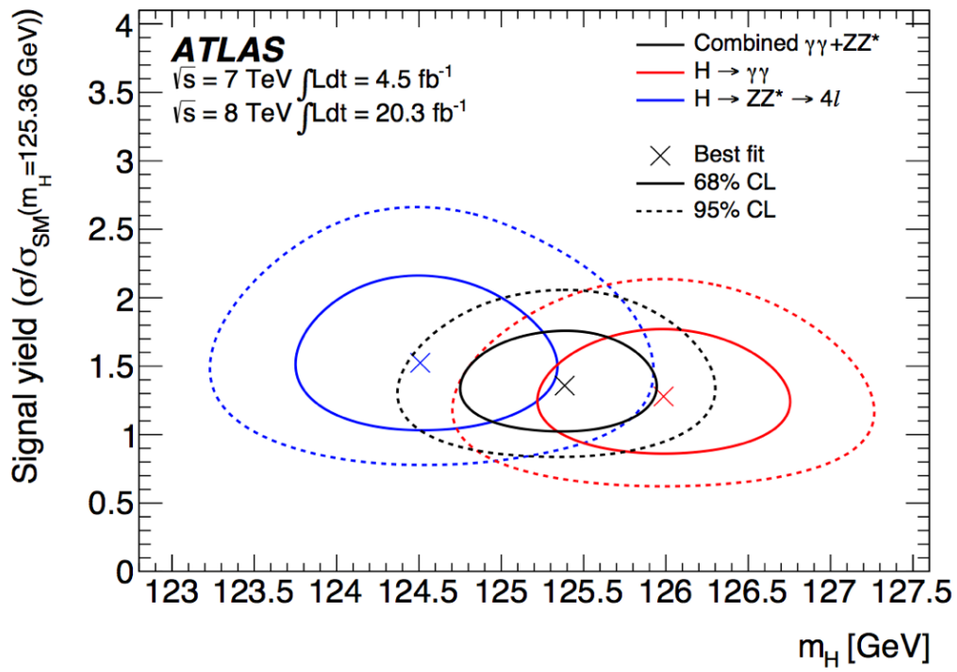
However m_t and m_h are tightly constrained!



[CMS PAS TOP-14-001]



[CMS PAS HIG-13-001]



[1406.3827]

In SM, our vacuum is likely to be meta-stable.

Higgs portal interaction

$$V \supset \lambda_{\Phi H} |\Phi|^2 H^\dagger H$$

Scalar mixing

$$\lambda_H = \left[1 - \left(1 - \frac{m_\phi^2}{m_h^2}\right) \sin^2 \alpha\right] \lambda_H^{\rm SM}$$

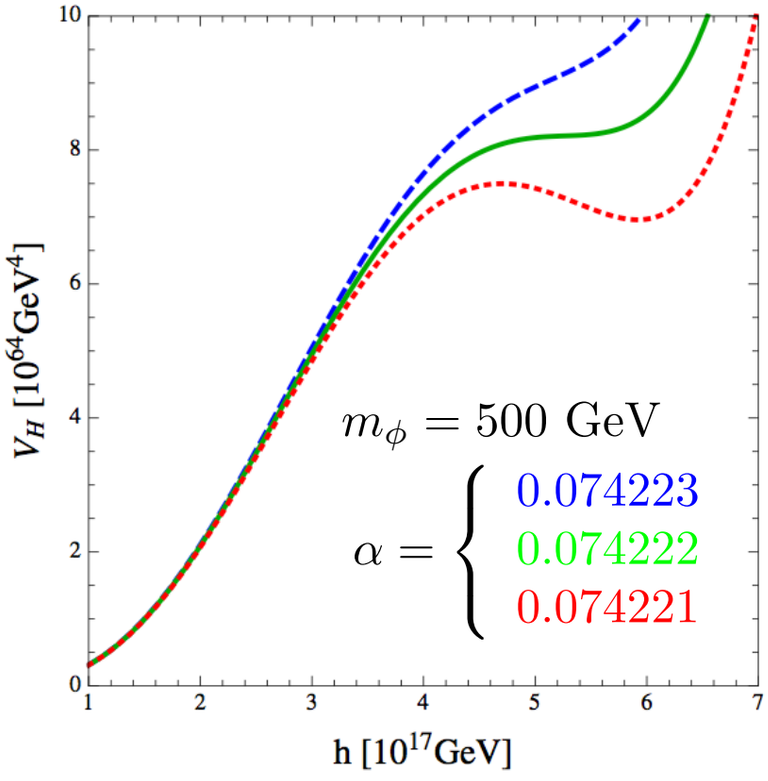
$\Rightarrow \lambda_H > \lambda_H^{\rm SM}$ for $m_\phi > m_h$ & $\alpha \neq 0$

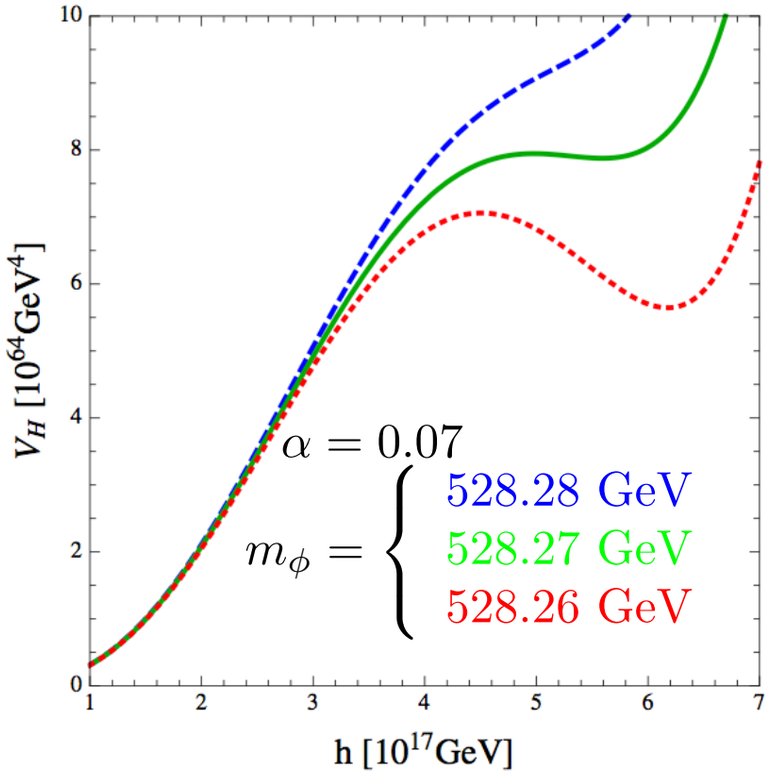
⇒ Vacuum instability along the Higgs direction is easily removed.

⇒ Higgs inflation consistent with BICEP2 is possible for a wide range of m_t and M_h

Higgs portal interaction disconnect m_t and M_h from inflationary observables.

Higgs-portal Higgs inflation

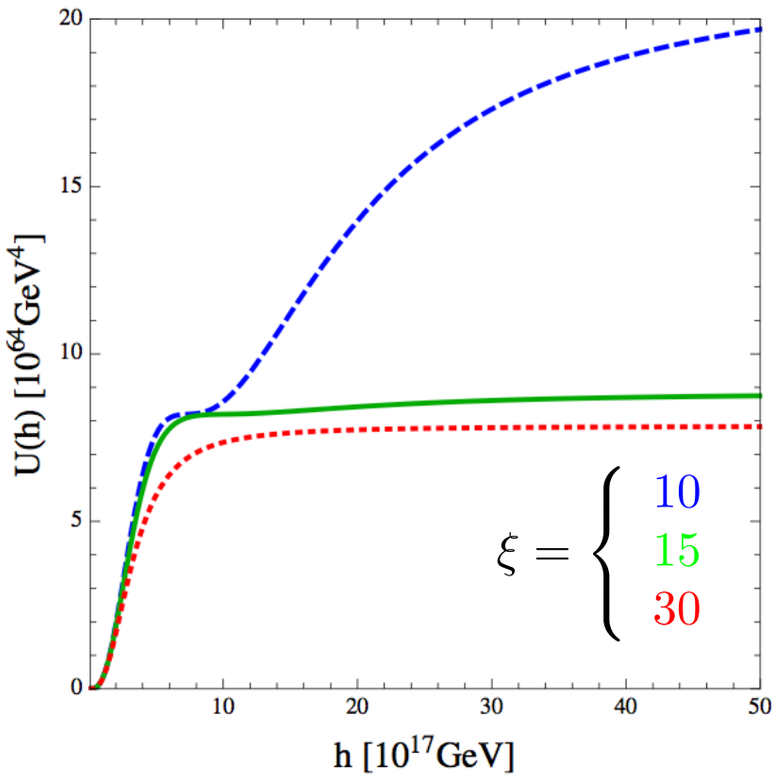




$m_t = 173.2$ GeV
$M_h = 125.5$ GeV

* Inflection point control

(α, m_ϕ) & $\lambda_{\Phi H}$



Result of numerical analysis

$k_* \times$ Mpc	N_e	$h_*/M_{\rm Pl}$	ϵ_*	η_*	$10^9 P_S$	n_s	r
0.002	59	0.83	0.00448	−0.02465	2.2639	0.9238	0.0717
0.05	56	0.72	0.00525	−0.00190	2.1777	0.9647	0.0840

- Result depends very sensitively on α, m_Φ and $\lambda_{\Phi H}$ -

Higgs Portal Higgs Inflation can have $r \lesssim O(0.1)$ without resorting to m_t and M_h.

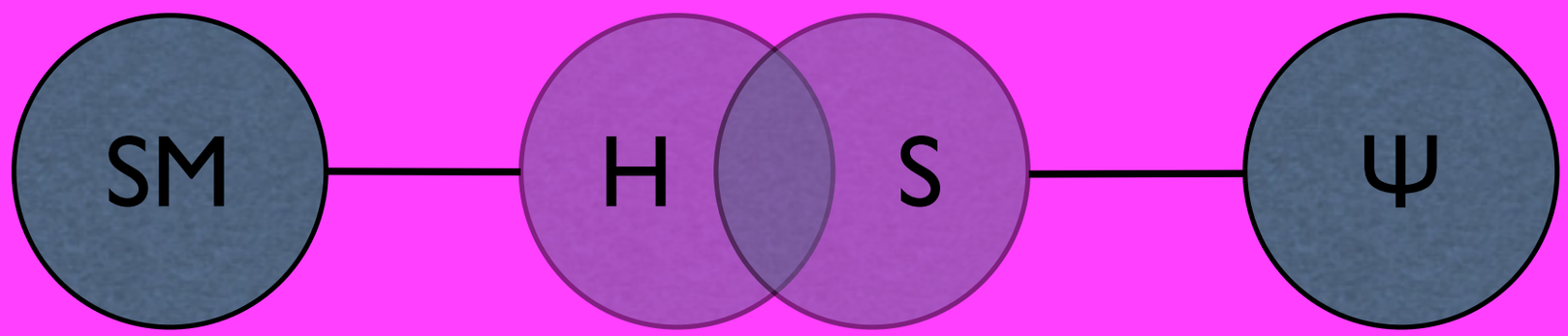
Singlet fermion CDM

Baek, Ko, Park, arXiv:1112.1847

$$\mathcal{L} = \mathcal{L}_{\rm SM} - \mu_{HS} S H^\dagger H - \frac{\lambda_{HS}}{2} S^2 H^\dagger H$$
$$+\frac{1}{2}(\partial_\mu S \partial^\mu S - m_S^2 S^2) - \mu_S^3 S - \frac{\mu'_S}{3} S^3 - \frac{\lambda_S}{4} S^4$$
$$+\overline{\psi}(i\ \partial\!\!\!/ - m_{\psi_0})\psi - \lambda S \overline{\psi}\psi$$

mixing

invisible decay



Production and decay rates are suppressed relative to SM.

