BelleII excess
&
Muon g-2
illuminating Light DM

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김종국

Based on

arXiv: 2401.10112

with Shu-Yu Ho (KIAS), Pyungwon Ko (KIAS)

2024 Korea-France STAR & 12th KIAS workshop

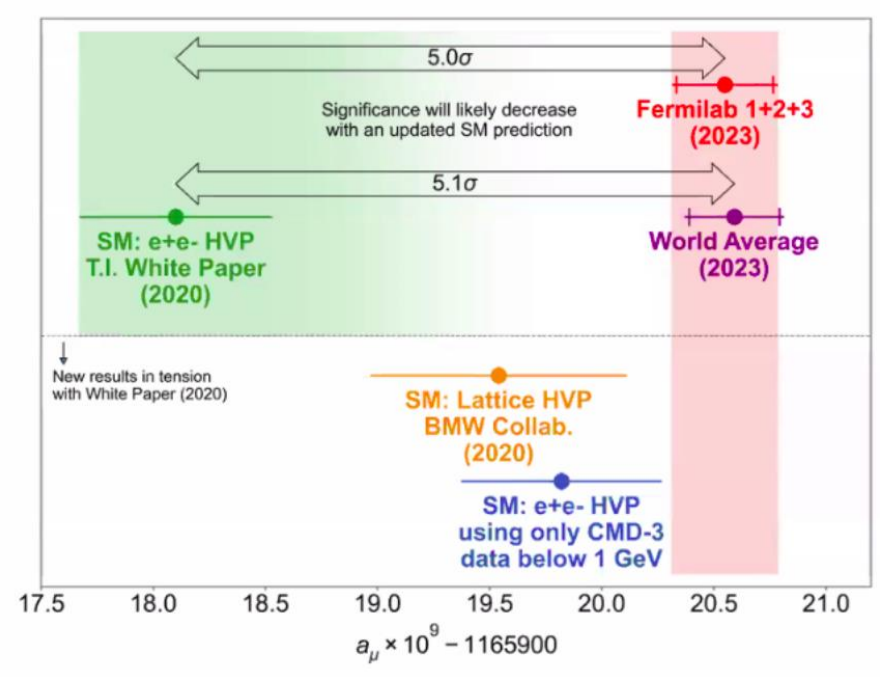
Nov 22 (Fri)

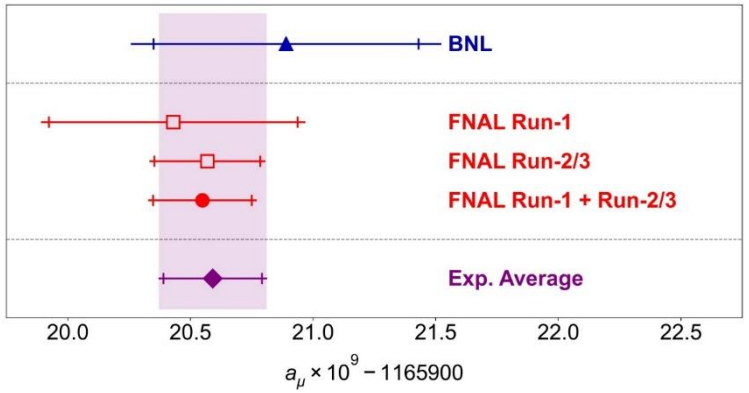


Evidences – Muon g-2

Muon g-2 collaboration, PRL 2023

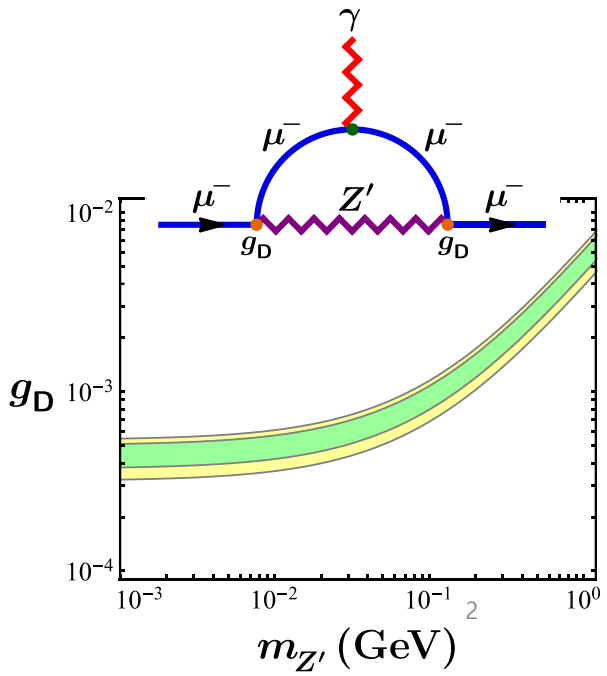
- Muon g-2 experiment improves the precision of their previous result by a factor of 2





S. Baek, Deshpande, He, P. Ko, 2001
S. Beak, P. Ko, 2008
…

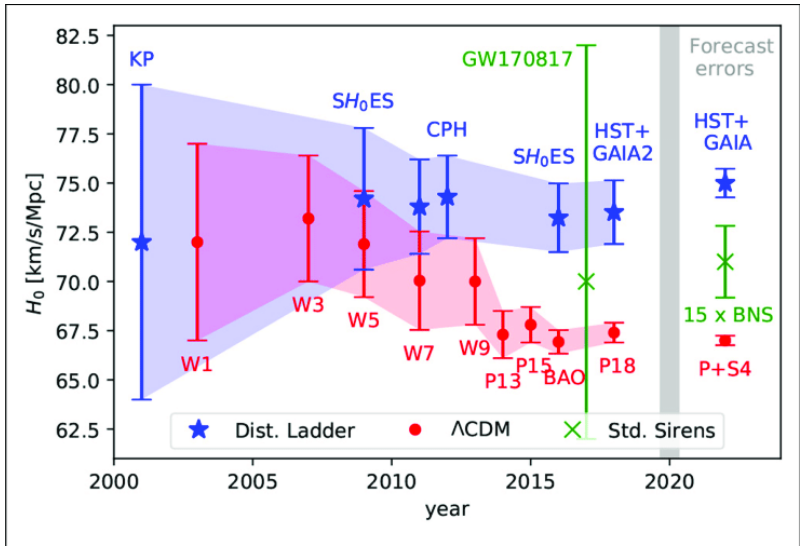
$$\Delta a_\mu = \frac{g_x^2}{4\pi^2}\int_0^1 dx \frac{m_\mu^2 x^2(1-x)}{x^2 m_\mu^2 + (1-x)m_{Z'}^2}$$



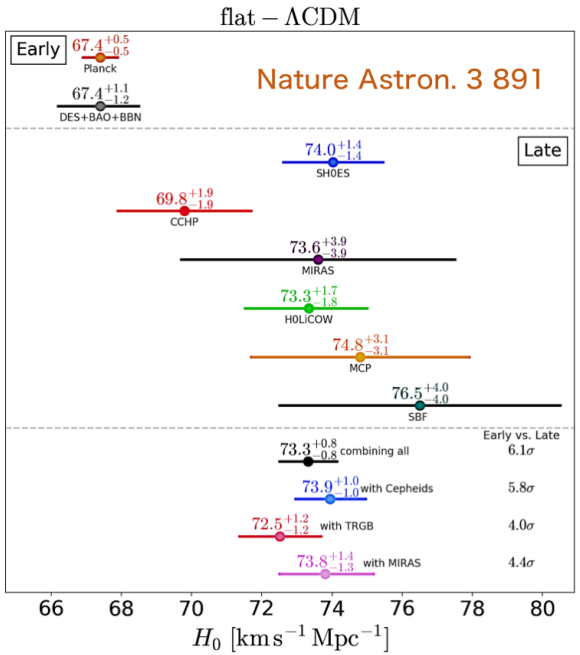
Evidences – Hubble tension

- Large difference between early and late H_0 measurement
  - Late-time: $H_0 = 73.2 \pm 1.3\ \mathrm{km s^{-1} Mpc^{-1}}$
  - Early-time: $H_0 = 67.4 \pm 0.5\ \mathrm{km s^{-1} Mpc^{-1}}$

- The discrepancy either arises because
  - Our distance measurements are incorrect (ΔG_N)
  - Cosmological model we use to fit all those distances is incorrect (ΔN_{eff})

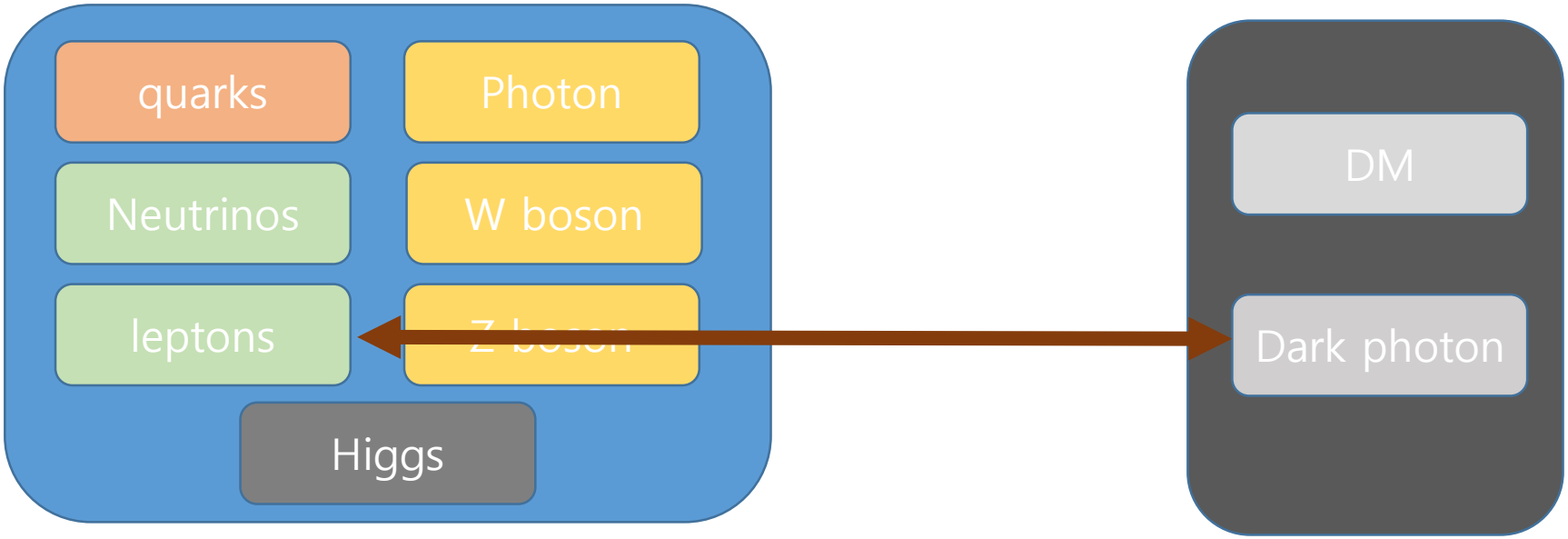


P. Shah et al, AAR 2021



$U(1)_{L_\mu - L_\tau}$-charged DM model

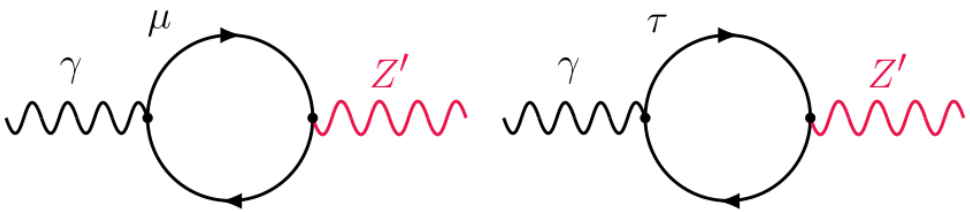
- $U(1)_{dark} \equiv U(1)_{L_\mu - L_\tau}$



- Let's call Z', $U(1)_{L_\mu - L_\tau}$ gauge boson, dark photon since it couple to DM

Gauged $U(1)_{L_\mu - L_\tau}$ Z' model

- Gauge one of the differences of two lepton-flavor numbers
  - $L_e - L_\mu, L_\mu - L_\tau, L_e - L_\tau$: anomaly free without extension of fermion contents **X. G. He et al, PRD 1991**
  - Symmetry including L_e is strongly constrained
  - Charge assignments: $\hat{\mathcal{Q}}_{\mathsf{L}_\mu - \mathsf{L}_\tau}(\nu_\mu, \nu_\tau, \mu, \tau) = (1, -1, 1, -1)$

- No kinetic mixing between Z' and B @ high-energy
  - Kinetic mixing is generated through
  - 

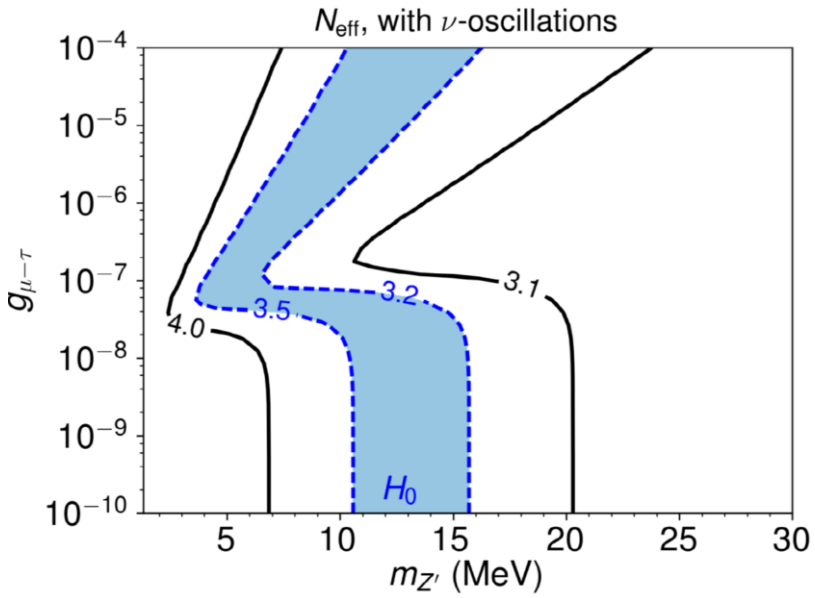
  - $\epsilon = -\frac{e g_{\mu-\tau}}{2\pi^2} \int_0^1 dx\, x(1-x) \log\left[\frac{m_\tau^2 - x(1-x)q^2}{m_\mu^2 - x(1-x)q^2}\right] \xrightarrow[m_\mu \gg q]{} -\frac{e g_{\mu-\tau}}{12\pi^2} \log\frac{m_\tau^2}{m_\mu^2} \simeq -\frac{g_{\mu-\tau}}{70}.$