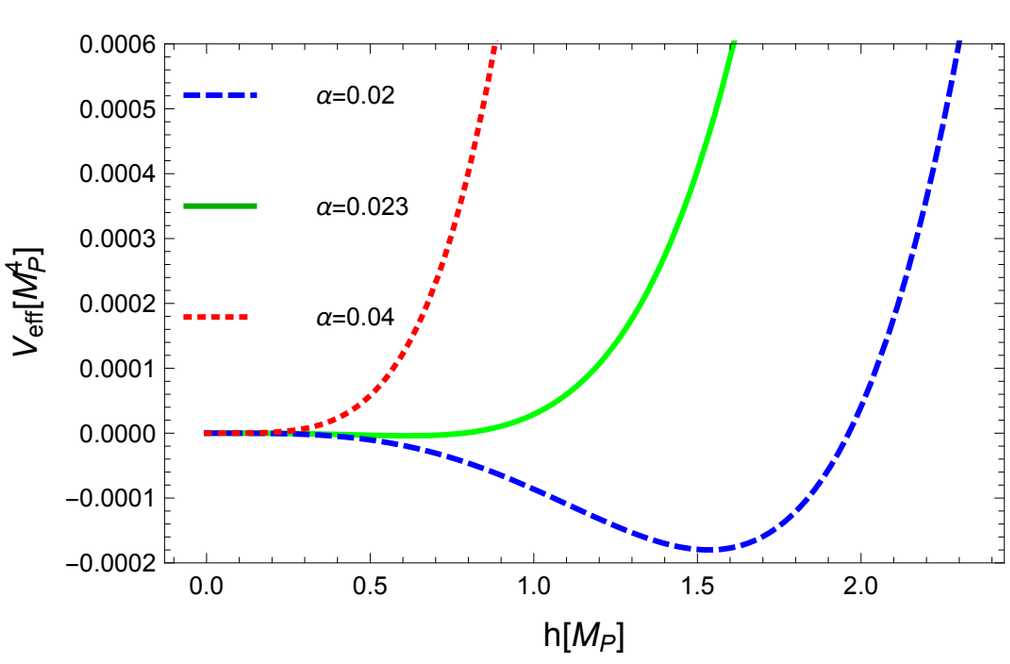
- This simple model has not been studied properly !!

HP assisted HI w/ SFDM

$$\mathcal{L} \supset \frac{1}{2}\xi_s S^2 R$$

ξ_s term is generated by RG, even if $\xi_s = 0$ at $\mu = m_t$ scale.

We assume $S = 0$ during inflation : Inflation along the Higgs direction.



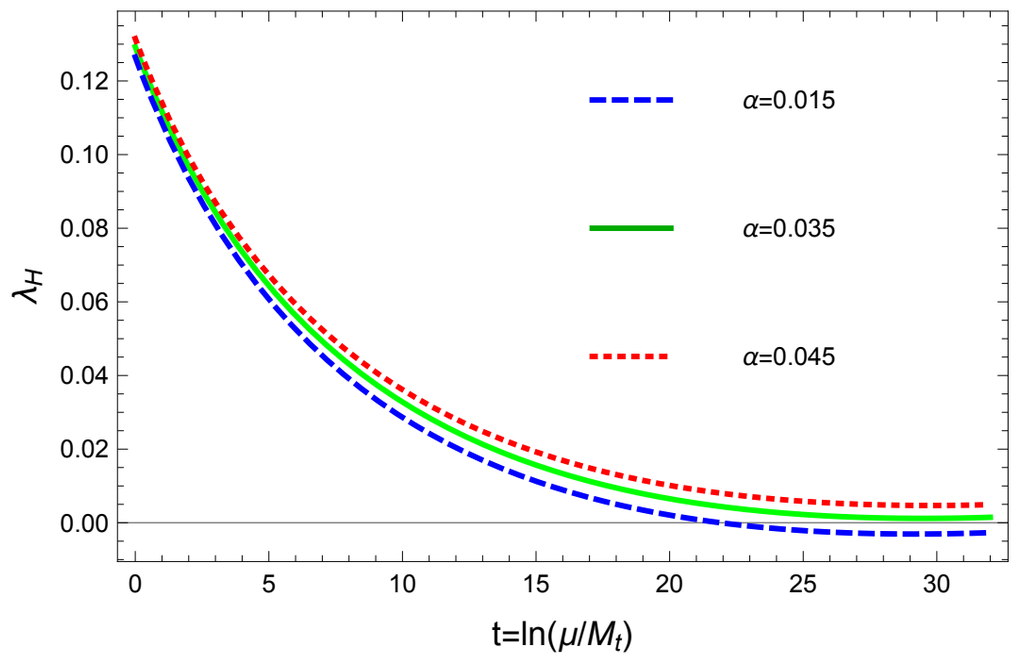


Figure 3. Jordan-frame Higgs potential $V_{\rm eff}$ (left panel) and the running of λ_H (right panel) in SFDM for $\xi_h = 440$, $\xi_s = 0$, $m_s = 600\,\text{GeV}$, $\lambda_{SH} = 0.1$, $\lambda_S = 0.2$, and $\lambda_\psi = 0.3$ chosen at M_t scale.

HP assisted HI w/ SFDM

α	m_s	λ_{SH}	λ_S	λ_ψ	ξ_h	N_e	$10^9 P_S$	n_s	r	α_s
0.036	500	0.1	0.2	0.3	433	57.3	2.2	0.9758	0.0926	-0.0003
0.03885	500	0.1	0.1	0.1	396	57.3	2.2	0.9775	0.0878	-0.0003

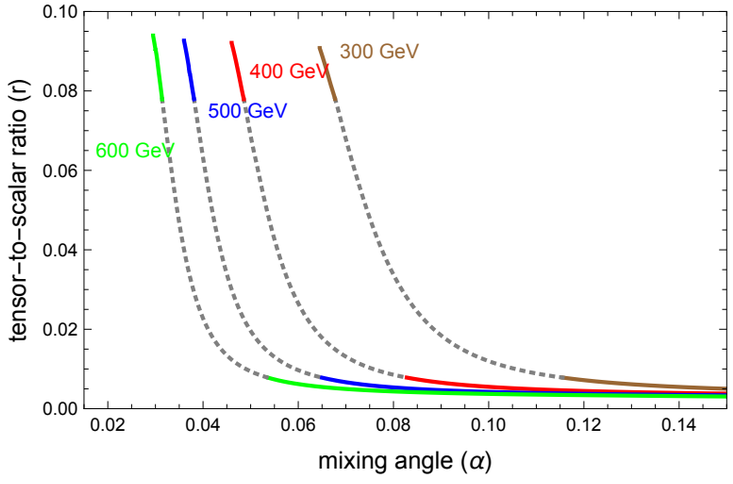


Figure 4. Tensor-to-scalar ratio as a function of the mixing angle α for $m_s = 300\,\text{GeV}$, $400\,\text{GeV}$, $500\,\text{GeV}$ and $600\,\text{GeV}$ at the pivot scale $k_* = 0.05\,\text{Mpc}^{-1}$. Here $\xi_s = 0$, $\lambda_{SH} = 0.1$, $\lambda_S = 0.2$, and $\lambda_\psi = 0.3$ at M_t scale are used. The nonminimal coupling of the SM Higgs to gravity, ξ_h, is chosen in such a way that the Planck normalization (3.8) is satisfied. The grey-dotted lines indicate the parameter region where the spectral index n_s becomes larger than 2σ Planck bound, $n_s \gtrsim 0.98$. Similar behaviors are found for different sets of model parameters.

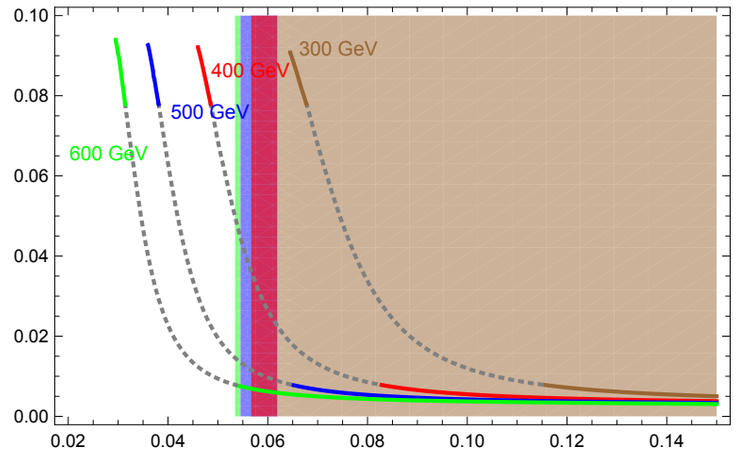


Figure 6. Tensor-to-scalar ratio as a function of the mixing angle α for $m_s = 300$ GeV, 400 GeV, 500 GeV and 600 GeV, with the constraints discussed in the main text. The stringent upper bounds for a given m_s comes from the DM physics. The values of the other parameters are the same as in figure 4. Color-shaded regions (following the scheme of colored lines) are the excluded regions from the latest LUX experiment, corresponding to different dark Higgs masses.

Large $r \sim O(0.1)$ is possible in HP assisted HI, without tight connection to m_t, m_h

Interacting Dark Matter

Why Interacting DM ?