Gauged $U(1)_{L_\mu - L_\tau}$ Z' model

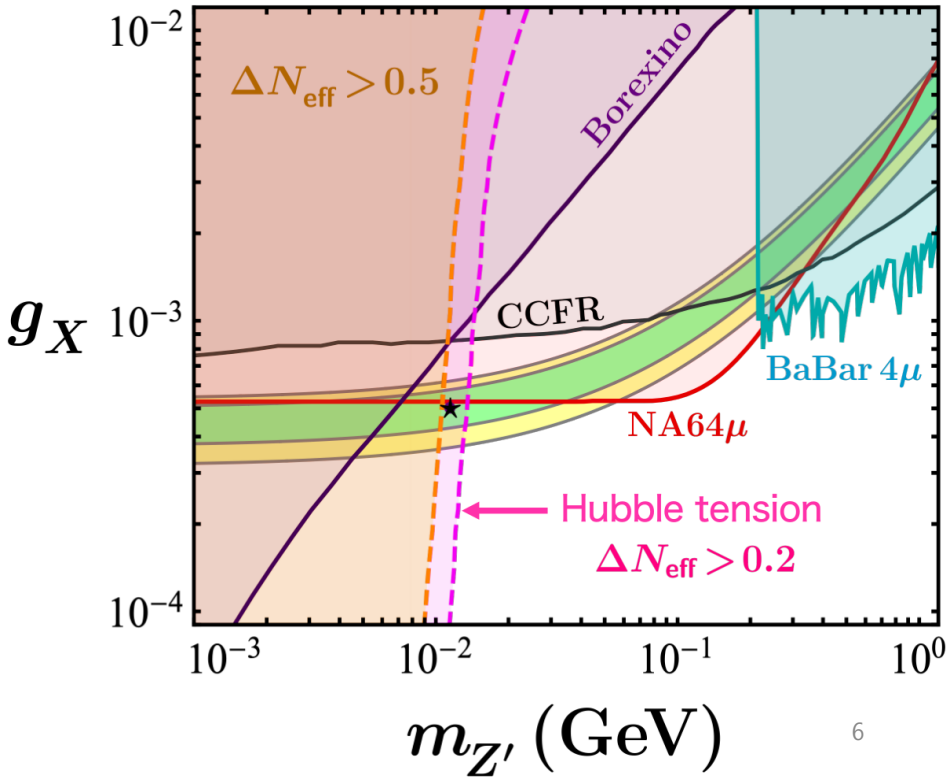
- ***Hubble tension***

M. Escudero et al, JHEP 2019

  - $\sim 10\text{MeV}$ Z' reached thermal equilibrium in the early Universe and decays, heating the neutrino population.
  - The expansion rate of the universe departed from the predictions of standard ΛCDM cosmology at early times
  - $0.2 < \Delta N_{\text{eff}} < 0.5$



- BP : $m_{Z'} = 11.5\text{MeV}$, $g_X = 5 \times 10^{-4}$



$U(1)_{L_\mu - L_\tau}$-charged DM model

- $U(1)_{L_\mu - L_\tau}$-charged scalar DM model

$$\mathcal{L}_{\text{int}} = i g_X Z'_\mu \left(X^* \partial^\mu X - X \partial^\mu X^*\right) + g_X Z'_\alpha \sum Q_\ell \bar{\ell} \gamma^\alpha \ell$$

  - Free parameters: $\{m_{Z'}, g_X, m_X, Q_X\}$
  - Dark Photon Z' plays a role of messenger particle between DM and the SM leptons
  - Dark Photon mass is generated Proca or Stueckelberg mechanism



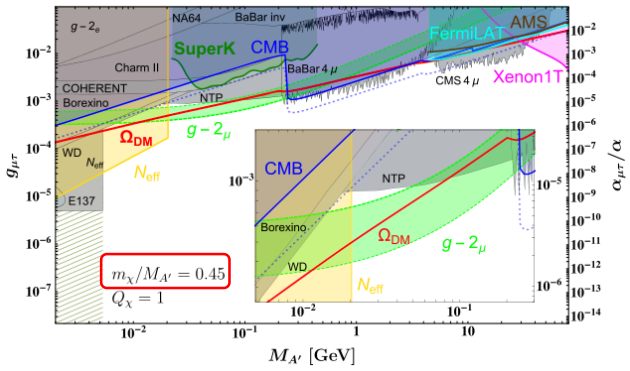
Only when $m_X > m_{Z'}$

- Consider Z' boson only & **$g_X \sim (3-5) \times 10^{-4}$ for the muon g-2**
  - $X\bar{X} \to f_{SM}\bar{f}_{SM}$: dominant annihilation channels

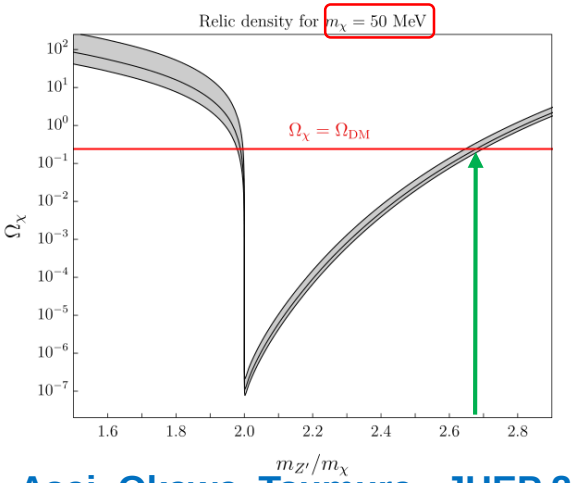
$U(1)_{L_\mu - L_\tau}$-charged DM model

- $XX^\dagger \to Z'^* \to \nu\bar{\nu}$: dominant annihilation channels
  - $m_{Z'} \sim 2m_X$ with the **s-channel Z' resonance** only gives the correct relic density

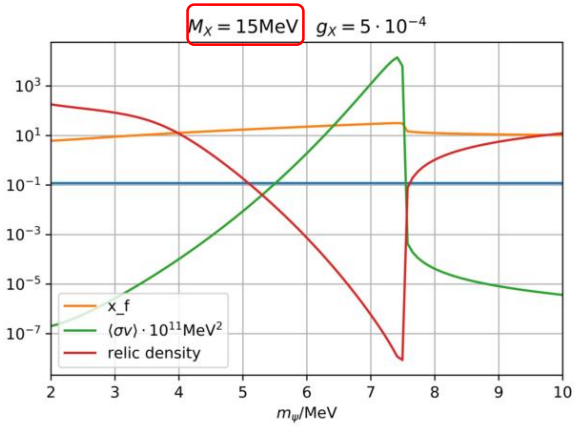
P. Foldenauer, PRD 2019



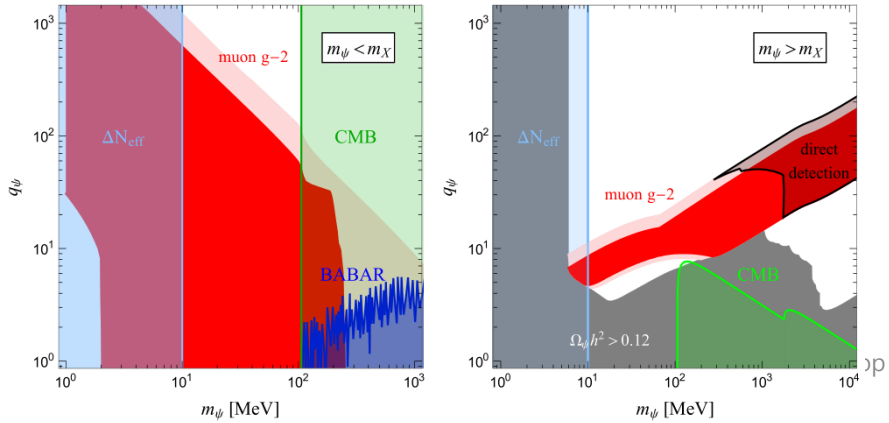
I. Holst, D. Hooper, G. Krnjaic, PRL 2022

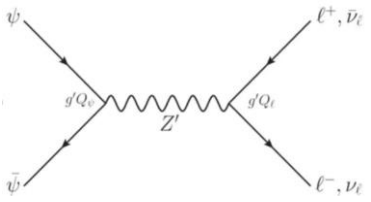


M. Drees, W. Zhao, PLB 2022



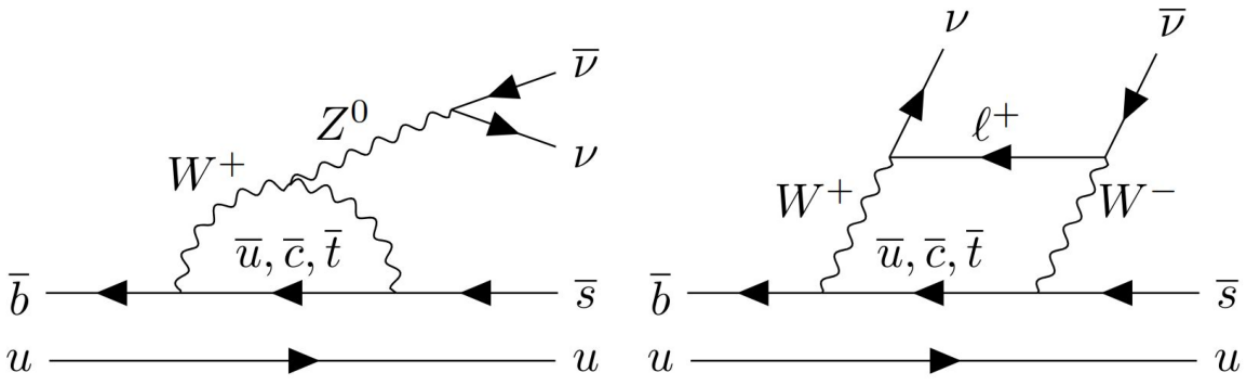
- Large DM charges **Asai, Okawa, Tsumura, JHEP 2021**





Measurement of $B^+ \to K^+ \nu\bar{\nu}$

- The $B^+ \to K^+ \nu\bar{\nu}$ process is known with high accuracy in the SM:
  - $Br(B^+ \to K^+ \nu\bar{\nu}) = (4.97 \pm 0.37) \times 10^{-6}$ **HPQCD, PRD 2023**



- $\mathcal{L}_{b\to s\nu\bar{\nu}} = -C_\nu \bar{s}_L \gamma^\mu b_L \bar{\nu}\gamma^\mu \nu$

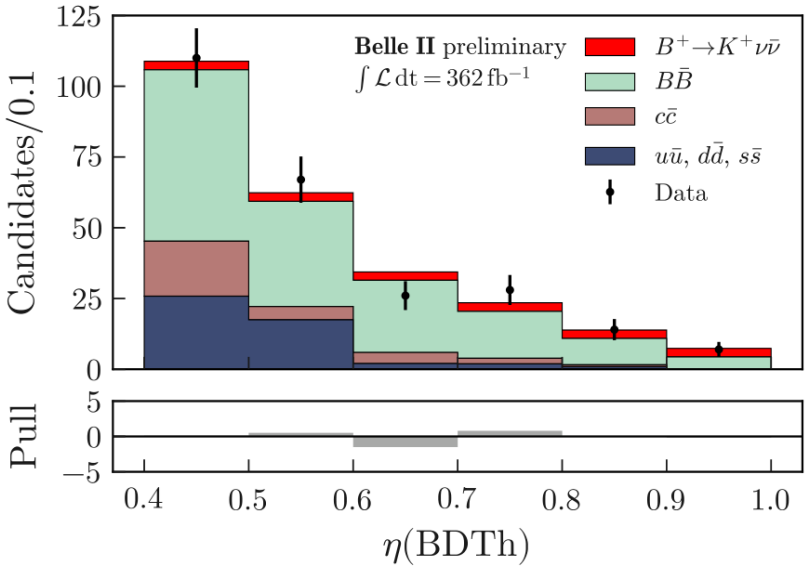
$$C_\nu = \frac{g_W^2}{M_W^2} \frac{g_W^2 V_{ts}^* V_{tb}}{16\pi^2} \left[\frac{x_t^2 + 2x_t}{8(x_t - 1)} + \frac{3x_t^2 - 6x_t}{8(x_t - 1)^2} \ln x_t \right],$$

where $x_t = m_t^2 / M_W^2$.

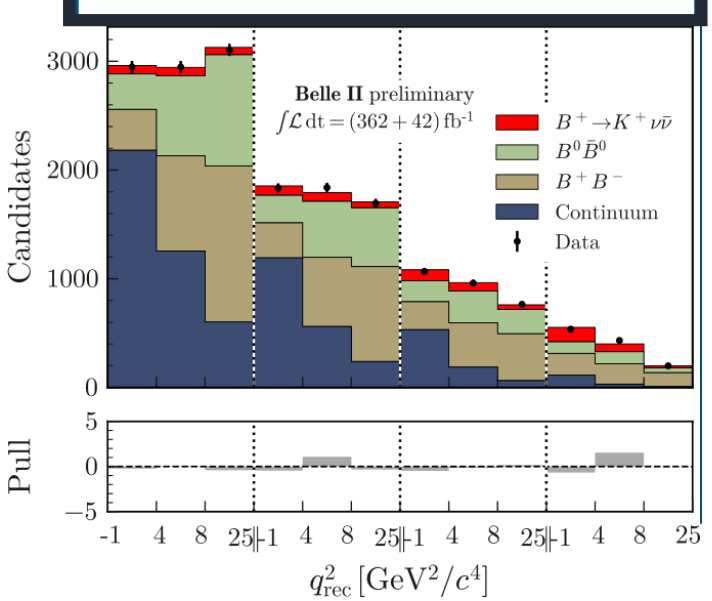
Measurement of $B^+ \to K^+ \nu\bar{\nu}$

- **Two ways** of tagging
  - HTA: Better resolution, purity
  - ITA: Better efficiency

Hadronic tagging (HTA)



Inclusive tagging (ITA)

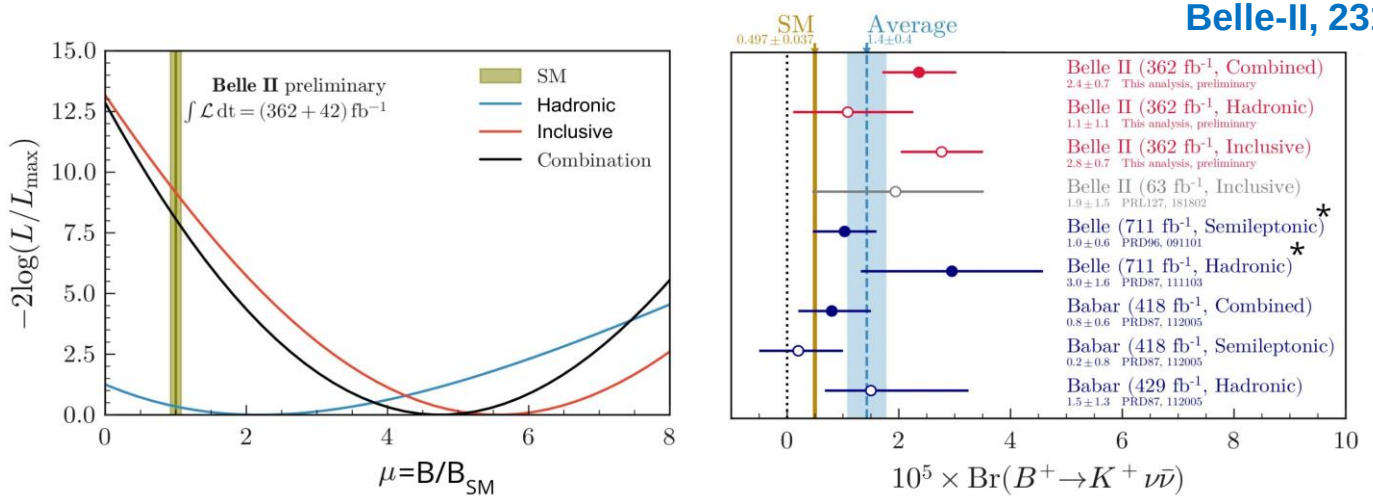


$$\mathcal{B}(B^+ \to K^+ \nu\bar{\nu})_{\text{HTA}} = (1.1^{+0.9+0.8}_{-0.8-0.5}) \times 10^{-5}$$

$$\mathcal{B}(B^+ \to K^+ \nu\bar{\nu})_{\text{ITA}} = (2.7 \pm 0.5 \pm 0.5) \times 10^{-5}$$