- Theoretically interesting
  - Atomic DM, Mirror DM, Composite DM
  - Eventually, all DM is *interacting* in some way, the question is how strongly?
  - Self-Interacting DM $\frac{\sigma}{M_X} \sim \mathrm{cm}^2/\mathrm{g} \sim \mathrm{barn}/\mathrm{GeV}$
- Possible new testable signatures
  - *CMB, LSS, BBN*
  - Other astrophysical effects,…
- Solution of CDM controversies
  - *Cusp-vs-Core, Too-big-to-fail, missing satellite,…*
  - H_0, σ_8? 2-3σ, systematic uncertainty

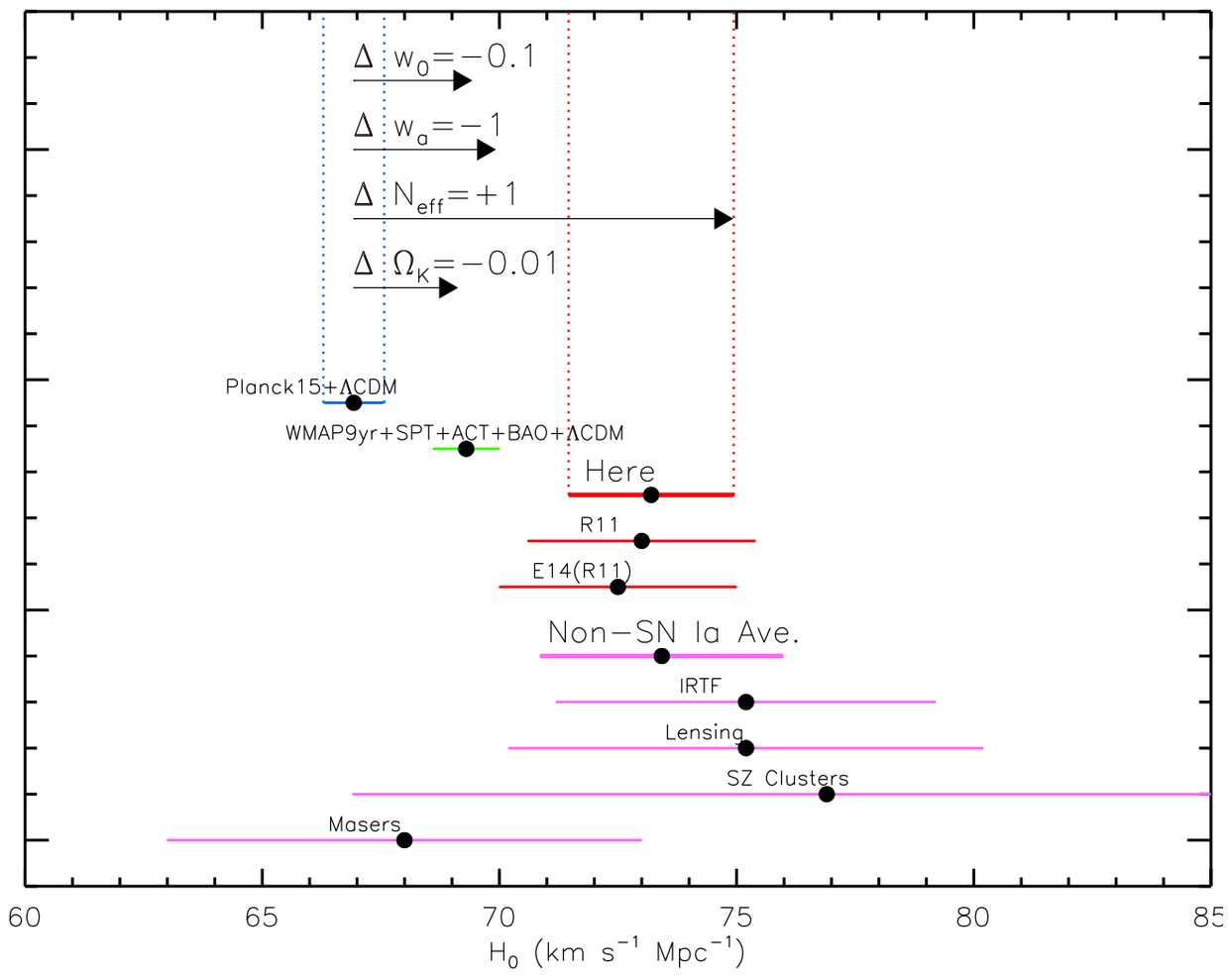
Tension in Hubble Constant?

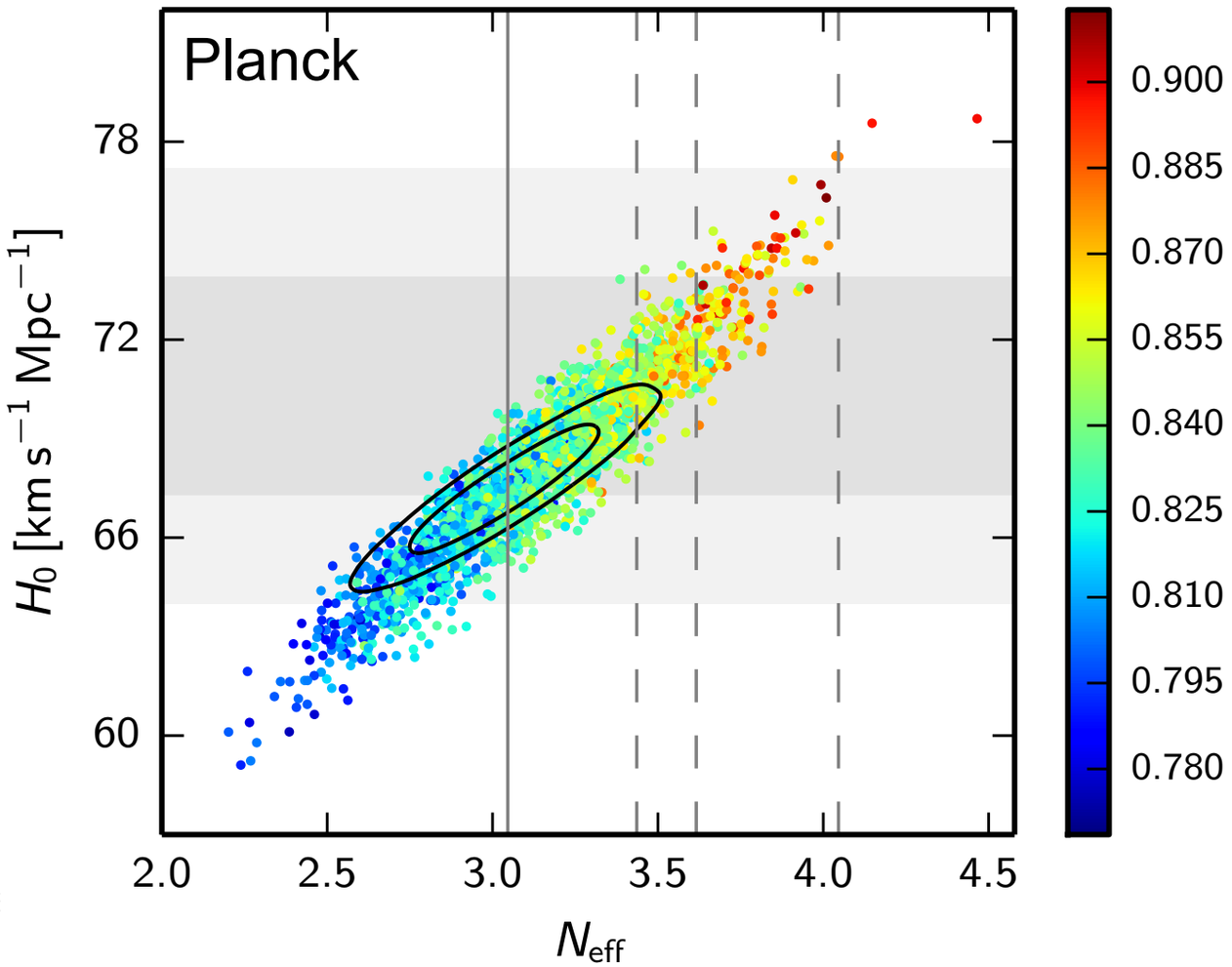
- Hubble Constant H_0 defined as the present value of

$$H \equiv \frac{1}{a}\frac{da}{dt} = \frac{\sqrt{\rho_r + \rho_m + \rho_\Lambda}}{M_p}$$

- Planck(2015) gives 67.8 ± 0.9 km s^{-1}Mpc^{-1}
- HST(2016) gives 73.24 ± 1.74 km s^{-1}Mpc^{-1}

RIESS ET AL.





Tension in σ_8 ?

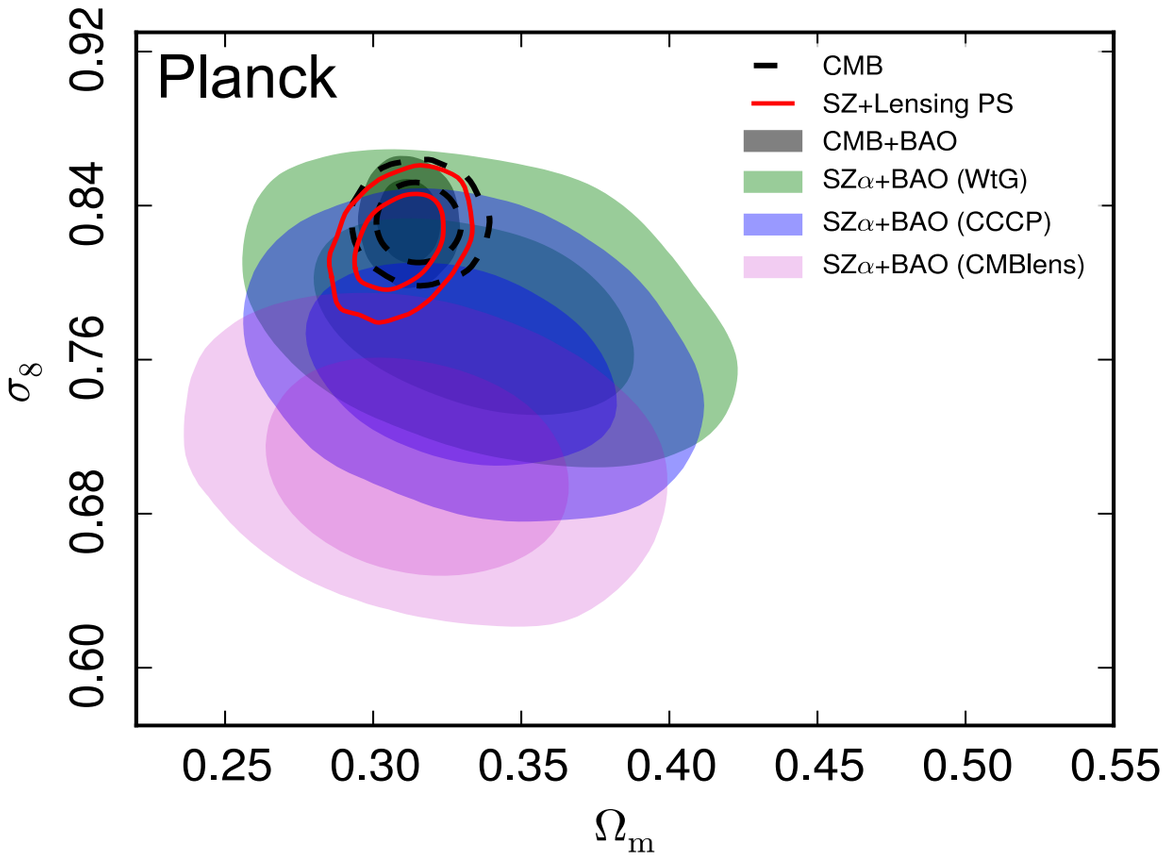
- Variance of perturbation field → collapsed objects

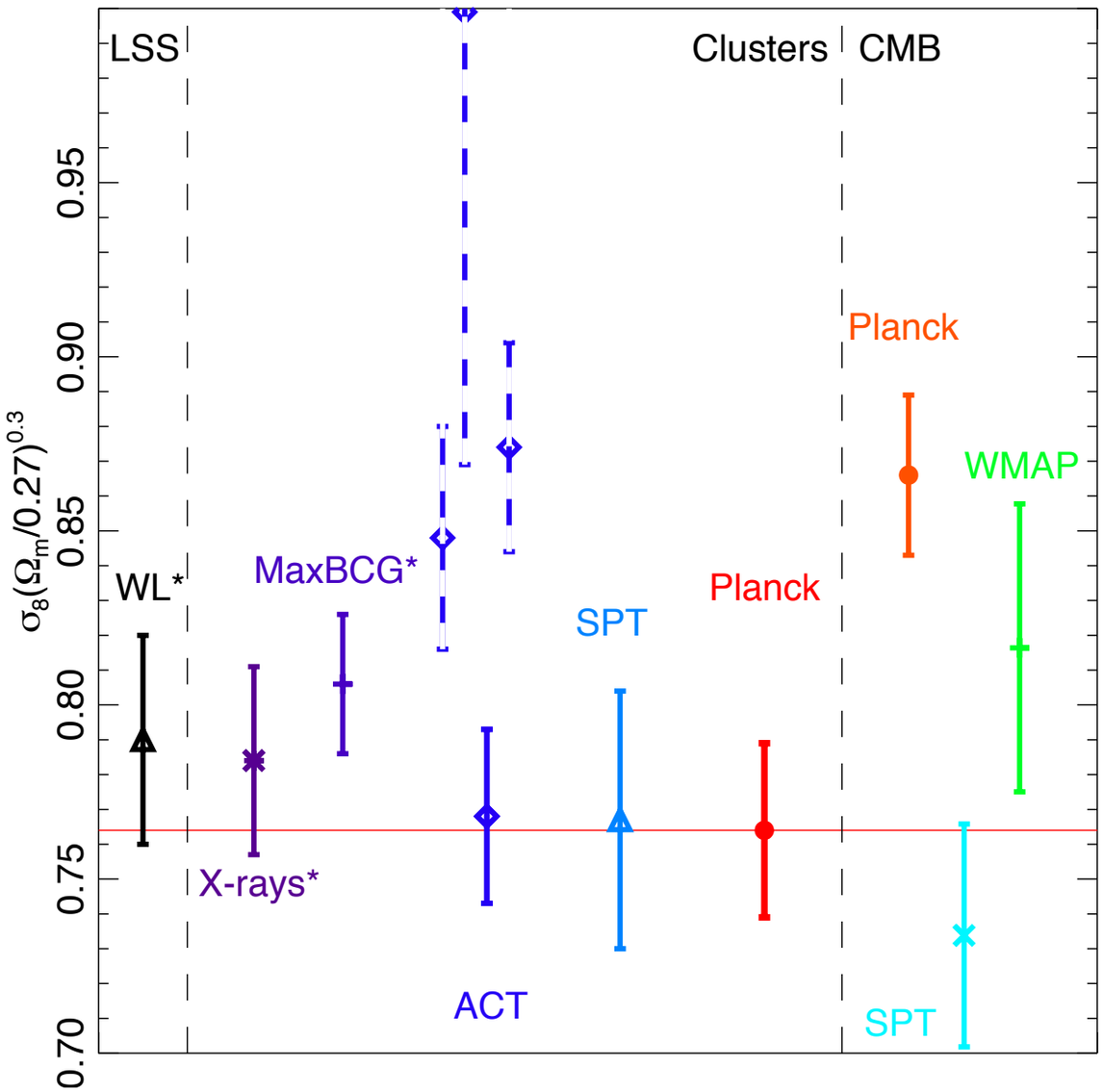
$$\sigma^2(R) = \frac{1}{2\pi^2}\int W_R^2(k) P(k) k^2 dk,$$

- where the filter function $W_R(k) = \frac{3}{(kR)^3}\left[\sin(kR) - kR\cos(kR)\right],$

  $P(k)$ is matter power spectrum.

- $\sigma_8 \equiv \sigma(8h^{-1}\mathrm{Mpc})$





Tension in σ_8 ?

Planck2015, Sunyaev–Zeldovich cluster counts

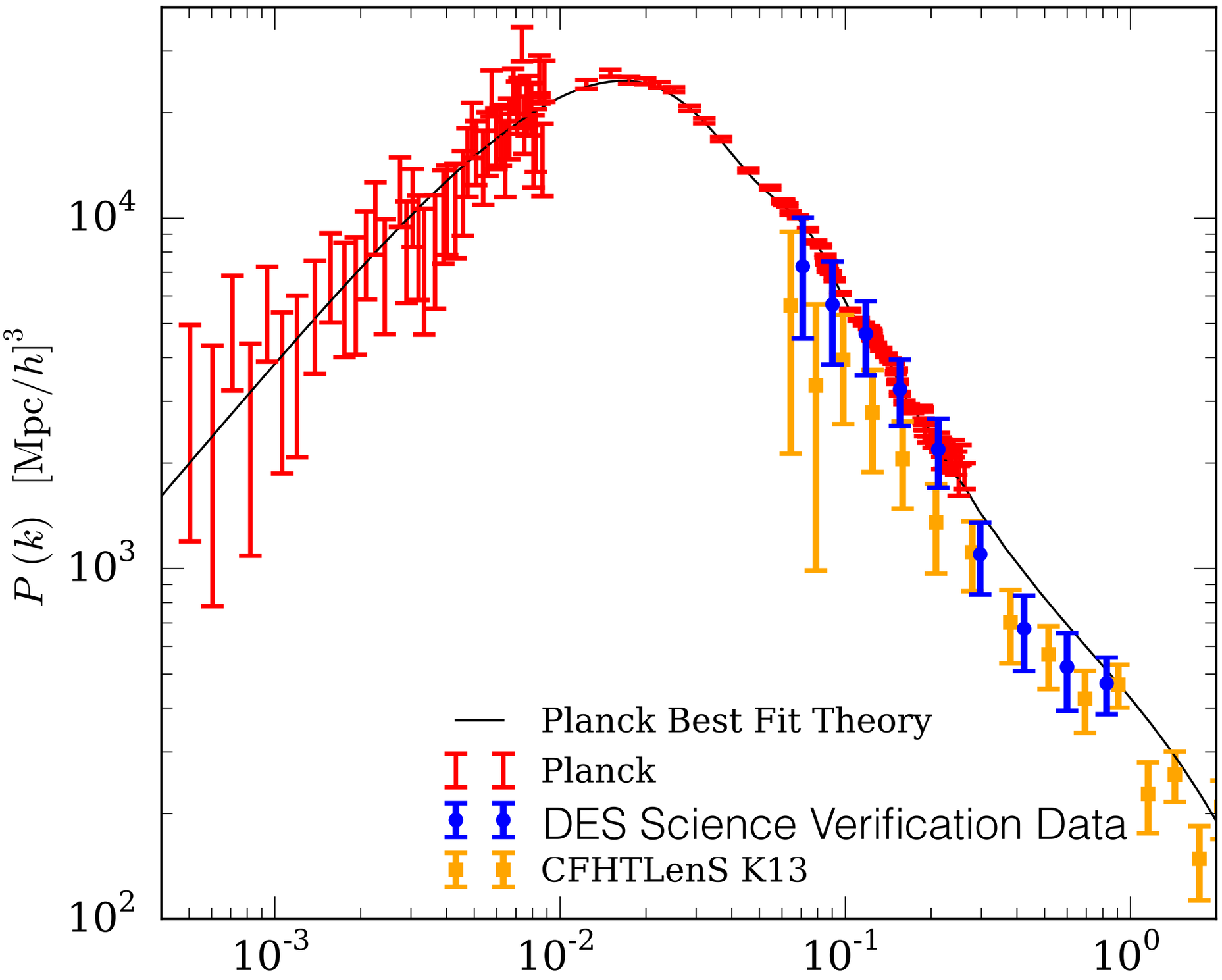
Data	$\sigma_8 \left(\frac{\Omega_m}{0.31}\right)^{0.3}$	Ω_m	σ_8
WtG + BAO + BBN	0.806 ± 0.032	0.34 ± 0.03	0.78 ± 0.03
CCCP + BAO + BBN **[Baseline]**	0.774 ± 0.034	0.33 ± 0.03	0.76 ± 0.03
CMBlens + BAO + BBN	0.723 ± 0.038	0.32 ± 0.03	0.71 ± 0.03
CCCP + H_0 + BBN	0.772 ± 0.034	0.31 ± 0.04	0.78 ± 0.04

Planck2015, Primary CMB

Parameter	[1] *Planck* TT+lowP	[2] *Planck* TE+lowP	[3] *Planck* EE+lowP	[4] *Planck* TT,TE,EE+lowP
$\Omega_b h^2$	0.02222 ± 0.00023	0.02228 ± 0.00025	0.0240 ± 0.0013	0.02225 ± 0.00016
$\Omega_c h^2$	0.1197 ± 0.0022	0.1187 ± 0.0021	$0.1150^{+0.0048}_{-0.0055}$	0.1198 ± 0.0015
$100\theta_{MC}$	1.04085 ± 0.00047	1.04094 ± 0.00051	1.03988 ± 0.00094	1.04077 ± 0.00032
τ	0.078 ± 0.019	0.053 ± 0.019	$0.059^{+0.022}_{-0.019}$	0.079 ± 0.017
$\ln(10^{10} A_s)$	3.089 ± 0.036	3.031 ± 0.041	$3.066^{+0.046}_{-0.041}$	3.094 ± 0.034
n_s	0.9655 ± 0.0062	0.965 ± 0.012	0.973 ± 0.016	0.9645 ± 0.0049
H_0	67.31 ± 0.96	67.73 ± 0.92	70.2 ± 3.0	67.27 ± 0.66
Ω_m	0.315 ± 0.013	0.300 ± 0.012	$0.286^{+0.027}_{-0.038}$	0.3156 ± 0.0091
σ_8	0.829 ± 0.014	0.802 ± 0.018	0.796 ± 0.024	0.831 ± 0.013
$10^9 A_s e^{-2\tau}$	1.880 ± 0.014	1.865 ± 0.019	1.907 ± 0.027	1.882 ± 0.012