Measurement of $B^+ \to K^+\nu\bar{\nu}$

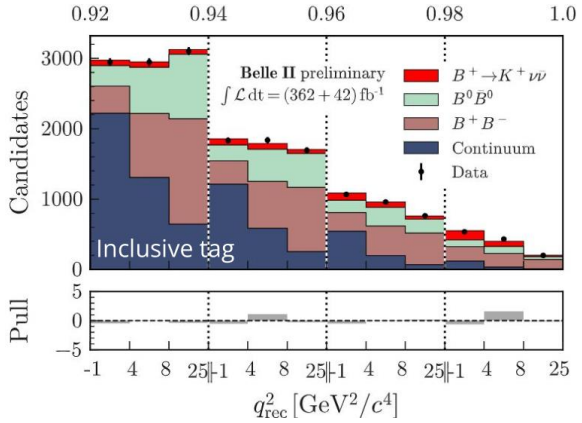
Belle-II, 2311.14647

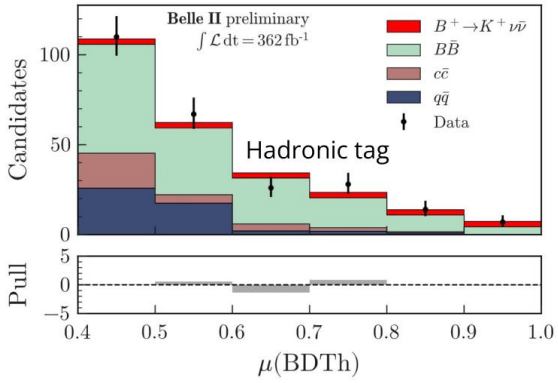


- $Br(B^+ \to K^+\nu\bar{\nu})_{Exp} = (2.3 \pm 0.7) \times 10^{-5}$
  - Prob(null signal from $B^+ \to K^+\nu\bar{\nu}$) = 0.012%
  - ➔ Significance of observation: 3.5 σ
  - Prob$(B^+ \to K^+\nu\bar{\nu})_{SM}$ = 0.17% (2.8σ tension with the SM prediction)

- $Br(B^+ \to K^+ E_{\mathrm{mis}})_{NP} = (1.8 \pm 0.7) \times 10^{-5}$
  - **Indirect NP effects**: The presence of heavy NP particles
  - **Direct NP effects**: the presence of new invisible particles

Solutions: 2- or 3-body decay

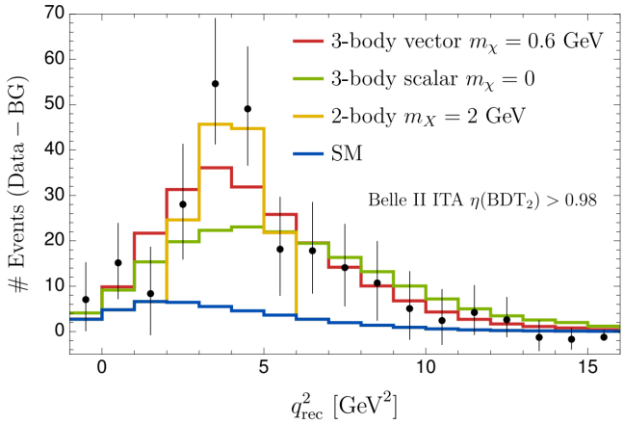


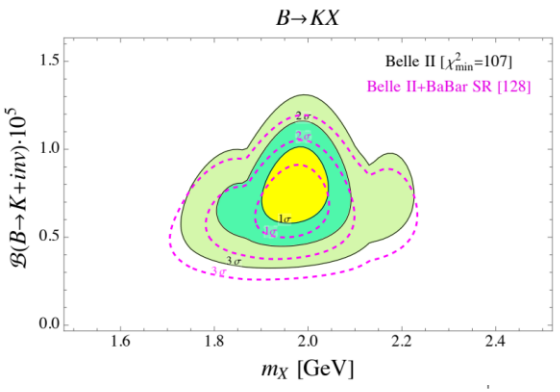


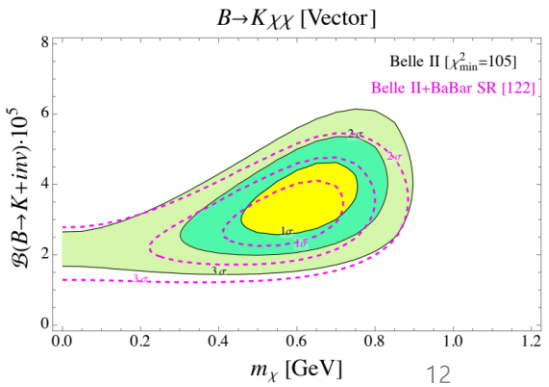
- Belle II provides information on the q^2_{rec} spectrum
  - q^2_{rec}: mass squared of the neutrino pair
  - A peak localized around $q^2_{rec} = 4\text{GeV}^2$
  - Two-body decay $(B \to KX), m_X = 2$ GeV
  - Three-body decay $(B \to KXX), m_X < 0.6$ GeV

W. Altmannshofer et al, 2311.14629

K. Fridell et al, 2312.12507







Can we find the integrated solution of Δa_μ, DM relic density, Hubble tension and $B^+ \to K^+ \nu\bar{\nu}$ at Belle II?

$U(1)_{L_\mu - L_\tau}$-charged DM model

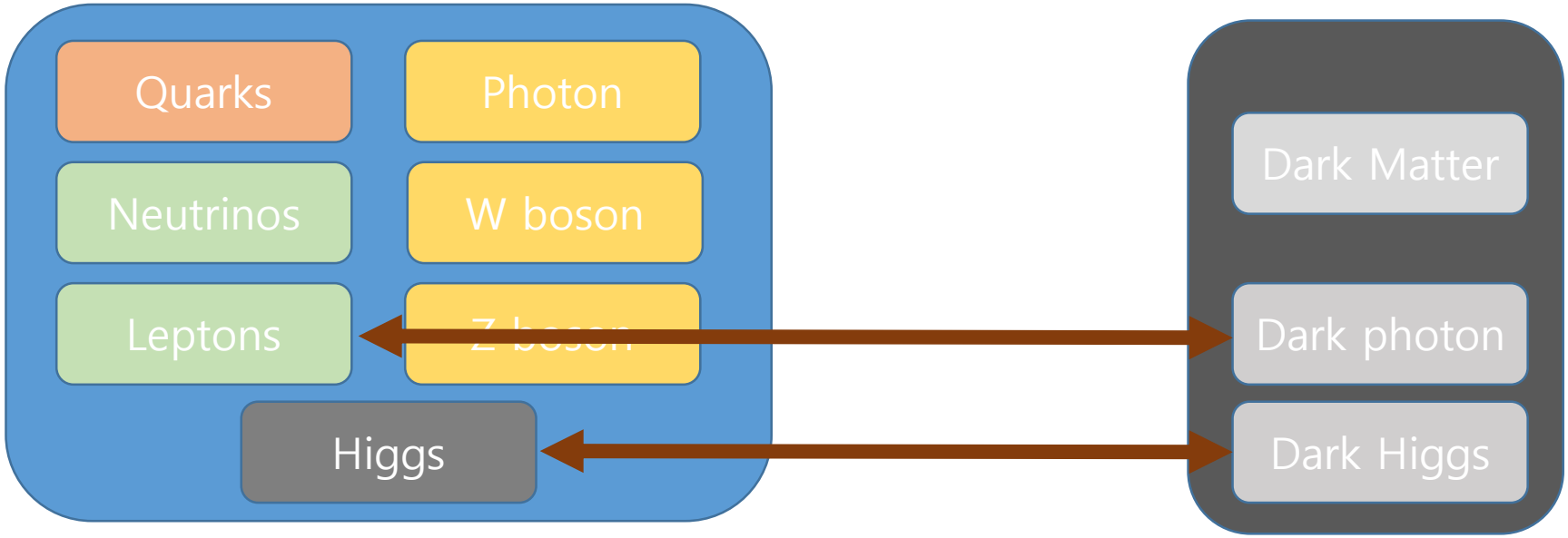
- **Muon g-2**
  - $m_{Z'} \sim O(10)\mathrm{MeV}$, & $g_X \sim 10^{-4}$ is too small to get $\Omega h^2 = 0.12$
  - $m_{Z'} \sim 2m_X$ with the s-channel Z' resonance
  - Only sub-GeV **DM** available
  - Tight correlation between DM mass and $\boldsymbol{Z'}$ mass
- No DM direct detection bound
  - DM-nucleon scattering: $\sigma_{\mathrm{el}}^{X-p} \simeq 10^{-46}\mathrm{cm}^2$
  - DM-electron scattering: $\sigma_{\mathrm{el}}^{X-e} \simeq 10^{-45}\mathrm{cm}^2$

$U(1)_{L_\mu - L_\tau}$-charged DM model

- **Muon g-2**
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  - DM-electron scattering: $\sigma_{\text{el}}^{X-e} \simeq 10^{-45}\text{cm}^2$
- **BelleII excess**
  - $B \to KZ'$ (2-body decay)
    ➔ disfavored by q^2 spectrum
  - $B \to K\boldsymbol{X}\boldsymbol{X}^\dagger$(3-body decay)
    ➔ suppressed by kinetic mixing and $g_X \sim 10^{-4}$

$U(1)_{L_\mu - L_\tau}$-charged DM + Dark Higgs

- $U(1)_{dark} \equiv U(1)_{L_\mu - L_\tau}$
  - Let's call Z',$U(1)_{L_\mu - L_\tau}$ gauge boson, dark photon since it couple to DM



- **UV complete** $U(1)_{L_\mu - L_\tau}$-charged **scalar** DM model
- Dark photon Z' gets massive through $U(1)_{L_\mu - L_\tau}$ breaking
- A new singlet scalar (**Dark Higgs**), which mixes with the SM Higgs

$U(1)_{L_\mu - L_\tau}$-charged DM + Dark Higgs

- After electroweak and $U(1)_{L_\mu - L_\tau}$ symmetry breaking

$$\mathcal{H} = \frac{1}{\sqrt{2}}(0 \;\; v_H + h)^\intercal \;, \;\; \Phi = \frac{1}{\sqrt{2}}(v_\Phi + \phi)$$

- Dark photon Z' gets massive: $m_{Z'} = g_X |Q_\Phi| v_\Phi$

- Two CP-even neutral scalar bosons mix each other due to non-zero of $\lambda_{H\Phi}$

$$H_1 = \phi \cos\theta - h \sin\theta \;, \;\; H_2 = \phi \sin\theta + h \cos\theta$$

dark Higgs boson — SM-like Higgs boson — mixing angle

$$m_{H_1} < m_{H_2} \simeq 125\,\text{GeV}$$

$U(1)_{L_\mu - L_\tau}$-charged DM + Dark Higgs

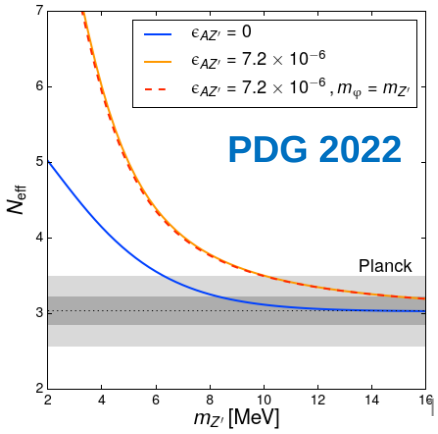
- Additional interactions with the dark Higgs

$$\mathcal{L}_\phi \supset \frac{1}{2} g_X^2 Q_\Phi^2 Z'^\mu Z'_\mu \phi^2 + g_X^2 Q_\Phi^2 v_\Phi Z'^\mu Z'_\mu \phi - \lambda_\Phi v_\Phi \phi^3 - \lambda_H v_H h^3 - \frac{\lambda_{\Phi H}}{2} v_\Phi \phi h^2 - \frac{\lambda_{\Phi H}}{2} v_H \phi^2 h$$

- **The SM-like Higgs invisible decay**
  - $\boldsymbol{H_2 \to H_1 H_1, Z'Z', XX^\dagger}$
  - SM Higgs mainly decays into dark photon and dark Higgs

$$\Gamma_{H_2 \to H_1 H_1} \simeq \Gamma_{H_2 \to Z'Z'} \propto \frac{\sin^2\theta\, m_{H_2}^3}{v_\Phi^2} \gg \Gamma_{H_2 \to X X^\dagger} \propto \frac{\sin^2\theta\, \lambda_{\Phi X}^2 v_\Phi^2}{m_{H_2}}$$

- $\mathrm{Br}(H_2 \to \mathrm{inv.}) = \dfrac{\Gamma_{H_2}^{ZZ^* \to 4\nu} + \Gamma_{H_2}^{H_1 H_1} + \Gamma_{H_2}^{Z'Z'} + \Gamma_{H_2}^{XX^\dagger}}{\Gamma_{H_2}^{SM} + \Gamma_{H_2}^{H_1 H_1} + \Gamma_{H_2}^{Z'Z'} + \Gamma_{H_2}^{XX^\dagger}} < 13\%$
- $sin\theta \leq 0.01$ to satisfy the Higgs invisible decay

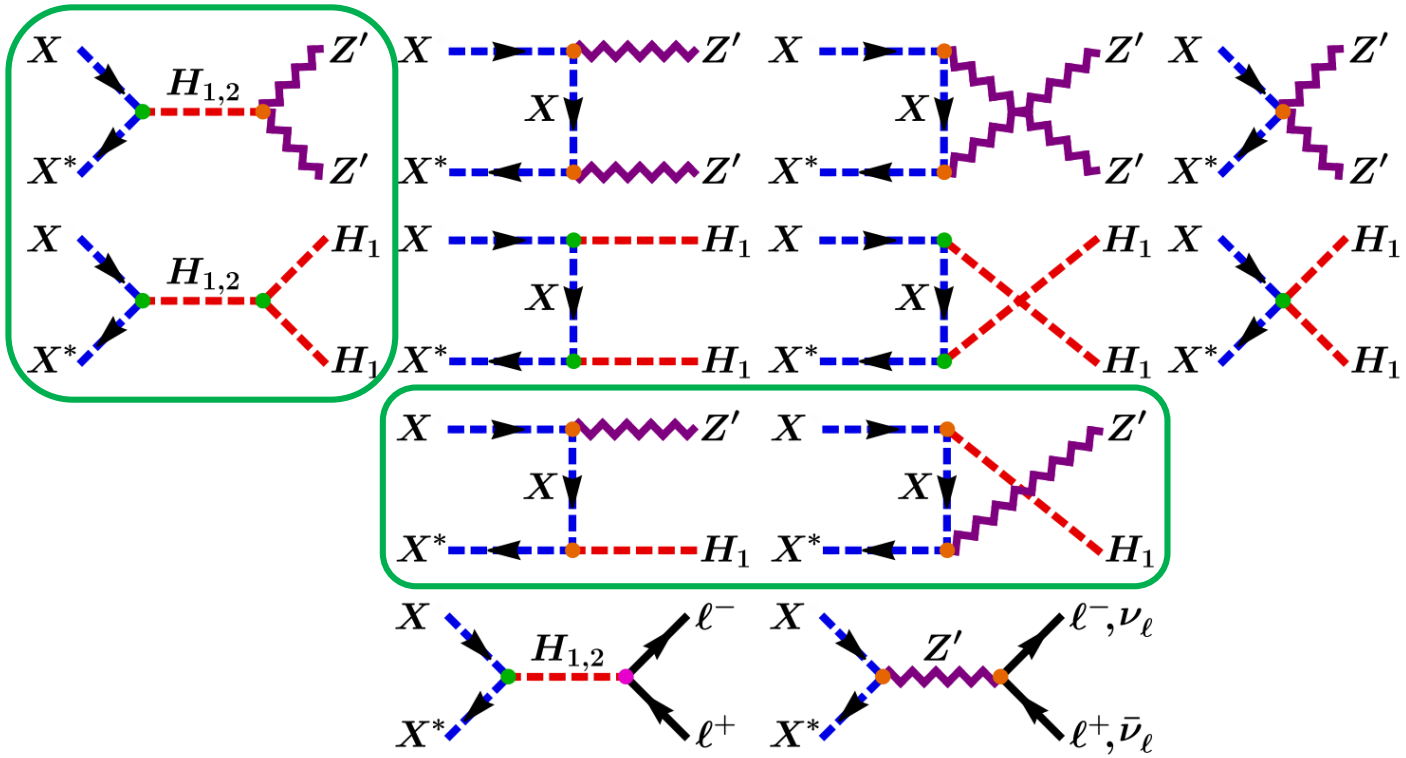


$U(1)_{L_\mu - L_\tau}$-charged DM + Dark Higgs

- UV-complete $U(1)_{L_\mu - L_\tau}$-charged scalar DM model Baek, **JK**, Ko, 2204.04889

$$\mathcal{L}_{\rm DM} = |D_\mu X|^2 - m_X^2 |X|^2 - \lambda_{\Phi X} |X|^2 \left(|\Phi|^2 - \frac{v_\Phi^2}{2} \right)$$

- Free parameters: $\{ m_{Z'}, g_X, \sin\theta, m_X, m_{H_1}, Q_\Phi, \lambda_{\Phi X} \}$



$U(1)_{L_\mu - L_\tau}$-charged DM + Dark Higgs

Baek, **JK**, Ko, 2204.04889

- Thermal WIMP DM relic density

$$\Omega_{\rm WIMP}\hat{h}^2 = 2\Omega_X\hat{h}^2 \simeq \frac{1.75\times 10^{-10}{\rm GeV}^{-2}x_f}{\sqrt{g_*}\langle\sigma v\rangle} \qquad x_f \equiv \frac{m_X}{T_f} \sim 12-19, \quad g_* \sim 10$$

- DM direct detection
  - $U(1)_{L_\mu - L_\tau}$ DM model without dark Higgs boson, DM-nucleon/electron scattering is highly suppressed: $\sigma_{\rm el}^{X-p} \simeq 10^{-46}{\rm cm}^2, \sigma_{\rm el}^{X-e} \simeq 10^{-51}{\rm cm}^2$
  - We can have a sizable DM-nucleon scattering due to the dark Higgs boson exchange

$$\sigma_{\rm el} \simeq \frac{4\mu_n^2 f_n^2 \lambda_{\Phi X}^2 \sin^2\theta}{\pi}\left(\frac{m_n}{m_X}\right)^2\left(\frac{v_\Phi}{v_H}\right)^2\left(\frac{1}{m_{H_1}^2}-\frac{1}{m_{H_2}^2}\right)^2$$

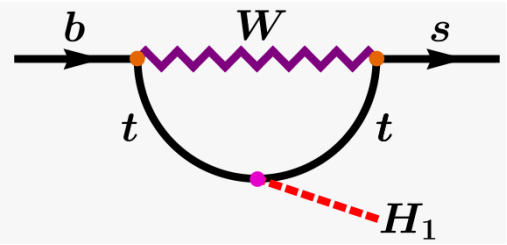
BelleII excess: 2- or 3-body decay

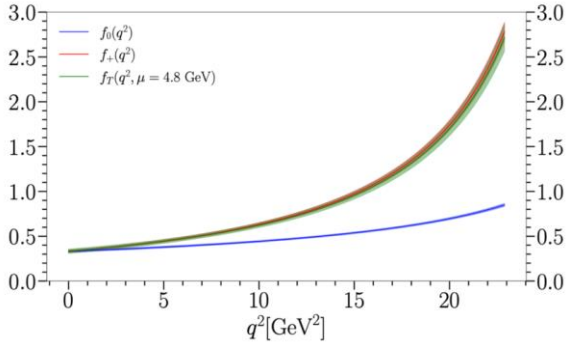
- When $m_{H_1} < m_B - m_K$, H_1 is on-shell

$$\Gamma_{B^+\to K^+H_1} \simeq \frac{|\kappa_{cb}|^2 \sin^2\theta}{64\pi m_{B^+}^3}\left(\frac{m_{B^+}^2 - m_{K^+}^2}{m_b - m_s}\right)^2 \left[f_0(m_{H_1}^2)\right]^2 \times \sqrt{\mathcal{K}(m_{B^+}^2, m_{K^+}^2, m_{H_1}^2)} \qquad \sin\theta \ll 1$$

form factor

$$|\kappa_{cb}| \simeq 6.7 \times 10^{-6} \qquad \mathcal{K}(a,b,c) = a^2 + b^2 + c^2 - 2(ab + bc + ca)$$

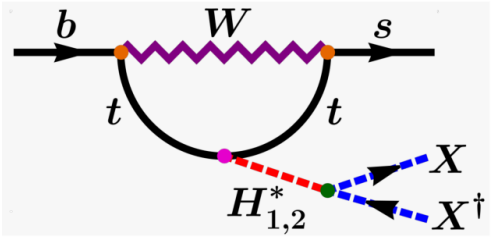




W. G. Parrott, C. Bouchard & C. T. H. Davies, ORD 2023

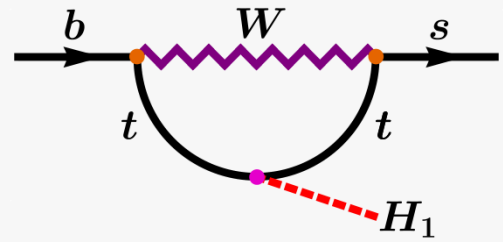
- When $m_{H_1} > m_B - m_K$, H_1 is off-shell → three-body decay

$$\Gamma_{B^+\to K^+XX^\dagger} \simeq \frac{\lambda_{\Phi X}^2 v_\Phi^2 |\kappa_{cb}|^2 \sin^2\theta}{1024\pi^3 m_{B^+}^3}\left(\frac{m_{B^+}^2 - m_{K^+}^2}{m_b - m_s}\right)^2 (m_{H_1}^2 - m_{H_2}^2)^2 \times \int_{4m_X^2}^{(m_{B^+}-m_{K^+})^2} dq^2 \frac{\sqrt{1 - 4m_X^2/q^2}\sqrt{\mathcal{K}(m_{B^+}^2, m_{K^+}^2, q^2)}\left[f_0(q^2)\right]^2}{(q^2 - m_{H_1}^2)^2 (q^2 - m_{H_2}^2)^2}$$

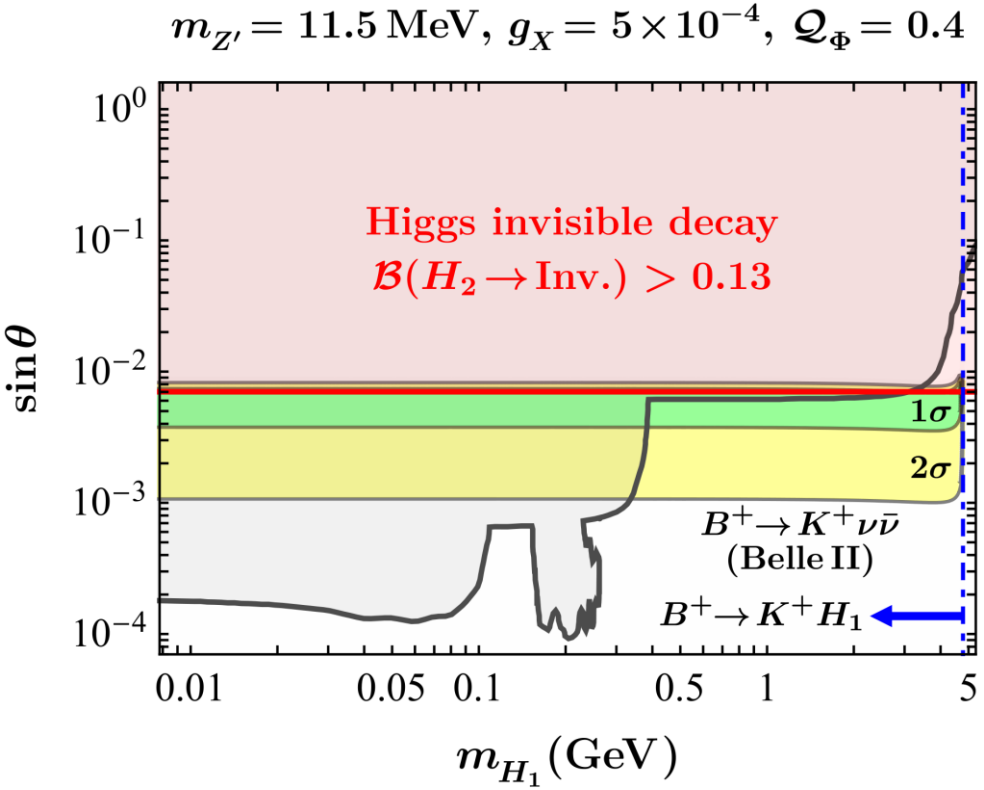


BelleII excess: 2-body decay

- When $m_{H_1} < m_B - m_K$, H_1 is on-shell
- The gray shaded area is excluded by BelleII $B^0 \to K^{*0}\nu\bar{\nu}$, KOTO $K_L^0 \to \pi^0\nu\bar{\nu}$ & NA62 $K^+ \to \pi^+$+ inv.

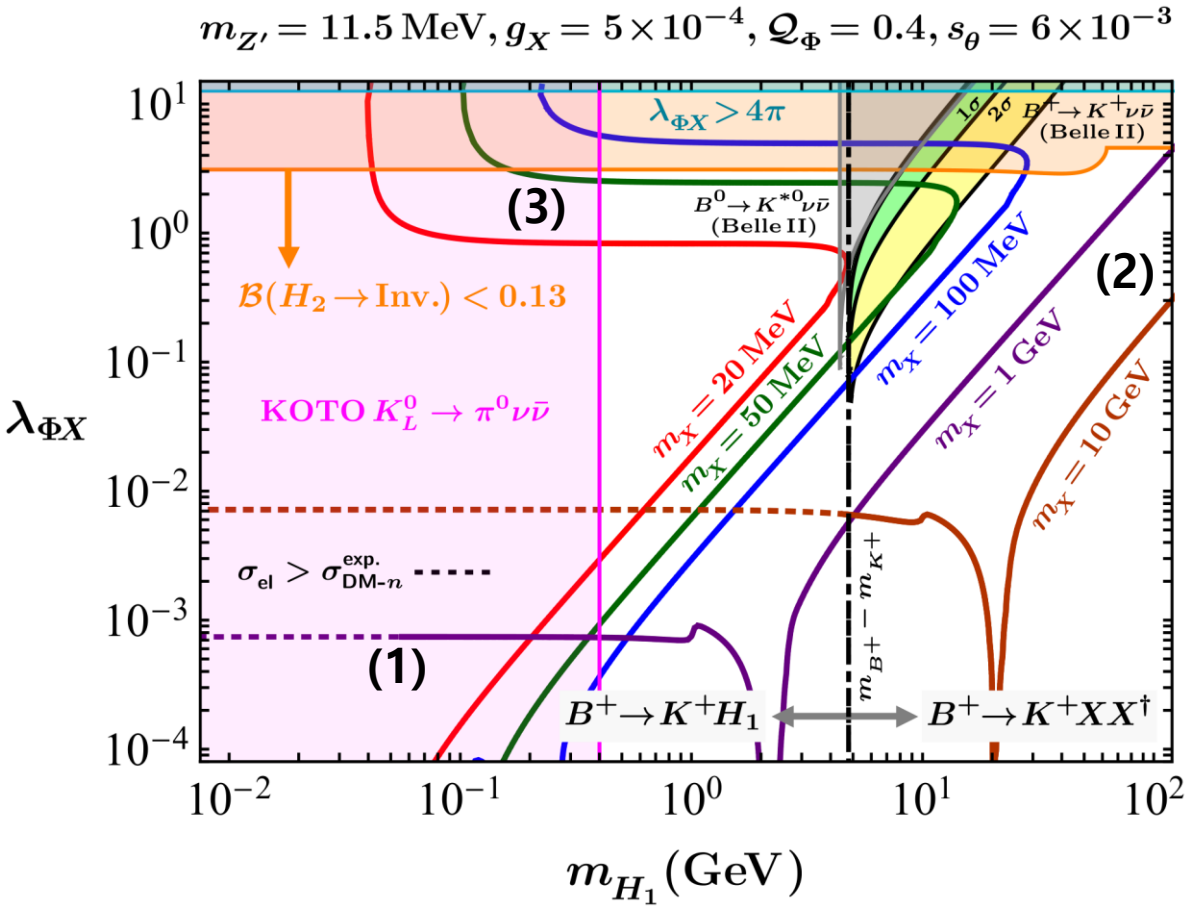


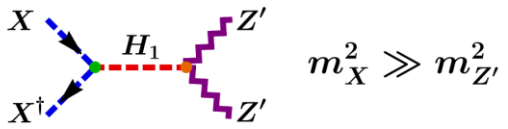
- H_1 decay process
  - $H_1 \to XX^\dagger, Z'Z', f\bar{f}$
- Allowed value
  - $10^{-3} \leq \sin\theta \leq 7 \times 10^{-3}$
  - take $\sin\theta = 6 \times 10^{-3}$



BelleII excess : 2- or 3-body decay

- When $m_{H_1} > (<)\ m_B - m_K$, H_1 is off(on)-shell → 3(2)-body decay
  - Two-body decay: $m_X \lesssim 10\ \mathrm{GeV}\ (m_{H_1} < m_B - m_K)$
  - Three-body decay: $20\mathrm{MeV} < m_X \lesssim 60\mathrm{MeV}\ (m_{H_1} > m_B - m_K)$





$m_X^2 \gg m_{Z'}^2$

$$\langle\sigma v\rangle \propto \frac{\lambda_{\Phi X}^2 m_X^2}{(m_{H_1}^2 - 4m_X^2)^2 + \Gamma_{H_1}^2 m_{H_1}^2}$$

$$\Gamma_{H_1}^2 m_{H_1}^2 \propto \lambda_{\Phi X}^4 v_\Phi^4 \sqrt{1 - 4m_X^2/m_{H_1}^2}$$

(1) $\lambda_{\Phi X} \ll 1$ & $m_X^2 \gg m_{H_1}^2$

$$\Rightarrow \langle\sigma v\rangle \propto \frac{\lambda_{\Phi X}^2}{m_X^2} \Rightarrow \lambda_{\Phi X} \simeq \text{const.}$$

(2) $\lambda_{\Phi X} \ll 1$ & $m_{H_1}^2 \gg m_X^2$

$$\Rightarrow \langle\sigma v\rangle \propto \frac{\lambda_{\Phi X}^2 m_X^2}{m_{H_1}^4} \Rightarrow \lambda_{\Phi X} \propto m_{H_1}^2$$