Matter Power Spectrum

DES astroph/150705552

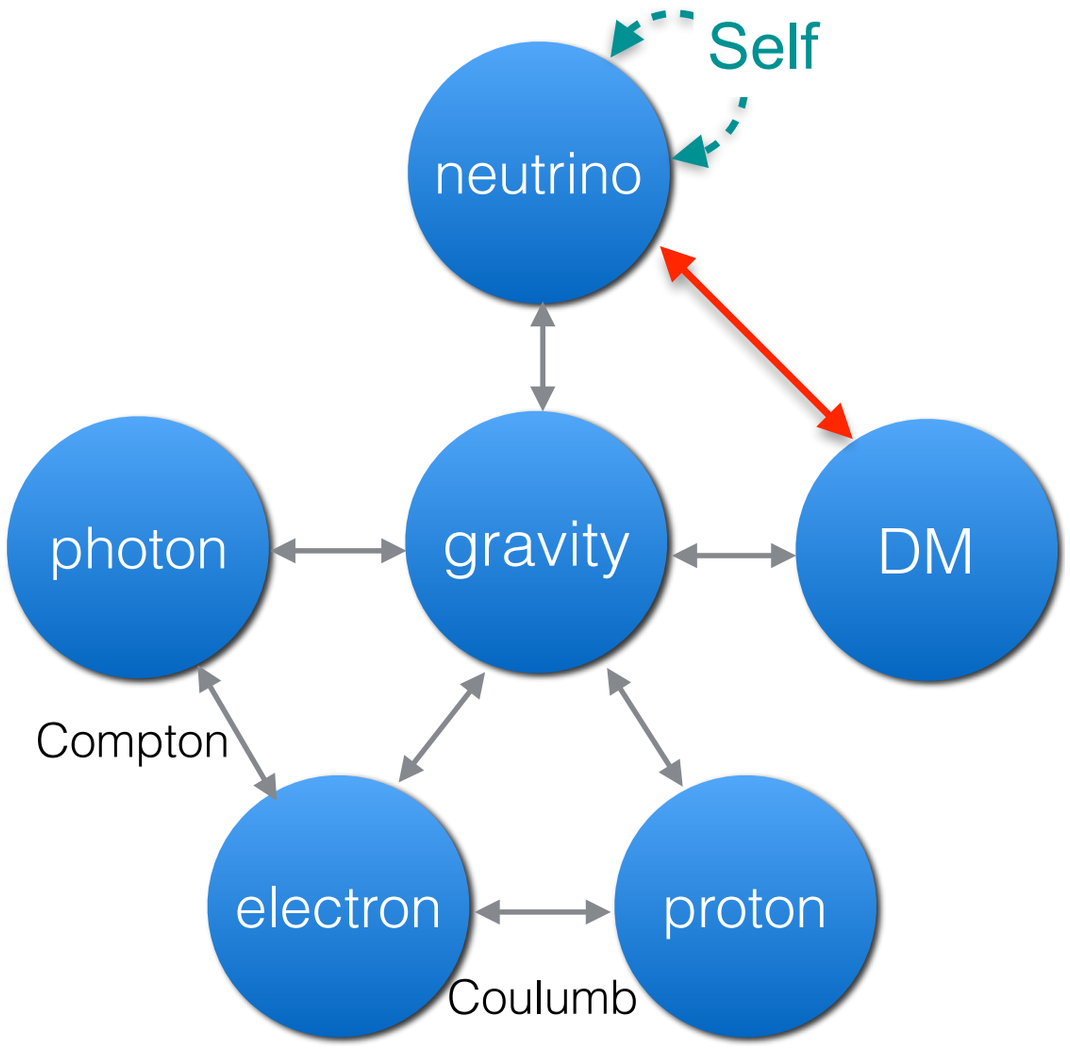


Interacting DM-DR

- Since all components are connected by Einstein's equation

$$R_{\mu\nu} - \frac{1}{2}Rg_{\mu\nu} + \Lambda g_{\mu\nu} = \frac{8\pi G}{c^4}T_{\mu\nu}$$

- first-order perturbation of Boltzmann equation
  - anisotropy in CMB
  - matter power spectrum for LSS
- (Self-)Interaction sometimes also matters



Interacting Radiation

- free-streaming

$$\dot{\delta}_\nu = -\frac{4}{3}\theta_\nu + 4\dot{\phi}\ ,$$

$$\dot{\theta}_\nu = k^2\left(\frac{1}{4}\delta_\nu - \sigma_\nu\right) + k^2\psi\ ,$$

$$\dot{F}_{\nu l} = \frac{k}{2l+1}\left[lF_{\nu(l-1)} - (l+1)F_{\nu(l+1)}\right]\ ,$$

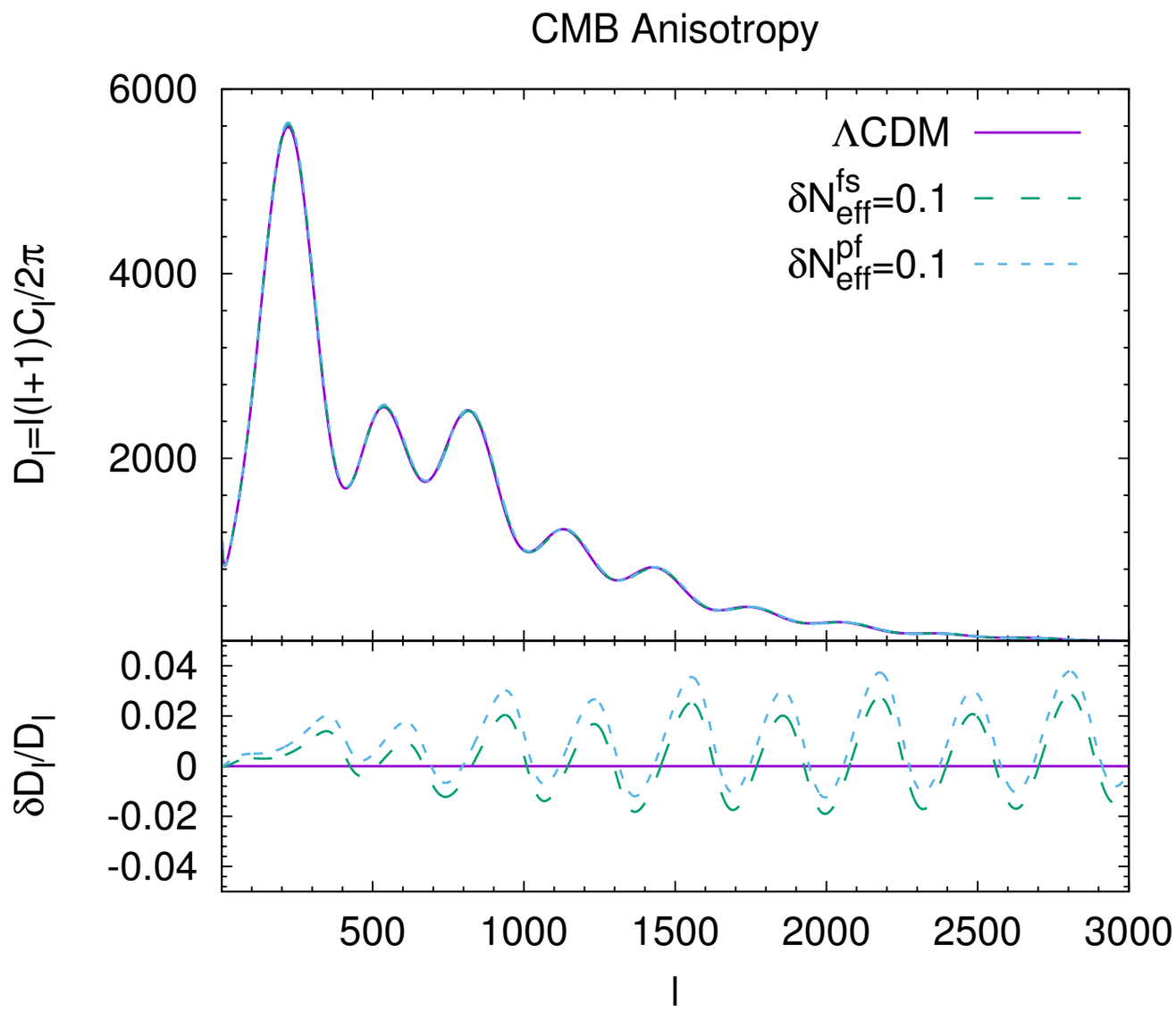
- perfect fluid $\Gamma \gg \mathcal{H}$

$$\dot{\delta}_\nu = -\frac{4}{3}\theta_\nu + 4\dot{\phi}\ ,$$

$$\dot{\theta}_\nu = k^2\left(\frac{1}{4}\delta_\nu - \sigma_\nu\right) + k^2\psi\ ,$$

σ_ν=0

Y.Tang, arXiv:1603.00165(PLB)



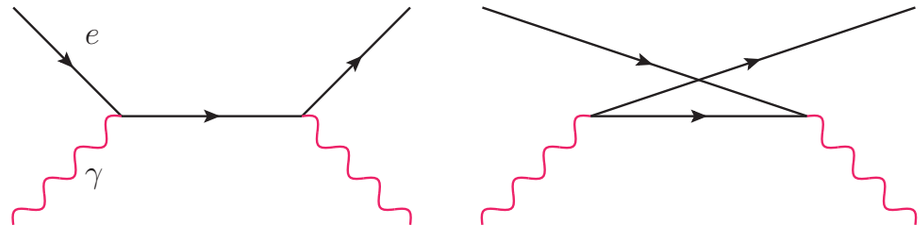
Neutrinos as perfect fluid excluded,
Audren **et al 1412.5948**

Relation to Particle Physics

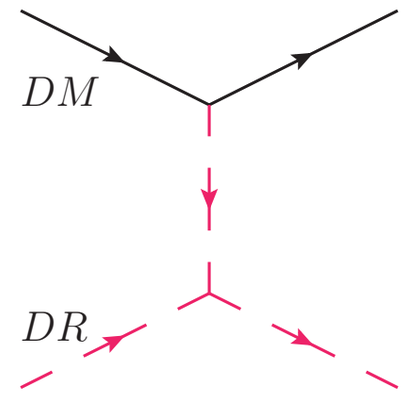
- The precise form of the scattering term, $\langle\sigma c\rangle$, is fully determined by the underlying microscopic or particle physics model, for example

IR behaviour

  - electron-photon, $\langle\sigma c\rangle \sim 1/m^2$
    Thomson scattering -> CMB, BAO



  - DM-radiation with massive mediator, $\langle\sigma c\rangle \sim T^2/m^4$
    Boehm *et al*(astro-ph/0410591,1309.7588)



  - non-Abelian radiation, $\langle\sigma c\rangle \sim 1/T^2$
    Schmaltz et al(2015), 1507.04351,1505.03542

  - (pseudo-)scalar radiation, $\langle\sigma c\rangle \sim 1/T^2$, μ^2/T^4, T^2/μ^4
    Y.Tang,1603.00165(PLB)