(3) $\lambda_{\Phi X} \gg 1$ & $m_{H_1}^2 \gg m_X^2$

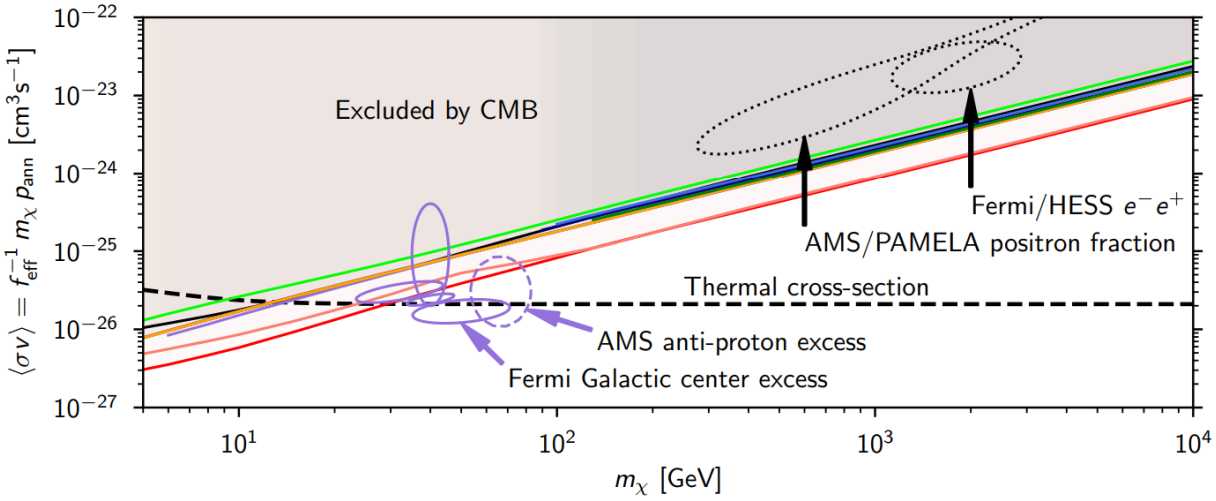
$$\Rightarrow \langle\sigma v\rangle \propto \frac{m_X^2}{\lambda_{\Phi X}^2 v_\Phi^4} \Rightarrow \lambda_{\Phi X} \simeq \text{const.}$$

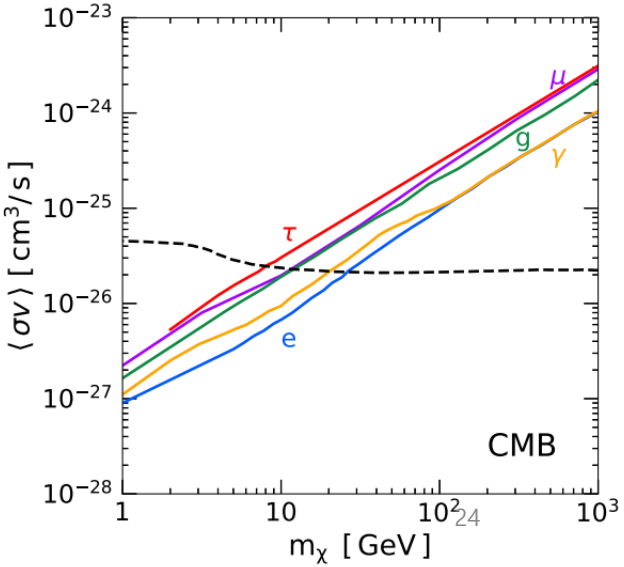
CMB constraints

- Any injection of ionizing particles modifies the ionization history of hydrogen and helium gas, perturbing CMB anisotropies
  - DM annihilations to the charged SM particles
- Measurements of these anisotropies provide robust constraints on production of ionizing particles from DM annihilation products.

$$\langle \sigma v \rangle \leqslant \frac{4.1 \times 10^{-28}\,\mathrm{cm^3\,sec^{-1}}}{f_{\mathrm{eff}}} \left(\frac{m_{\mathrm{DM}}}{\mathrm{GeV}} \right)$$

Planck 2018,
R. K. Leane et al, PRD 2018





CMB constraints

- For $m_X \lesssim 20\mathrm{GeV}$, CMB bound (DM annihilation @ $T \sim \mathrm{eV}$) excludes the thermal DM freeze-out determined by *s-wave* annihilation
  - DM annihilation should be mainly in **p-wave**
  - …

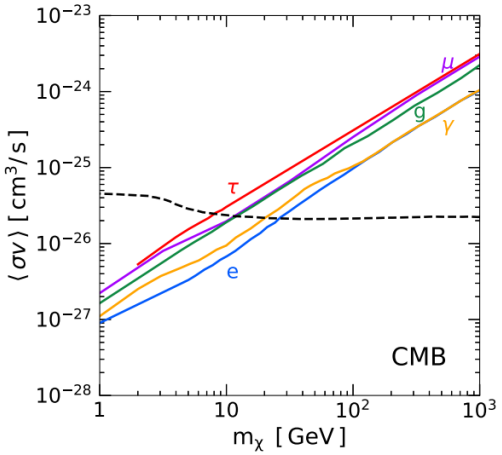
$$\sigma v = a + b v^2 + O(v^4)$$

p-wave (the $b v^2$ term)

s-wave (the a term)

- Dominant DM annihilation channel
  - $XX^\dagger \to Z'Z', H_1H_1$: **s-wave** annihilation
  - $XX^\dagger \to Z'H_1$: **p-wave** annihilation
- Z' decay

- H_1 decay



CMB constraints

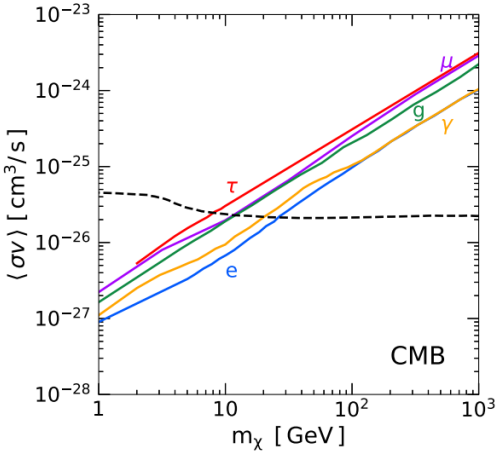
- For $m_X \lesssim 20\mathrm{GeV}$, CMB bound (DM annihilation @ $T \sim \mathrm{eV}$) excludes the thermal DM freeze-out determined by *s-wave* annihilation
  - DM annihilation should be mainly in **p-wave**
  - …

$$\sigma v = a + b v^2 + O(v^4)$$

p-wave (the $b v^2$ term)

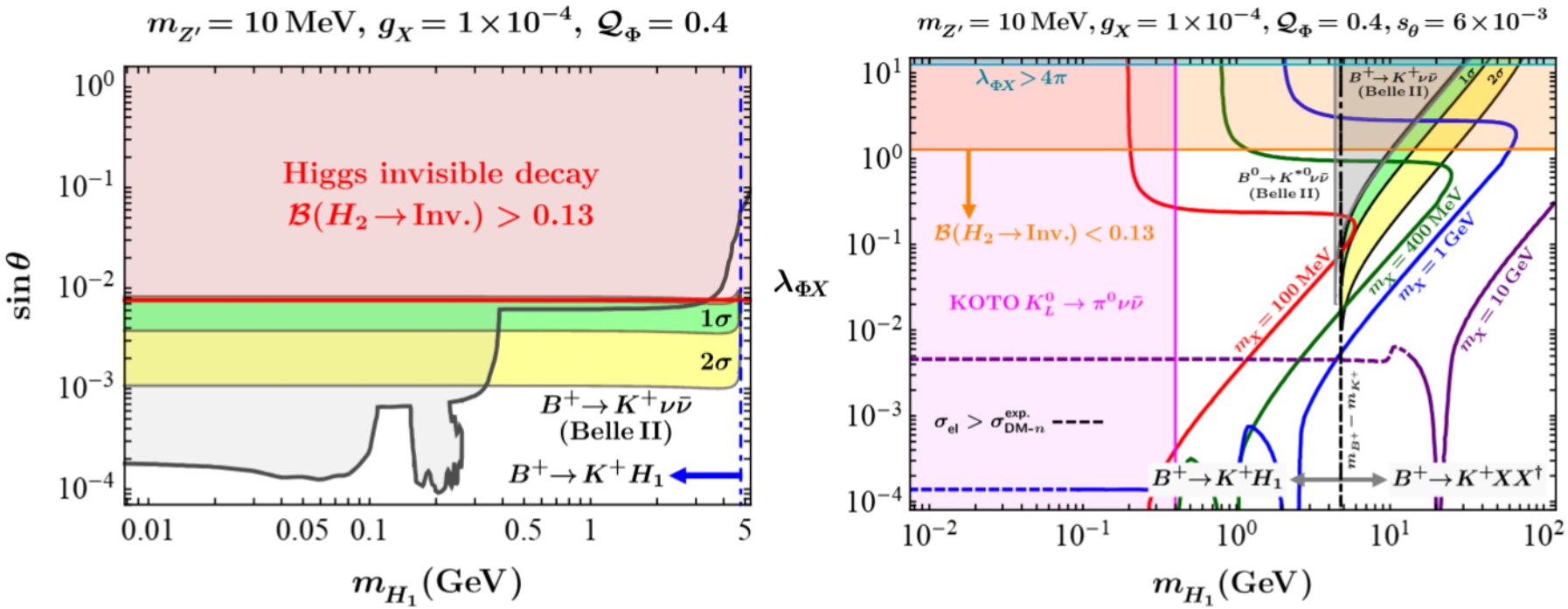
s-wave (the a term)

- Dominant DM annihilation channel
  - $XX^\dagger \to Z'Z', H_1H_1$: **s-wave** annihilation
  - $XX^\dagger \to Z'H_1$: **p-wave** annihilation
- Z' decay
  - A pair of ν
- H_1 decay
  - A pair of DM (open when $m_{H_1} > 2m_X$)
  - A pair of Z' ($Z' \to \nu\nu$)
  - SM particles (suppressed due to small Yukawa coupling & $\sin\theta$)



BelleII excess : 2- or 3-body decay

- $m_{Z'} = 10\text{MeV}$, $g_X = 10^{-4}$ ($m_{Z'} = g_X |Q_\Phi| v_\Phi$ → Larger v_Φ)
  - Hubble tension can be relaxed
  - $\Delta a_\mu = 10^{-10}$ **(BMW & CMD-3 collaboration)**
  - **Belle II** (2-body decay): $m_X \lesssim 8\ \text{GeV}$ $(m_{H_1} < m_B - m_K)$
  - **Belle II** (3-body decay): $\sim 90\text{MeV} < m_X \lesssim 450\text{MeV}$ $(m_{H_1} > m_B - m_K)$



Conclusions

- BelleII data shows a excess of $B^+ \to K^+ \nu\bar{\nu}$ over the SM prediction
- This excess can be interpreted as $B^+ \to K^+ +$ dark sector particles
- CMB constraints can be evaded because DM pair annihilations into $H_1 H_1, H_1 Z', Z'Z'$, all of which are invisible
- We can accommodate the muon g-2 and subsequently relax the tension in the Hubble constant with extra radiation

Conclusions

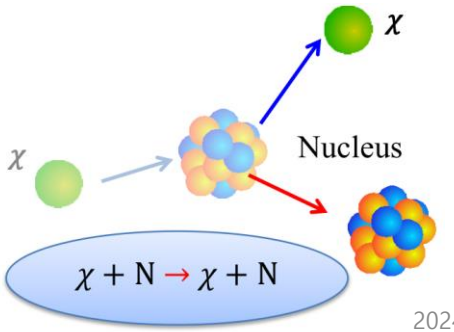
- BelleII data shows a excess of $B^+ \to K^+ \nu\bar{\nu}$ over the SM prediction
- This
part
- CM
into ions
- We
the tension in the Hubble constant with extra radiation x

Thank you very much

Back-up Slides

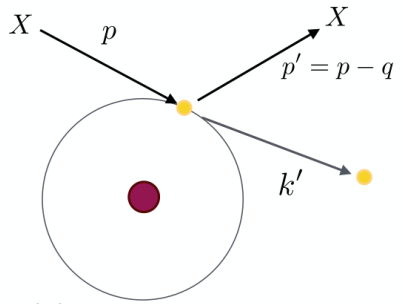
Thermal freeze-out DM Detection

- General idea:
  - The Earth is moving through dark matter medium. Or, from our point of view, there is a flux of dark matter particles going through the Earth
  - Once in a while a dark matter particle will interact with a nucleus or electron
  - The nucleus gains momentum and recoils. The existence of dark matter can then be inferred if there is a significant excess in the number of recoils compared to the expected recoils induced by natural radioactivity in the detector
- Try to observe recoil energy coming from DM scattering process
  - Nuclear Recoil (NR)
    - $E_R = 1\sim100$keV

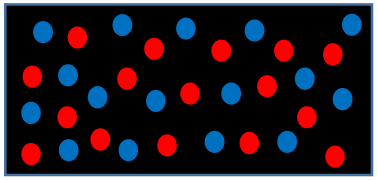


Electronic Recoil (ER)

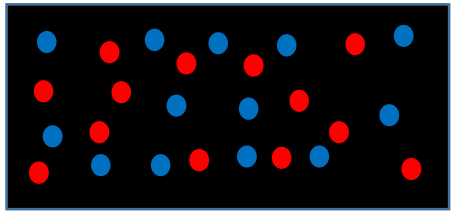
· Ionization



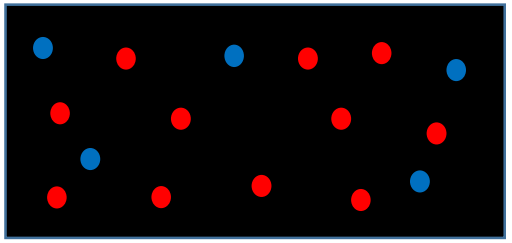
Evidences – Dark Matter



$T \gg M_{DM}$

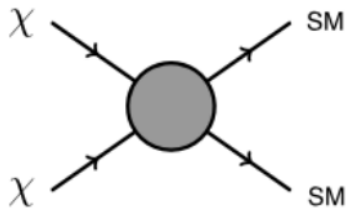


$T \approx M_{DM}$

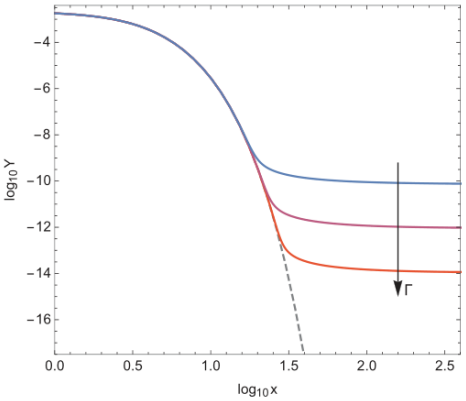


$T \ll M_{DM}$

- ● : Dark Matter
- ● : Standard Model

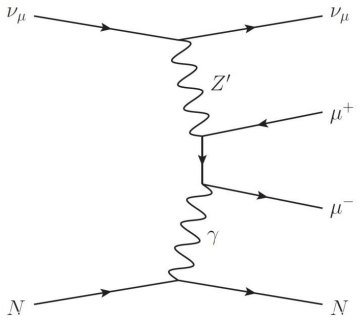


- Dark matter population in an expanding Universe
  - **Dark matter particles can no longer annihilate**
  - **The number of dark matter particles "freeze-out"**
- Standard calculation for WIMP DM relic density
  - The Boltzmann equation $\frac{dn_\chi}{dt} + 3Hn_\chi = -\langle\sigma v\rangle\left(n_\chi^2 - n_{\mathrm{eq}}^2\right)$
- Relic density: $\Omega h^2 = 0.12 \rightarrow \langle\sigma v\rangle \sim 10^{-9}\mathrm{GeV}^{-2}$