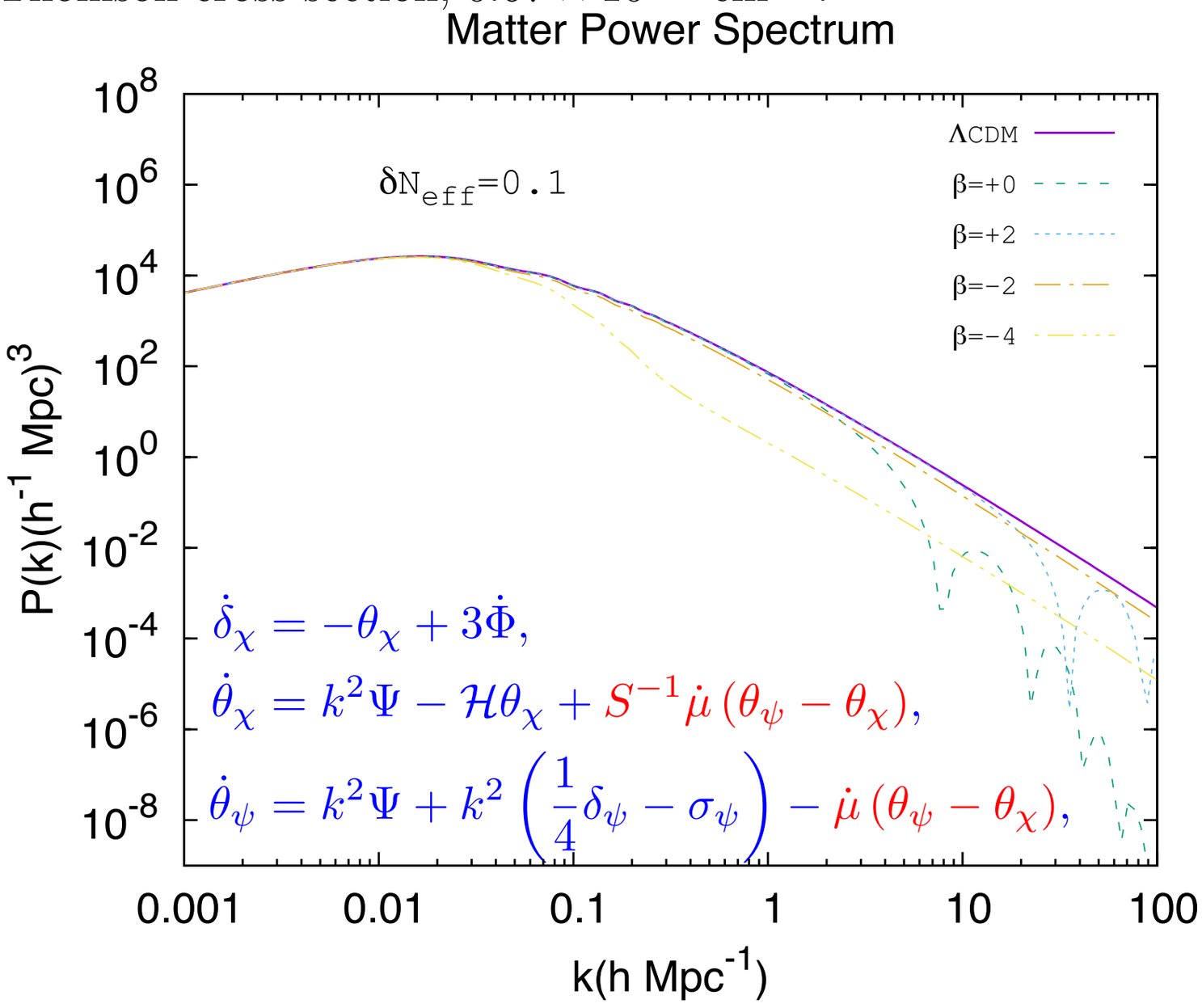
Effects on LSS

Parametrize the cross section ratio

Y.Tang,1603.00165(PLB)

$$u_0 \equiv \left[\frac{\sigma_{\chi\psi}}{\sigma_{\rm Th}}\right]\left[\frac{100{\rm GeV}}{m_\chi}\right], u_\beta(T) = u_0\left(\frac{T}{T_0}\right)^\beta,$$

where $\sigma_{\rm Th}$ is the Thomson cross section, $0.67\times10^{-24}{\rm cm}^{-2}$.



Paricle Physics Models for Interacting DM-DR

- Light sterile fermion DR + Dark photon : 1608.01083 (PLB)
- Nonabelian DM + DR : 1609.02307 (PLB)
- Hidden charged DM and chiral DR (DQCD) : 1706.05605 (PLB)

With Yong Tang, Natsumi Negata

A Light Dark Photon

P.Ko, YT, 1608.01083(PLB)

- Lagrangian

$$\mathcal{L} = -\frac{1}{4}V_{\mu\nu}V^{\mu\nu} + D_\mu\Phi^\dagger D^\mu\Phi + \bar{\chi}\left(i\not{D} - m_\chi\right)\chi + \bar{\psi}i\not{D}\psi$$
$$-\left(y_\chi\Phi^\dagger\bar{\chi}^c\chi + y_\psi\Phi\bar{\psi}N + h.c.\right) - V(\Phi, H),$$

- DM χ(+1), dark radiation ψ(+2), scalar(+2)
- *U(1)* symmetry (*unbroken*), massless dark photon V_μ **(Phi VEV = 0)**
- Φ is responsible for the DM relic density

$$\Omega h^2 \simeq 0.1 \times \left(\frac{y_\chi}{0.7}\right)^{-4}\left(\frac{m_\chi}{\text{TeV}}\right)^2.$$

- Φ can decay into ψ and ***N***.

Dark Radiation δN_{eff}

- Effective Number of Neutrinos, N_{eff}

$$\rho_R = \left[1 + N_{\rm eff} \times \frac{7}{8}\left(\frac{4}{11}\right)^{4/3}\right]\rho_\gamma,$$

$$\rho_\gamma \propto T_\gamma^4$$

- In SM cosmology, N_{eff}=3.046. Neutrinos decouple around MeV, and then freely stream.

- Cosmological bounds

Joint CMB+BBN, 95% CL preferred ranges *Planck 2015, arXiv:1502.01589*

$$N_{\rm eff} = \begin{cases} 3.11^{+0.59}_{-0.57} & \text{He+}\textit{Planck}\text{ TT+lowP}, \\ 3.14^{+0.44}_{-0.43} & \text{He+}\textit{Planck}\text{ TT+lowP+BAO}, \\ 2.99^{+0.39}_{-0.39} & \text{He+}\textit{Planck}\text{ TT,TE,EE+lowP}, \end{cases}$$

Constraint on New Physics

$$\left.\begin{array}{r} N_{\rm eff} < 3.7 \\ m^{\rm eff}_{\nu,\,\rm sterile} < 0.52\ {\rm eV} \end{array}\right\} \ 95\%,\ \textit{Planck}\text{ TT+lowP+lensing+BAO}.$$

Dark Radiation δN_{eff}

- Massless dark photon and fermion will contribute

$$\delta N_{\rm eff} = \left(\frac{8}{7}+2\right)\left[\frac{g_{*s}\left(T_\nu\right)}{g_{*s}\left(T^{\rm dec}\right)}\frac{g^D_{*s}\left(T^{\rm dec}\right)}{g^D_{*s}\left(T_D\right)}\right]^{\frac{4}{3}},$$

where T_ν is neutrino's temperature,

g_{*s} counts the effective number of dof for entropy density in SM,

g^D_{*s} denotes the effective number of dof being in kinetic equilibrium with V_μ.

For instance, when $T^{\rm dec} \gg m_t \simeq 173{\rm GeV}$ for $|\lambda_{\Phi H}| \sim 10^{-6}$, we can estimate $\delta N_{\rm eff}$ at the BBN epoch as

$$\delta N_{\rm eff} = \frac{22}{7}\left[\frac{43/4}{427/4}\frac{11}{9/2}\right]^{\frac{4}{3}} \simeq 0.53, \qquad (1)$$

δN_{eff}=0.4~1 for relaxing tension in Hubble constant

Diffusion Damping

- Dark Matter scatters with radiation, which induces new contributions in the cosmological perturbation equations,

$$\dot{\delta}_\chi = -\theta_\chi + 3\dot{\Phi},$$
$$\dot{\theta}_\chi = k^2\Psi - \mathcal{H}\theta_\chi + S^{-1}\dot{\mu}\,(\theta_\psi - \theta_\chi),$$
$$\dot{\theta}_\psi = k^2\Psi + k^2\left(\frac{1}{4}\delta_\psi - \sigma_\psi\right) - \dot{\mu}\,(\theta_\psi - \theta_\chi),$$

where dot means derivative over conformal time $d\tau \equiv dt/a$ (a is the scale factor), θ_ψ and θ_χ are velocity divergences of radiation ψ and DM χ's, k is the comoving wave number, Ψ is the gravitational potential, δ_ψ and σ_ψ are the density perturbation and the anisotropic stress potential of ψ, and $\mathcal{H} \equiv \dot{a}/a$ is the conformal Hubble parameter. Finally, the scattering rate and the density ratio are defined by $\dot{\mu} = an_\chi\langle\sigma_{\chi\psi}c\rangle$ and $S = 3\rho_\chi/4\rho_\psi$, respectively.

Scattering Cross Section

The averaged cross section $\langle \sigma_{\chi\psi} \rangle$ can be estimated from the squared matrix element for $\chi\psi \to \chi\psi$:

$$\overline{|\mathcal{M}|^2} \equiv \frac{1}{4} \sum_{\text{pol}} |\mathcal{M}|^2 = \frac{2g_X^4}{t^2} \left[t^2 + 2st + 8m_\chi^2 E_\psi^2 \right], \quad (9)$$

where the Mandelstam variables are $t = 2E_\psi^2 (\cos\theta - 1)$ and $s = m_\chi^2 + 2m_\chi E_\psi$, where θ is the scattering angle, and E_ψ is the energy of incoming ψ in the rest frame of χ. Integrated with a temperature-dependent Fermi-Dirac distribution for E_ψ, we find that $\langle \sigma_{\chi\psi} \rangle$ goes roughly as $g_X^4/(4\pi T_D^2)$.

- *In general, the cross section could have different temperature dependence, depending on the underlying particle models.*

Numerical Results

We take the central values of six parameters of ΛCDM from `Planck`,

$\Omega_b h^2 = 0.02227$, Baryon density today

$\Omega_c h^2 = 0.1184$, CDM density today

$100\theta_{\rm MC} = 1.04106$, $100 \times$ approximation to r_*/D_A

$\tau = 0.067$, Thomson scattering optical depth

$\ln\left(10^{10} A_s\right) = 3.064$, Log power of primordial curvature perturbations

$n_s = 0.9681$, Scalar Spectrum power-law index

which gives $\sigma_8 = 0.817$ in vanilla ΛCDM cosmology.

With the same input as above, now take

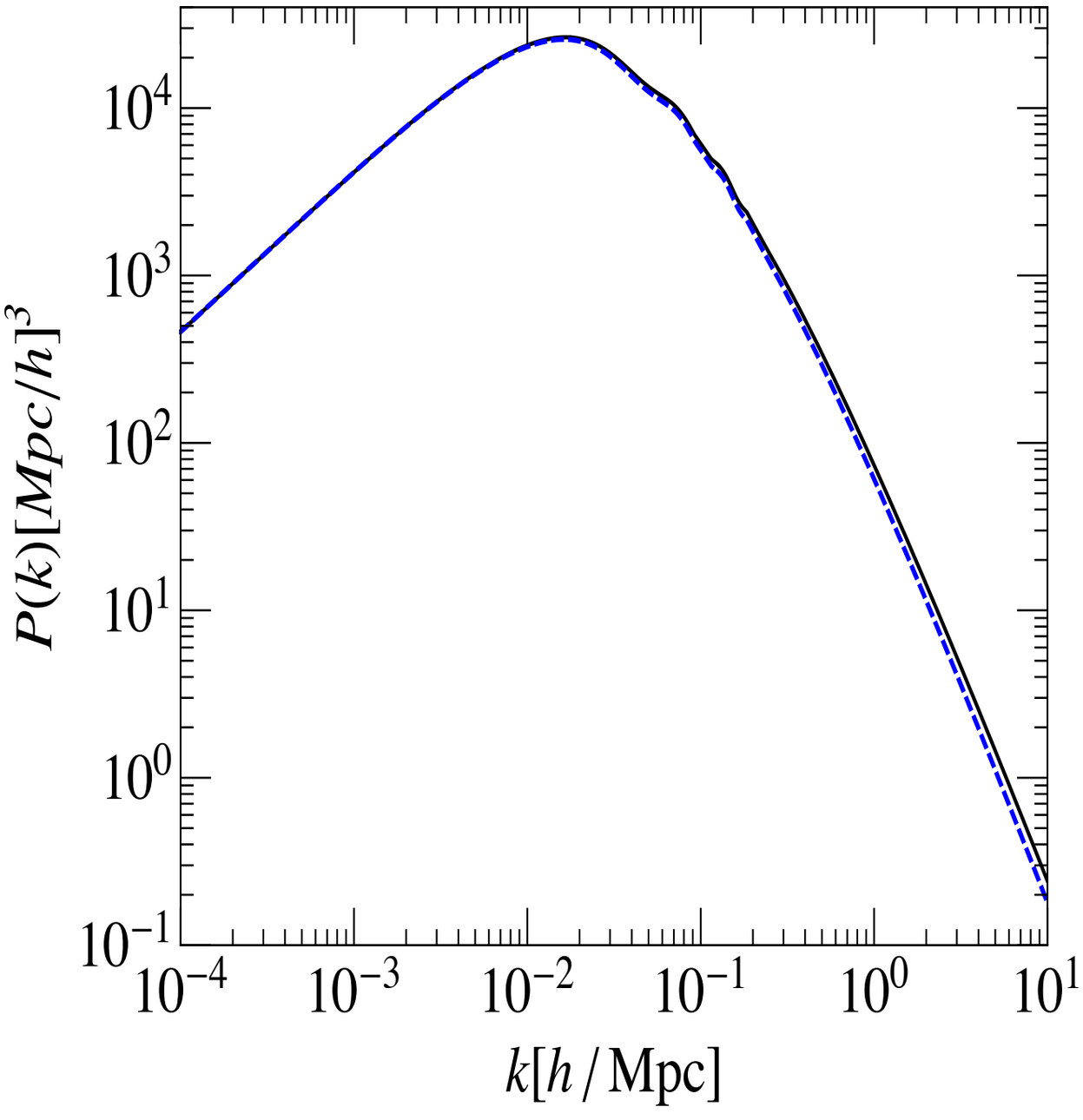
$$\delta N_{\rm eff} \simeq 0.53, m_\chi \simeq 100{\rm GeV} \text{ and } g_X^2 \simeq 10^{-8}$$