Gauged $U(1)_{L_\mu - L_\tau}$ Z' model

- ***Neutrino trident production*** **W. Altmannshofer et al, PRL 2014**
  - Production of a muon pair from the scattering of a muon neutrino with heavy nuclei
  - $R_{\mathrm{CCFR}} \equiv \frac{\sigma_{\mathrm{CCFR}}}{\sigma_{\mathrm{SM}}} = 0.82 \pm 0.28.$



- ***NA64*** **Y. Andreev, 2401.01708**
  - $\mu^- N \to \mu^- N Z', (Z' \to \mathrm{inv.})$
  - Upper limit on g_X for $1\mathrm{MeV} \leq m_{Z'} \leq 1\mathrm{GeV}$

- ΔN_{eff} **M. Escudero et al, JHEP 2019**
  - Z' will reheat the neutrino gas, resulting in a higher expansion rate
  - Increase the effective number of neutrinos N_{eff}
  - $\Delta N_{\mathrm{eff}} < 0.5$
- ***BOREXINO*** **R. Harnik et al, JCAP 2012**
  - $\nu - e$ scattering

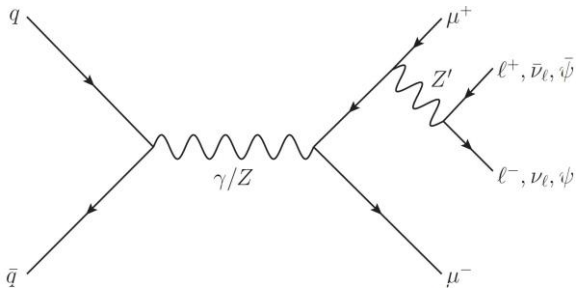
BaBar, LHC 4μ channels

BaBar Collaboration, PRD 2016

- $e^+e^- \to \mu^+\mu^- Z'$, $Z' \to \mu^+\mu^-$
  - Upper limit on g_X for $200\text{MeV} \leq M_{Z'} \leq 10\text{GeV}$

CMS Collaboration, PLB 2019

- The lowest order Z' production process at collider
  - Produce a charged lepton pair through Drell-Yan process
  - Z' is radiated from one of leptons



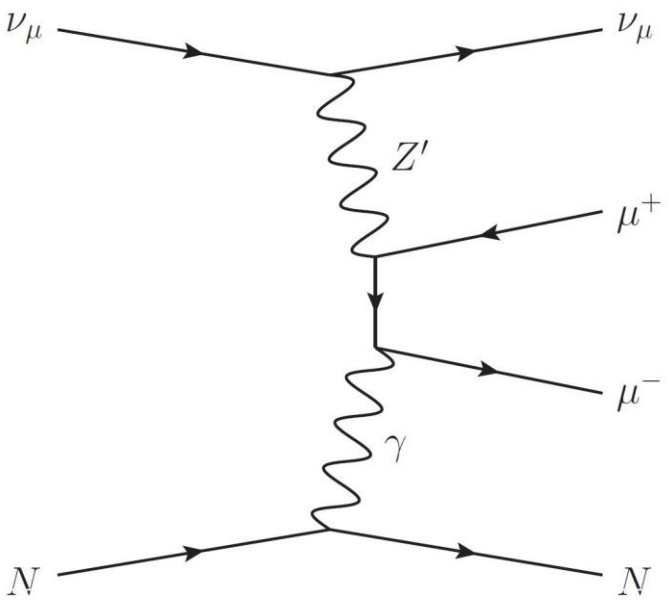
- Final states
  - two pair of charged-leptons
  - A pair of charged-lepton plus missing energy

Neutrino trident production

- Production of a muon pair from the scattering of a muon neutrino with heavy nuclei
  - $R_{\mathrm{CCFR}} \equiv \dfrac{\sigma_{\mathrm{CCFR}}}{\sigma_{\mathrm{SM}}} = 0.82 \pm 0.28.$

W. Altmannshofer et al, PRL 2014

- The leading order Z' contribution:



Borexino: $\nu - e$ scattering

- Borexino is a liquid scintillator experiment measuring solar neutrino scattering off electron
  - Probe non-standard interactions between neutrinos and target
  - Limits from Borexino for the $U(1)_{B-L}$ gauge boson have been derived.

R. Harnik et al, JCAP 2012

- Rescale the constraints on $U(1)_{B-L}$ boson as

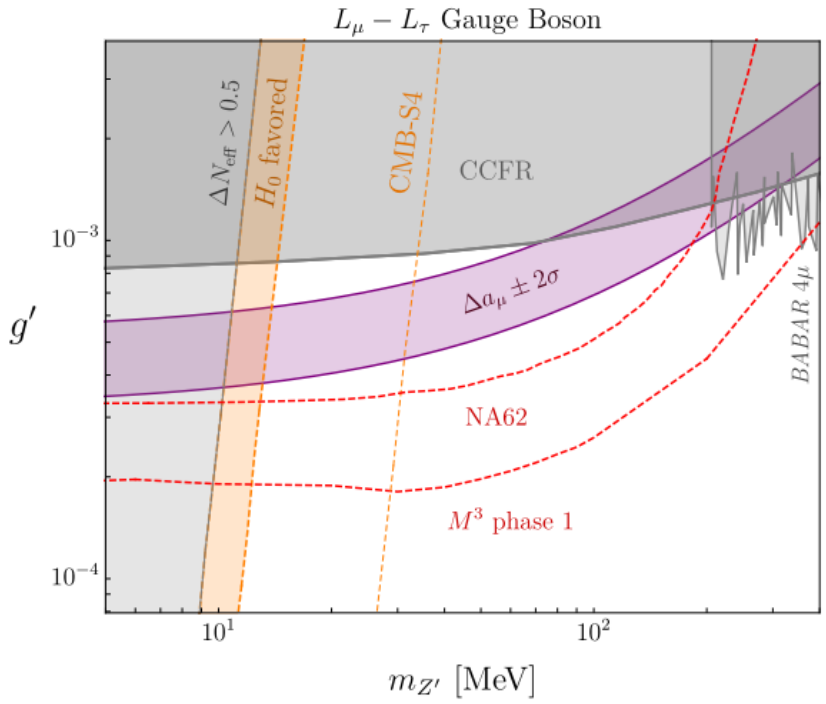
$$\alpha^2_{B-L} \to \begin{cases} \left[\sum_{i,j=1}^{3} f_i \left|(U^\dagger Q_{\mu e} U)_{ij}\right|^2\right]^{1/2} \alpha^2_{\mu e}\,, & \text{for} \quad \mathrm{U}(1)_{L_\mu - L_e}\,, \\ \left[\sum_{i,j=1}^{3} f_i \left|(U^\dagger Q_{e\tau} U)_{ij}\right|^2\right]^{1/2} \alpha^2_{e\tau}\,, & \text{for} \quad \mathrm{U}(1)_{L_e - L_\tau}\,, \\ \left[\sum_{i,j=1}^{3} f_i \left|(U^\dagger Q_{\mu\tau} U)_{ij}\right|^2\right]^{1/2} \alpha\, \alpha_{\mu\tau}\, \epsilon_{\mu\tau}(q^2)\,, & \text{for} \quad \mathrm{U}(1)_{L_\mu - L_\tau}\,, \end{cases}$$

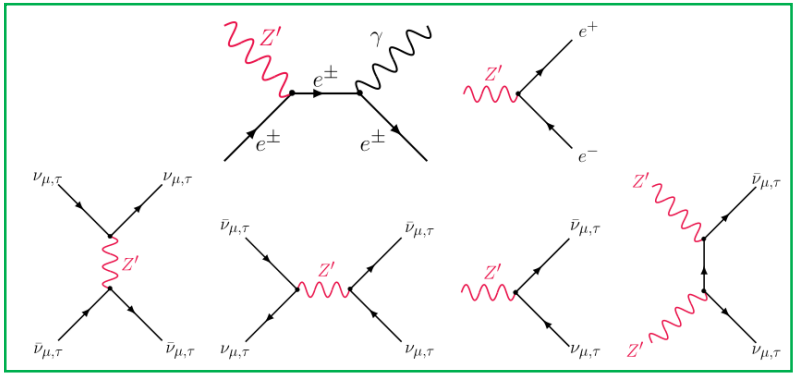
$$Q_{\mu\tau} = \mathrm{diag}(0, 1, -1)$$

CMB & Hubble tension

- Z' will reheat the neutrino gas
  - Resulting in a higher expansion rate
  - Increase the effective number of neutrinos $N_{\rm eff}$
- Taking into account kinetic mixing

M. Escudero et al, JHEP 2019





$U(1)_{L_\mu - L_\tau}$-charged DM model

- Conventional $U(1)_{L_\mu - L_\tau}$-charged fermion DM model

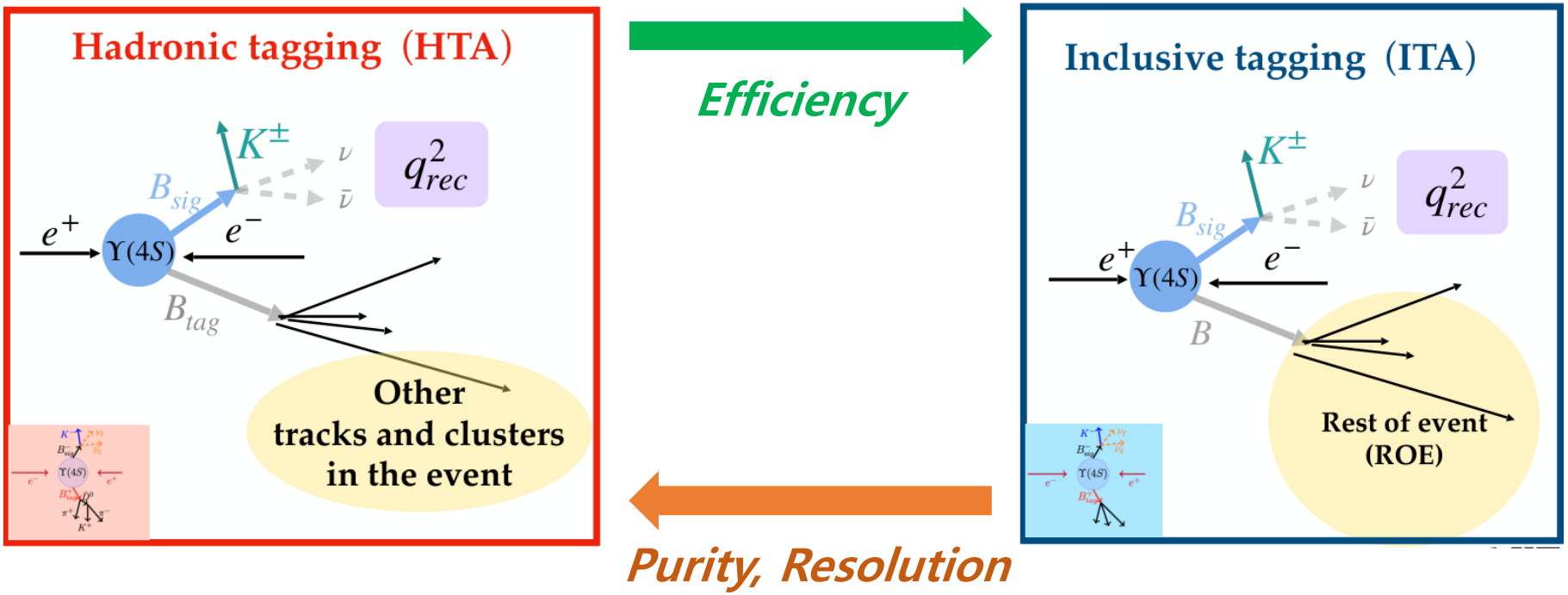
$$\mathcal{L} \supset \mathcal{L}_{\mathrm{SM}} - \frac{1}{4} Z'_{\alpha\beta} Z'^{\alpha\beta} + \frac{1}{2} m_{Z'}^2 Z'_\alpha Z'^\alpha + i\bar{\chi}\gamma^\alpha \partial_\alpha \chi - m_\chi \bar{\chi}\chi$$
$$+ g_X Q_\chi Z'_\alpha \bar{\chi}\gamma^\alpha \chi + g_X Z'_\alpha \sum Q_\ell \bar{\ell}\gamma^\alpha \ell$$

  - Dark Photon Z' plays a role of messenger particle between DM and the SM leptons
  - Dark Photon mass is generated by hand or Stueckelberg mechanism

- New parameters: $\{g_X, m_{Z'}, m_\chi, Q_\chi\}$
- Consider Z' boson only & **$g_X \sim (3-5) \times 10^{-4}$ for the muon g-2**
  - $\chi\bar{\chi}(X\bar{X}) \rightarrow f_{SM}\bar{f}_{SM}$: dominant annihilation channels
  - $g_X \sim 10^{-4}$ is too small to get $\Omega_\chi h^2 = 0.12$

Measurement of $B^+ \to K^+\nu\bar{\nu}$

- Two ways of tagging



- q^2_{rec}: mass squared of the neutrino pair
- Inclusive tagging: It allows one to reconstruct inclusively the decay $B^+ \to K^+\nu\bar{\nu}$ from the charged kaon

Measurement of $B^+ \to K^+ \nu\bar{\nu}$

- Challenges in reconstructing the events
  - Searches for $B \to K^{(*)} \nu\bar{\nu}$ have only been performed at the B factories Belle and BaBar

- Using the same techniques in Belle, BaBar
  - Semileptonic tagged analyses
  - Hadronic-tagged analyses

- Inclusive tag analysis (Belle & Belle II)
  - Allow one to reconstruct inclusively the decay $B^+ \to K^+ \nu\bar{\nu}$ from the charged kaon