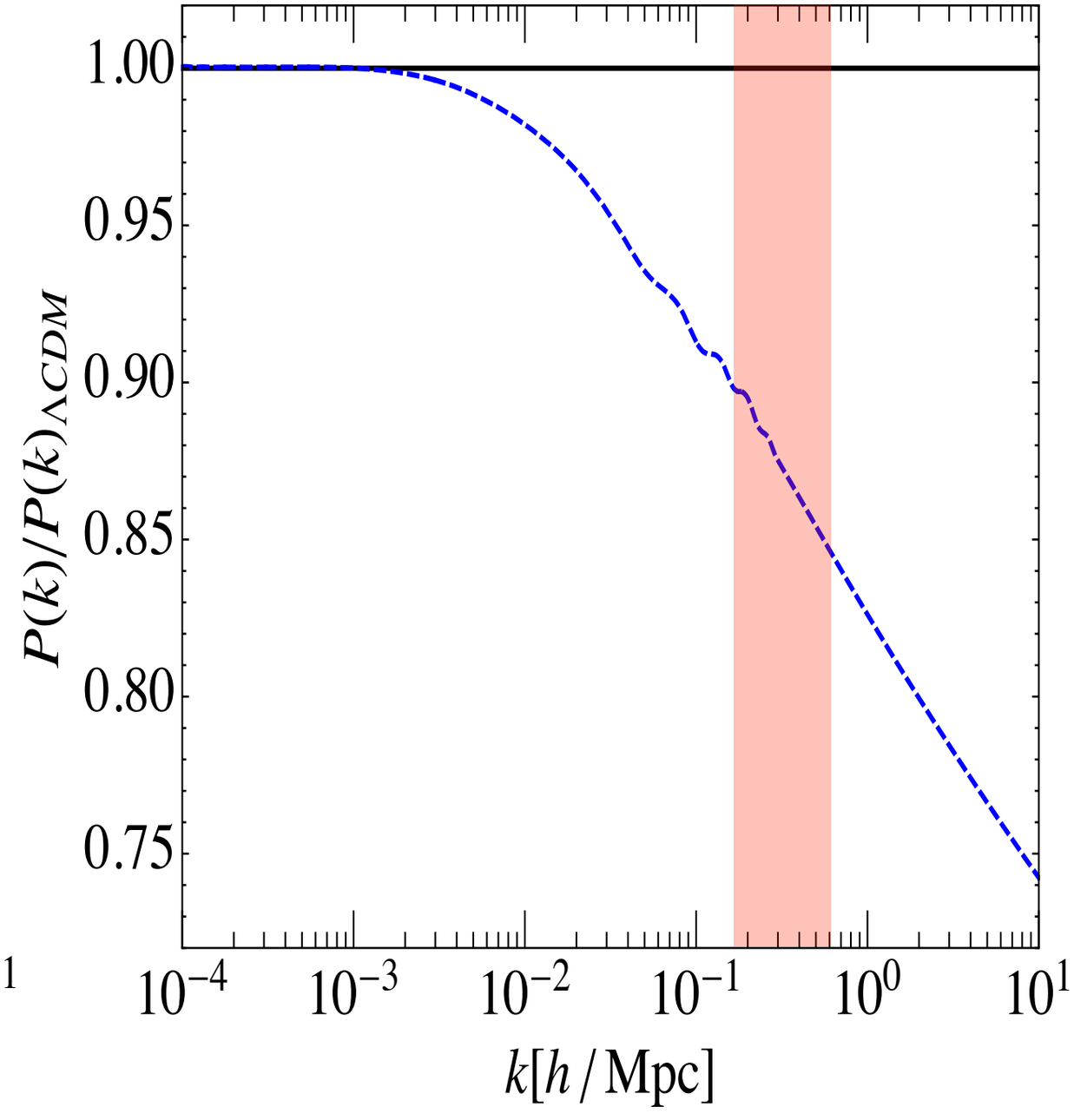
in the interacting DM case, we have $\sigma_8 \simeq 0.744$.

Modified Boltzmann code ***CLASS(Blas&Lesgourgues&Tram)***

Matter Power Spectrum

DM-DR scattering causes diffuse damping at relevant scales, resolving σ_8 problem





Results

We take the central values of six parameters of ΛCDM from `Planck` [1],

$$\Omega_b h^2 = 0.02227, \Omega_c h^2 = 0.1184, 100\theta_{\rm MC} = 1.04106,$$
$$\tau = 0.067, \ln\left(10^{10} A_s\right) = 3.064, n_s = 0.9681, \qquad (11)$$

which gives $\sigma_8 = 0.817$ in vanilla ΛCDM cosmology. With the same input as above, now we take $\delta N_{\rm eff} \simeq 0.53$, $m_\chi \simeq 100{\rm GeV}$ and $g_X^2 \simeq 10^{-8}$ in the interacting DM case, we have $\sigma_8 \simeq 0.744$ which is much closer to the value $\sigma_8 \simeq 0.730$ given by weak lensing survey CFHTLenS [3].

Residual Non-Abelian DM&DR

P.Ko&YT, 1609.02307

- Consider *SU(N)* Yang-Mills gauge fields and a Dark Higgs field Φ

$$\mathcal{L} = -\frac{1}{4} F^a_{\mu\nu} F^{a\mu\nu} + \left(D_\mu \Phi\right)^\dagger \left(D^\mu \Phi\right) - \lambda_\phi \left(|\Phi|^2 - v_\phi^2/2\right)^2 ,$$

- Take *SU(3)* as an example,

$$A^a_\mu t^a = \frac{1}{2} \begin{pmatrix} A^3_\mu + \frac{1}{\sqrt{3}} A^8_\mu & A^1_\mu - i A^2_\mu & A^4_\mu - i A^5_\mu \\ A^1_\mu + i A^2_\mu & -A^3_\mu + \frac{1}{\sqrt{3}} A^8_\mu & A^6_\mu - i A^7_\mu \\ A^4_\mu + i A^5_\mu & A^6_\mu + i A^7_\mu & -\frac{2}{\sqrt{3}} A^8_\mu \end{pmatrix} .$$

- *SU(3)* → *SU(2)*

$$\langle \Phi \rangle = \begin{pmatrix} 0 & 0 & \frac{v_\phi}{\sqrt{2}} \end{pmatrix}^T , \Phi = \begin{pmatrix} 0 & 0 & \frac{v_\phi + \phi(x)}{\sqrt{2}} \end{pmatrix}^T ,$$

The massive gauge bosons $A^{4,\cdots,8}$ as dark matter obtain masses,

$$m_{A^{4,5,6,7}} = \frac{1}{2} g v_\phi , \; m_{A^8} = \frac{1}{\sqrt{3}} g v_\phi ,$$

and massless gauge bosons $A^{1,2,3}_\mu$. The physical scalar ϕ can couple to $A^{4,\cdots,8}_\mu$ at tree level and to $A^{1,2,3}$ at loop level.

$SU(N) \to SU(N-1)$

- *2N-1* massive gauge bosons: Dark Matter
- *(N-1)²-1* massless gauge bosons: Dark Radiation
- mass spectrum

$$m_{A^{(N-1)^2,\ldots,N^2-2}} = \frac{1}{2} g v_\phi,\ m_{A^{N^2-1}} = \frac{\sqrt{N-1}}{\sqrt{2N}} g v_\phi,$$

This can be proved by looking at the structure of f^{abc}. Divide the generators t^a into two subset,

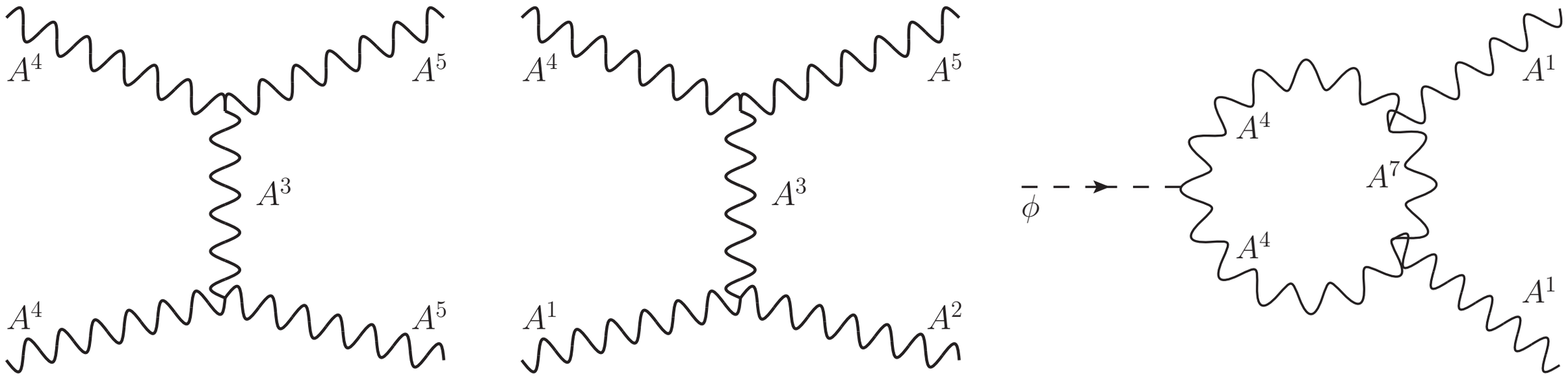
$$a \subset [1, 2, ..., (N-1)^2 - 1], a \subset [(N-1)^2, ..., N^2 - 1].$$

Since $[t^a, t^b] = i f^{abc} t^c$ for the first subset forms closed $SU(N-1)$ algebra, we have $f^{abc} = 0$ when only one of a, b and c is from the second subset. If one index is $N^2 - 1$, then other two must be among the second subset to give no vanishing f^{abc}, because t^{N^2-1} commutes with t^a from $SU(N-1)$.

Phenomenology

- Scattering and decay processes

P.Ko&**YT**, 1609.02307



- Constraints

$$\delta N_{\rm eff} = \frac{8}{7}\left[(N-1)^2 - 1\right] \times 0.055,$$

$$g^2 \lesssim \frac{T_\gamma}{T_A}\left(\frac{m_A}{M_P}\right)^{1/2} \sim 10^{-7},$$

$$\frac{m_A}{T_{\rm reh}} \sim \ln\left[\frac{\Omega_b M_P g^4}{\Omega_X m_p \eta}\right] \sim \mathcal{O}(30).$$

- ***N<6 if thermal***
- ***small coupling,***
- ***non-thermal production,***
- ***low reheating temperature***

Schmaltz et al(2015) EW charged DM

Matter Power Spectrum

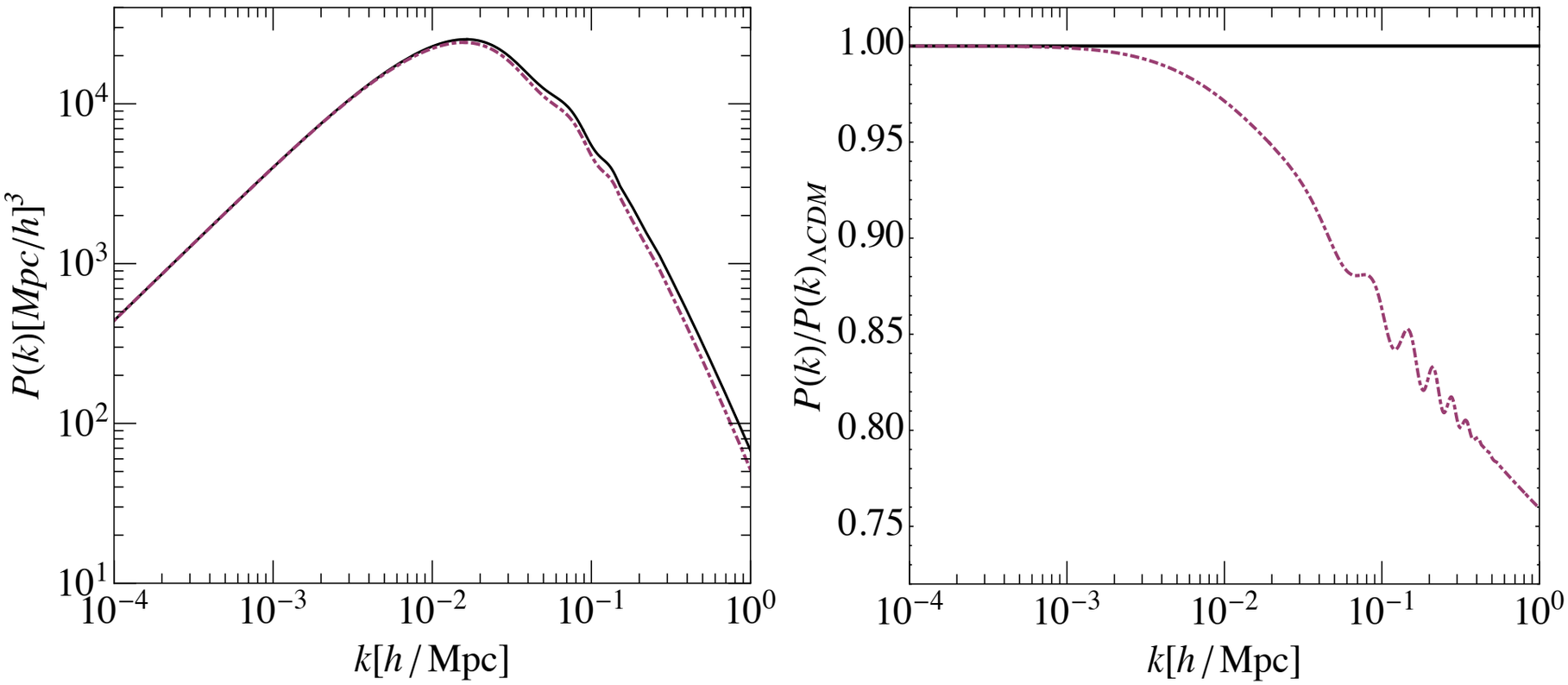


FIG. 3. Matter power spectrum $P(k)$ (left) and ratio (right) with $m_\chi \simeq 10\mathrm{TeV}$ and $g_X^2 \simeq 10^{-7}$, in comparison with ΛCDM. The black solid lines are for ΛCDM and the purple dot-dashed lines for interacting DM-DR case, with input parameters in Eq. 21. We can easily see that $P(k)$ is suppressed for modes that enter horizon at radiation-dominant era. Those little wiggles are due to the well-known baryon acoustic oscillation.

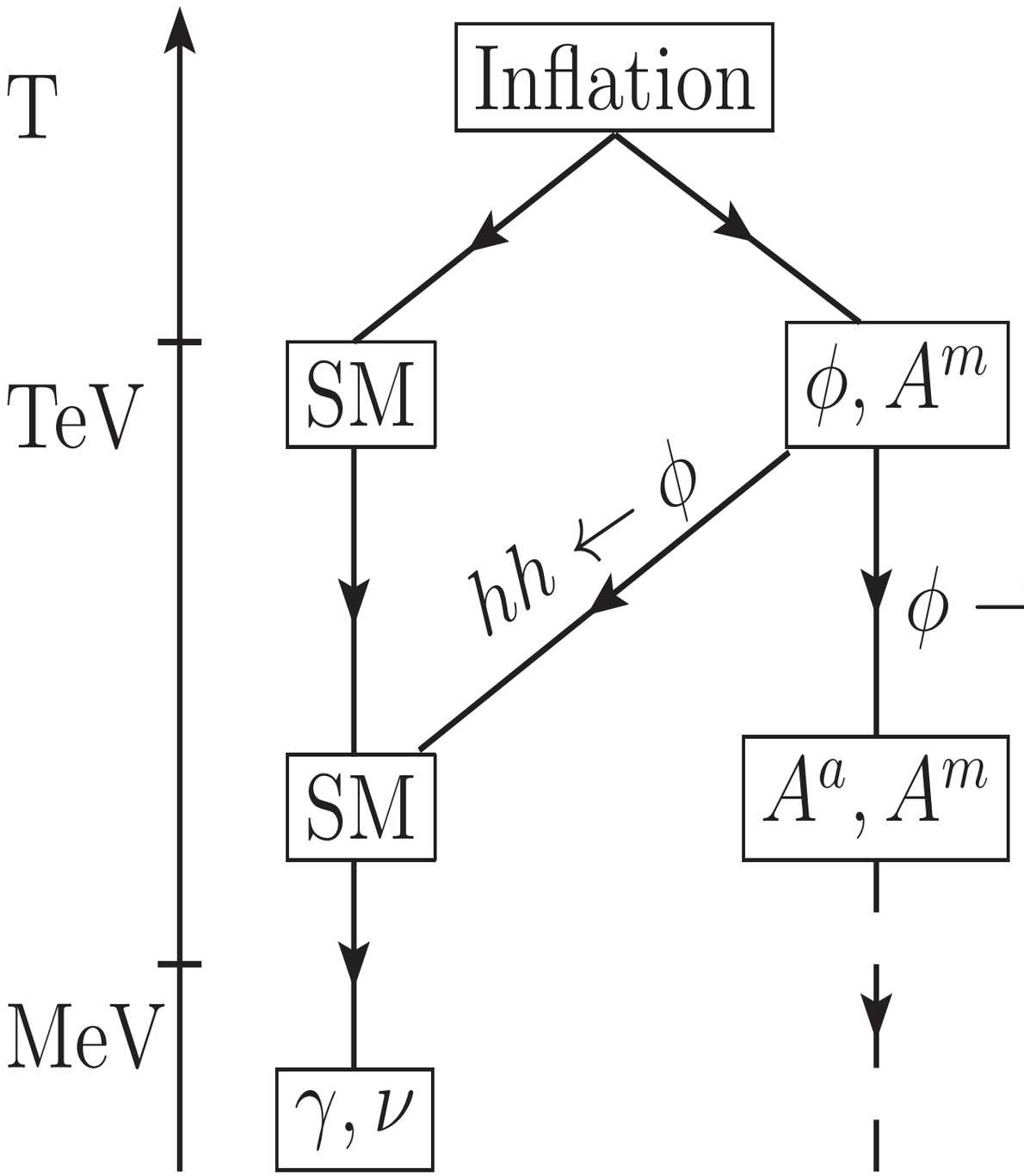
Results

$$\Omega_b h^2 = 0.02227, \Omega_c h^2 = 0.1184, 100\theta_{\rm MC} = 1.04106,$$
$$\tau = 0.067, \ln\left(10^{10} A_s\right) = 3.064, n_s = 0.9681, \quad (21)$$

and treat neutrino mass the same way as `Planck` did with $\sum m_\nu = 0.06$eV, which gives $\sigma_8 = 0.815$ in vanilla ΛCDM cosmology. Together with the same inputs as above, we take $\delta N_{\rm eff} \simeq 0.5$, $m_\chi \simeq 10$TeV and $g_X^2 \simeq 10^{-7}$ in the interacting DM-DR case, we have $\sigma_8 \simeq 0.746$ which is much closer to the value $\sigma_8 \simeq 0.730$ given by weak lensing survey CFHTLenS [12].

- Within DM models with local dark SU(3) broken into SU(2), DM, DR and their interactions have common origin!
- And we could increase Neff, H_0 whereas making σ_8 decrease, thereby relaxing the tension between H_0 and σ_8

Thermal History



- The minimal setup with Higgs portal interaction

  $\lambda_{\phi H} \Phi^\dagger \Phi H^\dagger H$

- SM and DS are decoupled early, DM is produced by freeze-in mechanism

- Late time decay, entropy production due to non-relativistic decay, DR(δN_{eff})

- DM and DS scattering suppress the matter power spectrum

Summary

- We discussed some cosmological effects with *interacting* Dark Matter and Dark Radiation within DM models with dark gauge symmetries
- This scenario is motivated theoretically and also from observational tensions, H_0 and σ_8
- We present two particle physics models:
  - A massless dark photon with *unbroken U(1)* gauge symmetry
  - *Residual non-Abelian* Dark Matter and Dark Radiation
- It is possible to resolve tensions simultaneously

To-Do List (Particle physicist's point of view)

- Charge/color neutral : no renormalizable int's w/ γ, g
- Eq of State : $\rho \simeq 0$ $(i\,.\,e\,.\,p \simeq 0)$
- $\tau_{\rm DM} \gg \tau$ (Age of the Universe) or ∞

What is the DM mass ?

- If very light, DM is long lived for the kinematical reason
- Axion and light sterile ν's are good examples

- If not, reasonable to assume some conserved quantum #, either exactly or approximately conserved
- Local or global Dark Sym