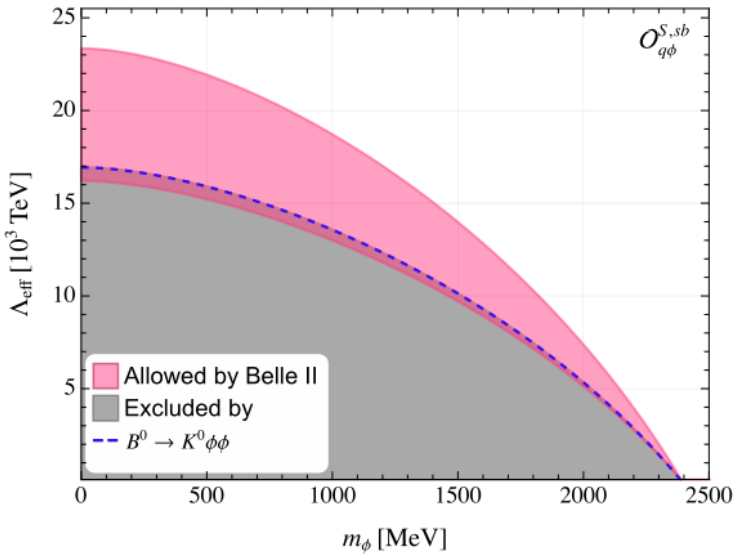
Solutions: EFT-approach

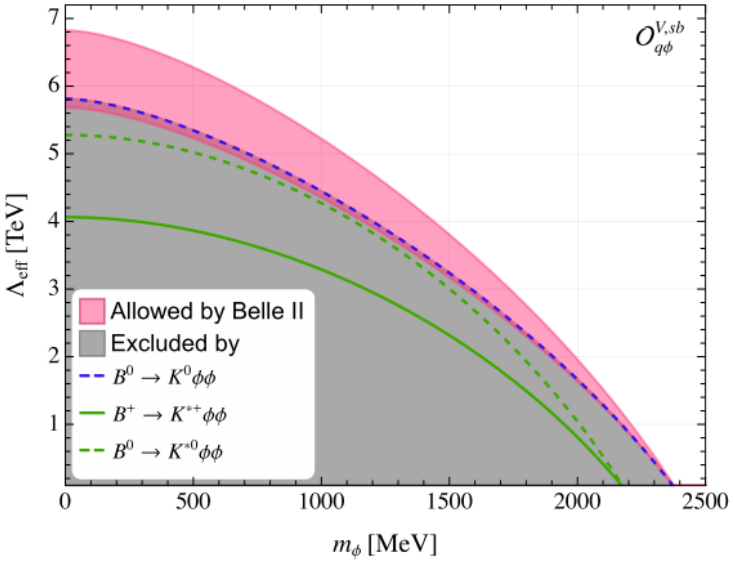
- Real/Complex scalar DM

X. He et al, 2309.12741

$$\mathcal{O}_{q\phi}^{S,sb} = (\bar{s}b)(\phi^\dagger\phi),$$

$$\mathcal{O}_{q\phi}^{V,sb} = (\bar{s}\gamma^\mu b)(\phi^\dagger i\overleftrightarrow{\partial_\mu}\phi), \ (\times)$$



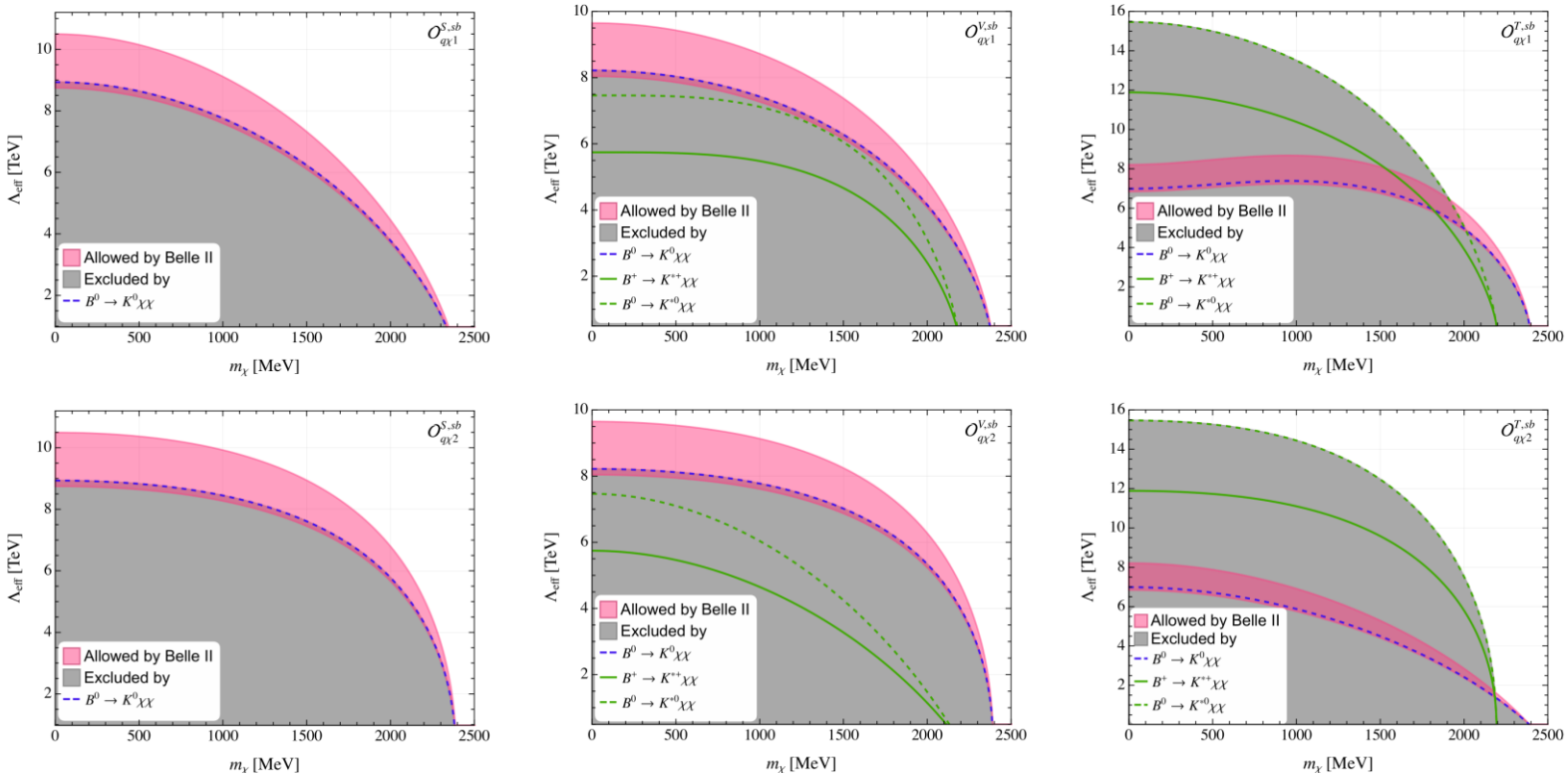


Solutions: EFT-approach

- Majorana/Dirac fermion DM

X. He et al, 2309.12741

$$\mathcal{O}^{S,sb}_{q\chi 1} = (\bar{s}b)(\bar{\chi}\chi), \qquad \mathcal{O}^{S,sb}_{q\chi 2} = (\bar{s}b)(\bar{\chi}i\gamma_5\chi),$$
$$\mathcal{O}^{V,sb}_{q\chi 1} = (\bar{s}\gamma^\mu b)(\bar{\chi}\gamma_\mu\chi), \ (\times) \qquad \mathcal{O}^{V,sb}_{q\chi 2} = (\bar{s}\gamma^\mu b)(\bar{\chi}\gamma_\mu\gamma_5\chi),$$
$$\mathcal{O}^{T,sb}_{q\chi 1} = (\bar{s}\sigma^{\mu\nu} b)(\bar{\chi}\sigma_{\mu\nu}\chi), \ (\times) \qquad \mathcal{O}^{T,sb}_{q\chi 2} = (\bar{s}\sigma^{\mu\nu} b)(\bar{\chi}\sigma_{\mu\nu}\gamma_5\chi), \ (\times)$$

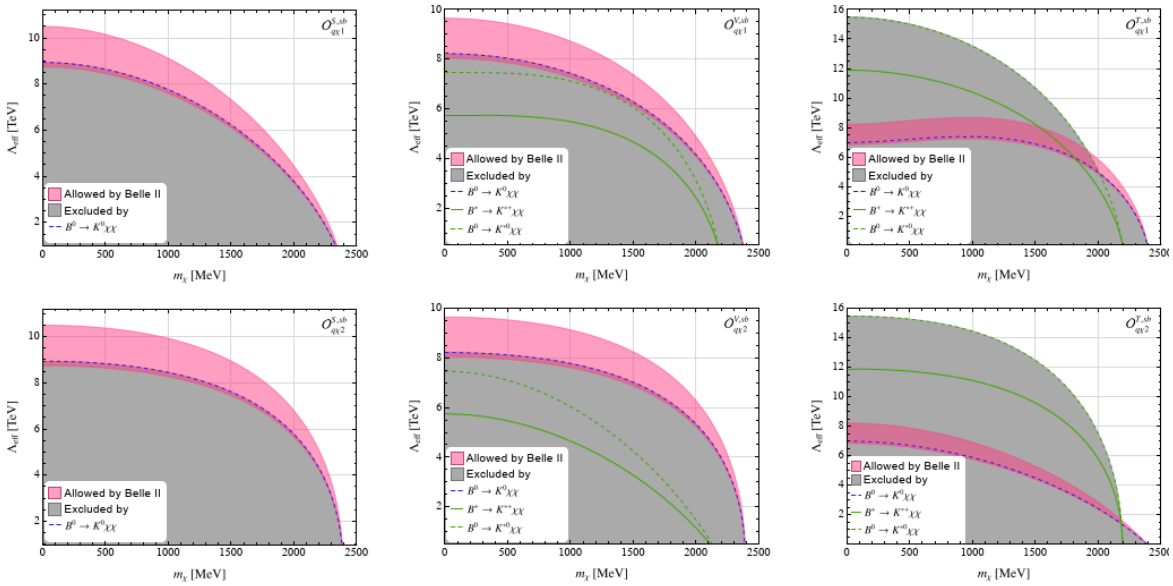


Solutions: EFT-approach

- Real/Complex vector DM

X. He et al, 2309.12741

$$\mathcal{O}_{qX}^{S,sb} = (\bar{s}b)(X_\mu^\dagger X^\mu),$$
$$\mathcal{O}_{qX1}^{T,sb} = \frac{i}{2}(\bar{s}\sigma^{\mu\nu}b)(X_\mu^\dagger X_\nu - X_\nu^\dagger X_\mu), \ (\times)$$
$$\mathcal{O}_{qX2}^{T,sb} = \frac{1}{2}(\bar{s}\sigma^{\mu\nu}\gamma_5 b)(X_\mu^\dagger X_\nu - X_\nu^\dagger X_\mu), \ (\times)$$
$$\mathcal{O}_{qX2}^{V,sb} = (\bar{s}\gamma_\mu b)\partial_\nu(X^{\mu\dagger}X^\nu + X^{\nu\dagger}X^\mu),$$
$$\mathcal{O}_{qX3}^{V,sb} = (\bar{s}\gamma_\mu b)(X_\rho^\dagger \overleftrightarrow{\partial_\nu} X_\sigma)\epsilon^{\mu\nu\rho\sigma},$$
$$\mathcal{O}_{qX4}^{V,sb} = (\bar{s}\gamma^\mu b)(X_\nu^\dagger i\overleftrightarrow{\partial_\mu} X^\nu), \ (\times)$$
$$\mathcal{O}_{qX5}^{V,sb} = (\bar{s}\gamma_\mu b)i\partial_\nu(X^{\mu\dagger}X^\nu - X^{\nu\dagger}X^\mu), \ (\times)$$
$$\mathcal{O}_{qX6}^{V,sb} = (\bar{s}\gamma_\mu b)i\partial_\nu(X_\rho^\dagger X_\sigma)\epsilon^{\mu\nu\rho\sigma}. \ (\times)$$



Solutions: 2-body decay

W. Altmannshofer et al, 2311.14629

- Light particle X
  - Light neutral vector boson Z'
  - Flavoured axions and ALPs

- Light → on-shell: $m_X < m_B - m_K$: $m_X = 2\ \mathrm{GeV}$
- Undetected particle X is stable, long-lived or decays invisibly
  - Couplings to electrons, muons, and light quarks should be absent or sufficiently small

- For $B \to K^* \nu\bar{\nu}$, only BaBar data is available, there is no excess seen
  - Use the $B \to K^* \nu\bar{\nu}$ measurements of BaBar to set an upper limit on $\mathrm{Br}(B \to K^* \nu\bar{\nu})$

Solutions: 2-body decay

- $B \to KZ'$ decay rate
  - $m_{Z'} = 2\text{GeV}$

$$\Gamma^{(4)}_{B\to KZ'} = \frac{|g_V^{(4)}|^2}{64\pi}\frac{m_B^3}{m_{Z'}^2}\lambda^{\frac{3}{2}} f_+ ,$$

$$\Gamma^{(5)}_{B\to KZ'} = \frac{|g_V^{(5)}|^2}{16\pi}\frac{m_B m_{Z'}^2}{\Lambda^2}\left(1+\frac{m_K}{m_B}\right)^{-2}\lambda^{\frac{3}{2}} f_T ,$$

$$\Gamma^{(6)}_{B\to KZ'} = \frac{|g_V^{(6)}|^2}{64\pi}\frac{m_B^3 m_{Z'}^2}{\Lambda^4}\lambda^{\frac{3}{2}} f_+ ,$$

W. Altmannshofer et al, 2311.14629

Including couplings up to dimension 6, the interaction Lagrangian is [47]

$$\mathcal{L}_{Z'} \supset \left\{ g_L^{(4)} Z'_\mu (\bar{s}\gamma^\mu P_L b) + \frac{g_L^{(5)}}{\Lambda} Z'_{\mu\nu}(\bar{s}\sigma^{\mu\nu} P_R b) + \frac{g_L^{(6)}}{\Lambda^2}\partial^\nu Z'_{\mu\nu}(\bar{s}\gamma^\mu P_L b) + \text{h.c.} \right\} + \{L \leftrightarrow R\}, \quad (2)$$

$$g_V^{(d)} = g_R^{(d)} + g_L^{(d)} \text{ and } g_A^{(d)} = g_R^{(d)} - g_L^{(d)}.$$

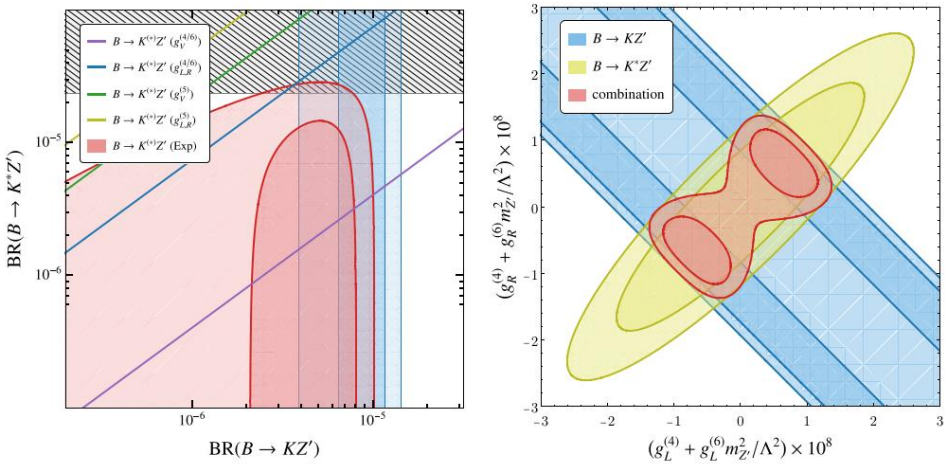


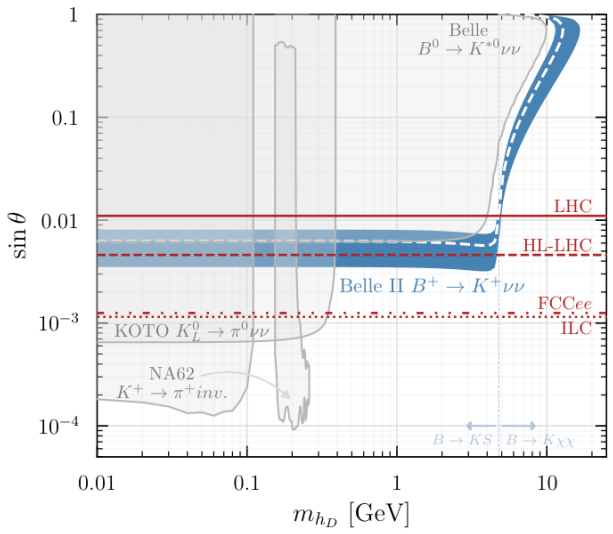
FIG. 2: *Left:* Correlations between $B \to KZ'$ and $B \to K^*Z'$ (colored lines) for the different $\bar{s}bZ'$ operators considered in this work. These are compared to the experimental data stemming from the combination of Belle-II, Babar and Belle measurements,which is represented by the red regions correspondingto $\Delta\chi^2 = 2.3$ and $\Delta\chi^2 = 6.18$. Belle's upper limit (hatched region at 2σ) and the new Belle II measurement (blue vertical band at 1σ and 2σ). *Right:* preferred regions in the $g_L - g_R$ plane. One can see that (approximately) vectorial couplings of the order of 10^{-8} are suggested by current data.

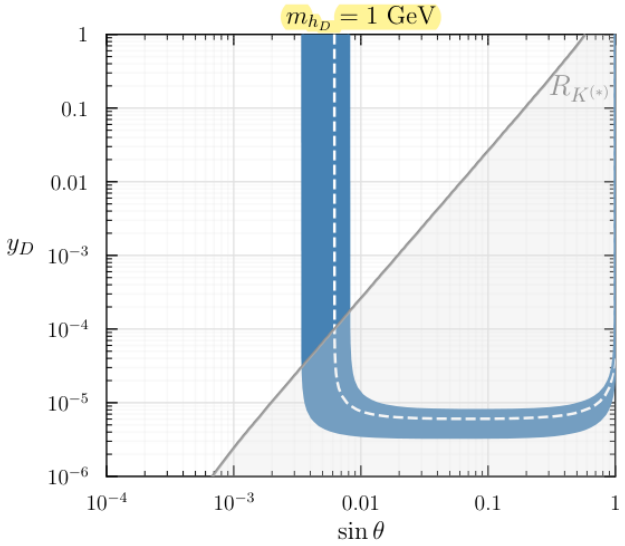
Solutions: 2- or 3-body decay

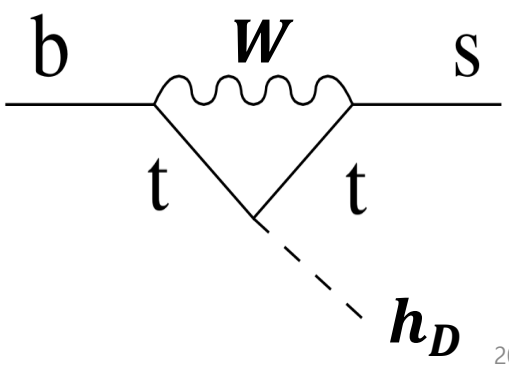
- Dark Higgs on-shell decay or three-body decay

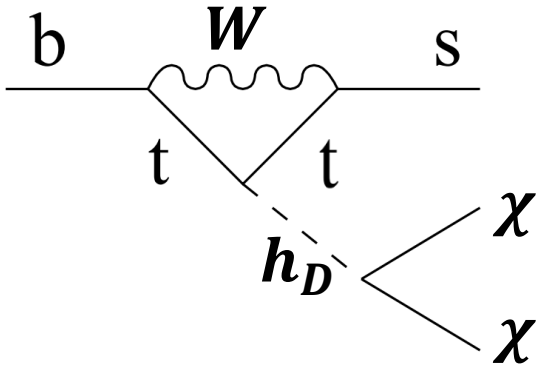
McKeen et al, 2312.00982

$$\mathcal{L}_{\rm DM} = y_D \phi \bar{\chi} \chi$$





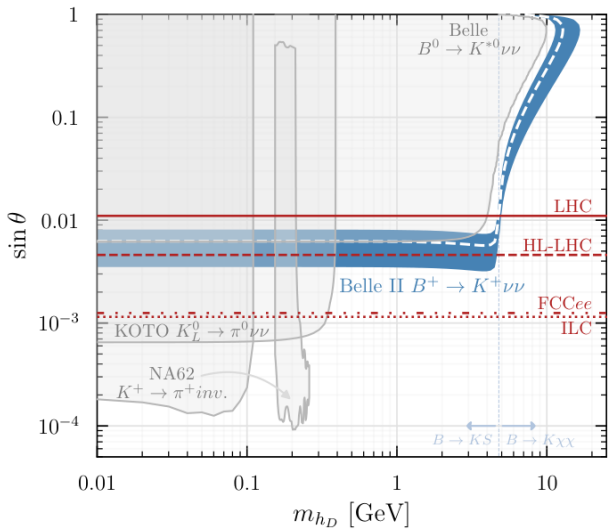


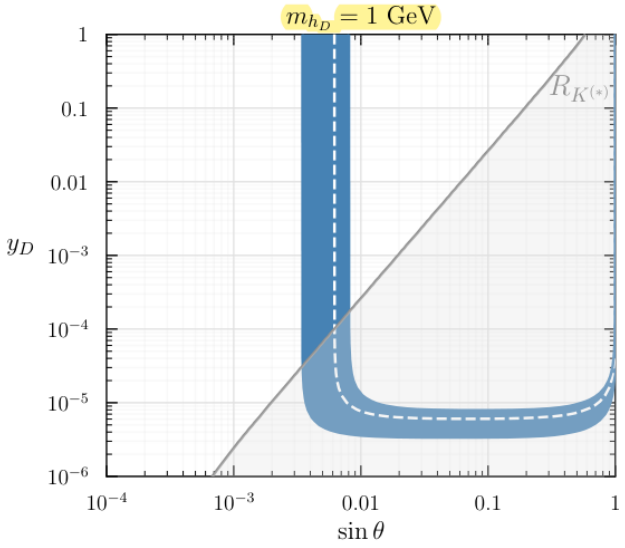


Solutions: 2- or 3-body decay

- Dark Higgs on-shell decay or three-body decay **McKeen et al, 2312.00982**

$$\mathcal{L}_{\rm DM} = y_D \phi \bar{\chi} \chi$$



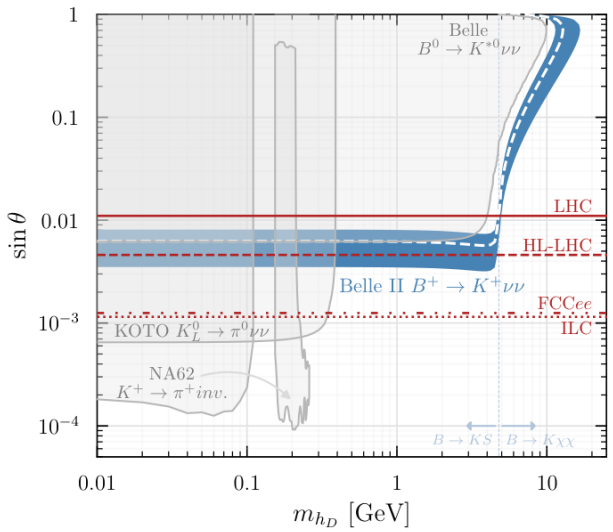


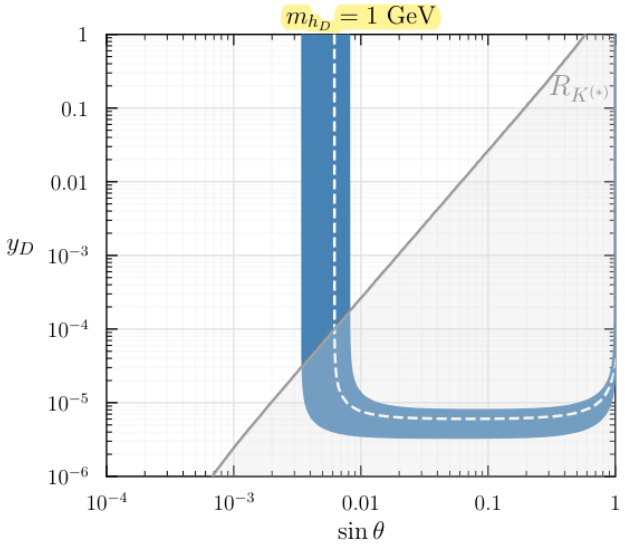
- **Extremely large relic density**
  - $\Omega h^2 \simeq 10^{20} \left(\frac{10^{-4}}{y_D}\right)^2 \left(\frac{\sin\theta}{10^{-3}}\right)^2 \left(\frac{m_\chi}{100\,\mathrm{MeV}}\right)^2 \left(\frac{1\,\mathrm{GeV}}{m_{H_1}}\right)^2$: overclose the Universe

Solutions: 2- or 3-body decay

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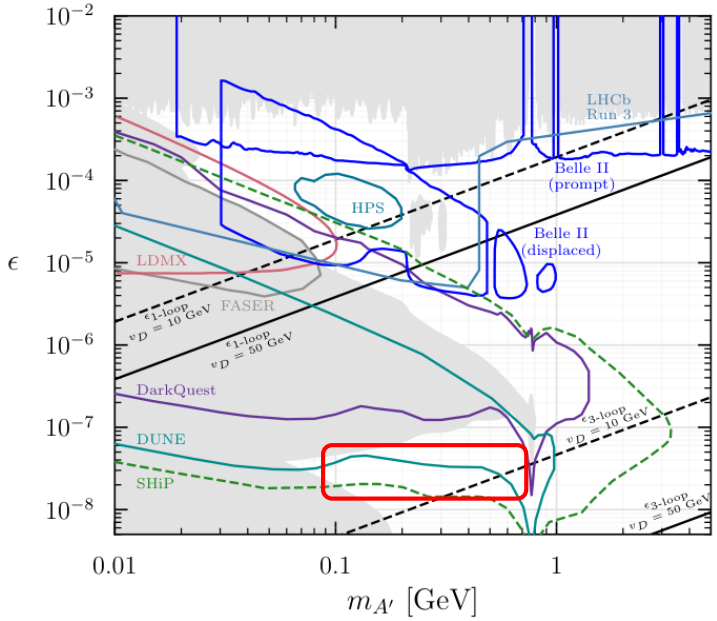
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  - Either introduce a new DM annihilation or allow DM to decay
  - In that sense, **fermion DM does not work…**

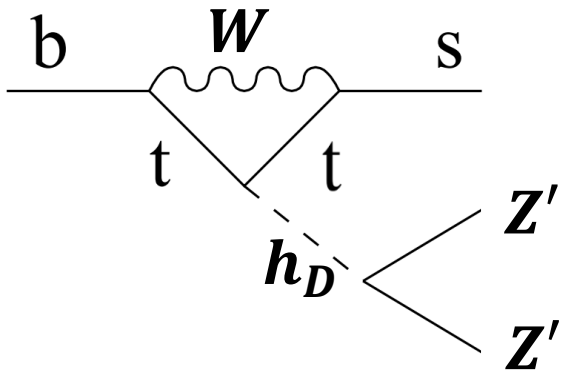
Solutions: 3-body decay

McKeen et al, 2312.00982

- Dark Higgs decays to dark Photon
  - Dark Photon can be long-lived → appear missing energy at BelleII
  - $\mathcal{L} \supset g_D^2 v_D A'_\mu A'^\mu (-h \sin\theta + h_D \cos\theta)$

- Two-regions for sub-GeV dark photon that unconstrained by existing experimental searches:





1. $m_{A_D} \gtrsim 100$ MeV with $10^{-8} \lesssim \epsilon \lesssim 10^{-7}$
2. $m_{A_D} \gtrsim 50$ MeV with $10^{-6} \lesssim \epsilon \lesssim 10^{-4}$.

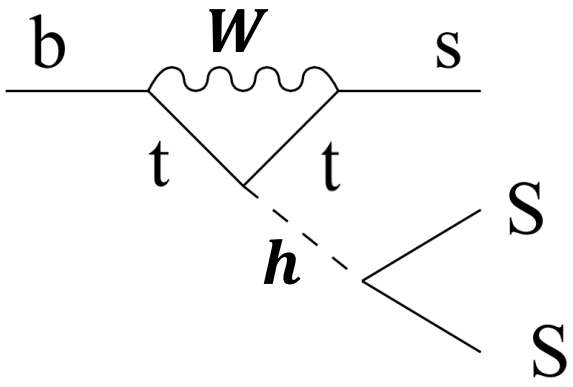
Solutions: 3-body decay

- Singlet scalar DM model ($m_s \leq 2.3\mathrm{GeV}$)

Bird et al, PRL 2004

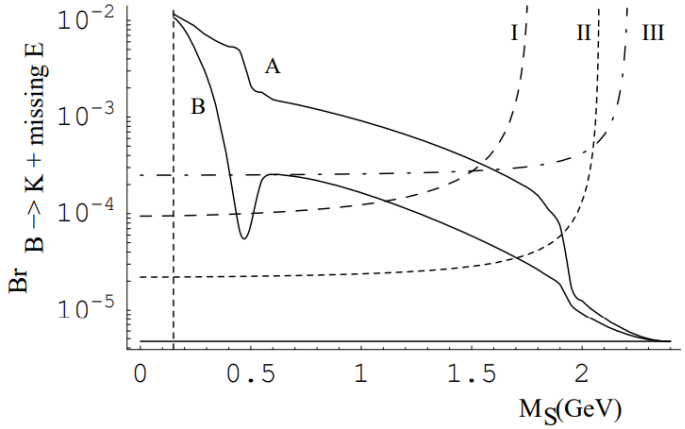
$$-\mathcal{L}_S = \frac{\lambda_S}{4}S^4 + \frac{m_0^2}{2}S^2 + \lambda S^2 H^\dagger H$$

$$= \frac{\lambda_S}{4}S^4 + \frac{1}{2}(m_0^2 + \lambda v_{EW}^2)S^2 + \boxed{\lambda v_{EW} S^2 h} + \frac{\lambda}{2}S^2 h^2,$$



- Belle ⇒ $\frac{C_{DM}}{C_\nu} \simeq \frac{4.4\lambda M_W^2}{g_W^2 m_h^2}$
- Relic density: $\sigma_{\mathrm{ann}} v_{\mathrm{rel}} = \frac{8 v_{EW}^2 \lambda^2}{m_h^4} \left(\lim_{m_{\tilde{h}} \to 2m_S} m_{\tilde{h}}^{-1} \Gamma_{\tilde{h}X} \right).$

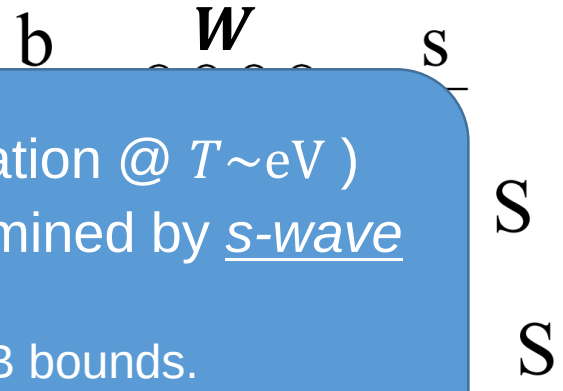
  - λ should be large to fit the relic as well as Belle II
  - $m_s \leq 1\mathrm{GeV}$ is already excluded by BABAR limits (2004 data).



Solutions: 3-body decay

- Singlet scalar DM model ($m_s \leq 2.3\mathrm{GeV}$)

Bird et al, PRL 2004



- For $m_\chi \lesssim 10\mathrm{GeV}$, CMB bound (DM annihilation @ $T \sim \mathrm{eV}$) excludes the thermal DM freeze-out determined by *s-wave* annihilation
- At that time, the authors did not consider the CMB bounds.
  This model does not work anymore.

- λ should be large to fit the relic as well as Belle II
- $m_s \leq 1\mathrm{GeV}$ is already excluded by BABAR limits (2004 data).

